## QUESTIONS:

1. In regression analysis, the equation that describes how the response variable $(y)$ is related to the explanatory variable $(x)$ is:
A. the correlation model.
B. the regression model.
C. used to compute the correlation coefficient.
D. none of these alternatives is correct.
2. A negative relationship between two variables means that if the independent variable increases, the dependent variable will
A. Not change
B. Increase
C. Decrease
D. Can't be predicted
3. The predicted rate of response of the dependent variable to changes in the independent variable is called:
A. Slope
B. Intercept
C. Error
D. Regression equation
4. Regression analysis was applied to return rates of sparrow-hawk colonies. Regression analysis was used to study the relationship between return rate ( x : \% of birds that return to the colony in a given year) and immigration rate ( $\mathrm{y}: \%$ of new adults that join the colony per year). The following regression equation was obtained.

$$
y=31.9-0.34 x
$$

Based on the above estimated regression equation, if the return rate were to decrease by $10 \%$ the rate of immigration to the colony would:
A. increase by $34 \%$
B. increase by $3.4 \%$
C. decrease by $0.34 \%$
D. decrease by 3.4\%
5. Which one of the following statements about time-series forecasting is true?
A. Forecasting is based on the future.
B. The analysis of past demand helps predict future demand.
C. It makes extensive use of the data collected in the qualitative approach.
D. Because it accounts for trends, cycles, and seasonal patterns, it is more powerful than causal forecasting.
6. The fundamental difference between cycles and seasonality is the
A. duration of the repeating patterns
B. magnitude of the variation
C. ability to attribute the pattern to a cause
D. all of the above
7. The rise and fall of a time series over periods longer than one year is called:
A. Secular trend.
B. Seasonal variation.
C. Cyclical variation.
D. Irregular variation.
8. The general pattern of increase or decrease in economics or social phenomena is shown by:
A. Seasonal trend.
B. Cyclical trend.
C. Secular trend.
D. Irregular trend.
9. The following table contains the number of complaints received in a department store for the first 6 months of last year.

| Month | Complaints |  |  |  |
| :---: | :---: | :--- | :--- | :--- |
| January | 36 |  |  |  |
| February | 45 |  |  |  |
| March | 81 |  |  |  |
| April | 90 |  |  |  |
| May | 108 |  |  |  |
| June | 144 |  |  |  |
|  |  |  |  |  |

Using the given data above, formulate the trend equation using the method of least squares
A. $\hat{y}=31.29+21.09 x$
B. $\hat{y}=-0.35+0.05 x$
C. $\hat{y}=10.2+21.09 x$
D. None of the above
10. Six friends play regularly in a chess club. The number of games that each person has won is recorded in the table below.

| Player | Games won | Games lost |
| :---: | :---: | :---: |
| Tom | 5 | 10 |
| Andy | 7 | 3 |
| Daniel | 3 | 9 |
| Rachel | 4 | 16 |
| Maria | 6 | 14 |
| Charles | 12 | 6 |

If Maria played against Tom, who do you think would be most likely to win?
A. The probability of a win for Maria is $43 \%$ and for Tom $50 \%$, therefore Tom would be most likely to win
B. Maria won more games than Tom, therefore Maria would be most likely to win
C. The probability of a win for Maria is $30 \%$ and for Tom $29 \%$, therefore Maria would be most likely to win
D. The probability of a win for Maria is $30 \%$ and for Tom $33 \%$, therefore Tom would be most likely to win
11. Below is a table showing the country of origin of visitors to some tourist destinations in Gauteng. Complete the table and answer the following questions.

|  | Tourist destination |  |  |
| :---: | :---: | :---: | :---: |
| Country of origin | Gold Reef City | Lost City | Total |
| UK | 300 | 500 |  |
| Germany | 250 |  | 550 |
| USA | 350 | 400 | 750 |
| Total | 900 |  | 2100 |

What is the most popular destination?
A. Gold Reef City
B. United Kingdom
C. Lost City
D. USA
12. With reference to Question 11: If a visitor is selected at random, what is the probability the visitor is from the USA or goes to the Lost City?
A. 0.9286
B. 0.7381
C. 0.5476
D. 0.3571
13. With reference to Question 11: If a visitor is selected at random, what is the probability that helshe visited Gold Reef City, given that the visitor is from Germany?
A. 0.4545
B. 0.2778
C. 0.1190
D. 0.0510
14. Outside a house there is a keypad that can be used to open the garage door if the correct four digit code (from 0 to 9 ) is entered. How many codes are possible?
A. 40
B. 210
C. 5040
D. 151200
15. A Cape Town courier service promises that $80 \%$ of Johannesburg-bound parcel deliveries will reach their destinations within 12 hours. What is the probability that of 7 parcels sent at random times by a particular client in Cape Town:

Only 1 will be delivered late
A. 0.0000002
B. 0.00036
C. 0.2062
D. 0.3670
16. With reference to Question 15: Only one will be delivered within 12 hours
A. 0.00036
B. 0.2684
C. 0.0056
D. 0.0141
17. A telephone help line receives calls that can be described by the Poisson distribution. The average rate at which calls come in is 2 calls per minute. The probability that the help-line will receive exactly five calls in 30 seconds is
A. 0.0361
B. 0.9969
C. 0.0031
D. 0.00028
18. The normal probability distribution is symmetrical around the
A. Tails
B. $x$-axis
C. mean
D. area to the right of the mean
19. The cost of treatment per patient for a certain medical problem was modelled by one insurance company as a normal random variable with a mean of R775 and standard deviation of R150.

What is the probability that the treatment cost of a patient is less than R1 000?
A. 0.0668
B. 0.4332
C. 0.9332
D. 0.9525
20. With reference to Question 19: What is the probability that the treatment cost of a patient is more than R1 000?
A. 0.0668
B. 0.4332
C. 0.5668
D. 0.9332
21. With reference to Question 19: The $30 \%$ of the patients, whose treatment costs are the lowest, pay less than how much?
A. R649
B. R697
C. R853
D. R901
22. With reference to Question 19: What is the probability that the treatment cost of a patient is between R600 and R700?
A. 0.1875
B. 0.2486
C. 0.3125
D. 0.5705
23. An estimate of a population parameter that provides an interval of values believed to contain the value of the parameter is known as the
A. Confidence level
B. Interval estimate
C. Parameter value
D. Population estimate
24. Which of the following statements completes the following statement correctly? The larger the level of confidence used in constructing a confidence interval estimate of the population mean:
A. The smaller the probability that the confidence interval will contain the population mean
B. The narrower the confidence interval
C. The wider the confidence interval
D. The more the width of the confidence interval remains the same
25. A random sample of size 15 taken from a normally distributed population revealed a sample mean of 75 and a sample variance of 25 . The margin of error of a $95 \%$ confidence interval for the population would equal:
A. 2.77
B. 1.29
C. 1.96
D. 13.84
26. From a random sample of 500 registered voters in South Africa, 400 indicated that they would vote in favor of a proposed policy in an upcoming election. The $98 \%$ confidence interval estimate for the population proportion in favor of this policy is:
A. $75.83 \%<\pi<84.17 \%$
B. $76.33 \%<\pi<83.67 \%$
C. $76.49 \%<\pi<83.51 \%$
D. $78.21 \%<\pi<81.79 \%$
27. An advertising agency would like to create an advertisement for a fast food restaurant claiming that the average waiting time from ordering to receiving your order at the restaurant is less than 5 minutes. The agency measured the time from ordering to delivery for 25 customers and found that the average time was 4.7 minutes with a standard deviation of 0.6 minutes. At the $5 \%$ level of significance, the confidence interval estimate for the average time between ordering and receiving the order is
A. $4.7 \pm 0.2053$
B. $4.7 \pm 0.2352$
C. $4.7 \pm 0.2477$
D. $4.7 \pm 0.2572$
28. The manufacturer of a new chewing gum claims that $80 \%$ of dentists surveyed prefer their type of gum and recommend it for their patients who chew gum. An independent consumer research firm decides to test their claim since the distribution company believes the number of patients who prefer the dentist's type of gum is higher than claimed. The findings in a sample of dentists indicate that 210 of the 250 respondents do actually prefer their gum.

If the null and the alternative hypothesis are: $\mathrm{H}_{0}: \pi=0.8 ; \mathrm{H}_{\mathrm{a}}: \pi>0.8$, the rejection region for the $\mathrm{H}_{0}$ at a $2 \%$ level of significance will be
A. If $z$-test statistic is more than 0.48
B. If $z$-test statistic is more than 2.05
C. If $z$-test statistic is more than 1.96 or less than -1.96
D. If the $z$-test statistic is more than 2.33 or less than -2.33
29. With reference to Question 28: The z-test statistic value will be
A. -1.73
B. -1.58
C. 1.58
D. 7.90
30. With reference to Question 28: If the test statistic falls in the acceptance region, the decision will be
A. Do not reject $H_{0}$. There is evidence to suggest that a higher number of patients prefer the dentist's type of gum.
B. Do not reject $\mathrm{H}_{0}$. There is no evidence to suggest that a higher number of patients prefer the dentist's type of gum.
C. Reject $\mathrm{H}_{0}$. There is no evidence to suggest that a higher number of patients prefer the dentist's type of gum
D. Reject $H_{0}$. There is evidence to suggest that a higher number of patients prefer the dentist's type of gum.

## FORMULAE SHEET:

$$
\begin{aligned}
& r=\frac{n \sum x y-\sum x \sum y}{\sqrt{\left[n \sum x^{2}-\left(\sum x\right)^{2}\left\lfloor n \sum y^{2}-\left(\sum y\right)^{2}\right.\right.}} \quad Z=\frac{x-\mu}{\sigma} \\
& r^{\prime}=1-\frac{6\left(d^{2}\right)}{n\left(n^{2}-1\right)} \\
& \hat{y}=a+b X \\
& b=\frac{n \sum x y-\sum x \sum y}{n \sum x^{2}-\left(\sum x\right)^{2}} \\
& a=\frac{\sum y}{n}-b \frac{\sum x}{n} \\
& \mathrm{P}(A \text { or } B)=\mathrm{P}(A)+\mathrm{P}(B) \\
& \mathrm{P}(A \text { or } B)=\mathrm{P}(A)+\mathrm{P}(B)-\mathrm{P}(A \text { and } B) \\
& \mathrm{P}(A \text { and } B)=\mathrm{P}(A) \cdot \mathrm{P}(B) \\
& \mathrm{P}(A \text { and } B)=\mathrm{P}(A) \cdot \mathrm{P}(B \backslash A) \\
& \mathrm{n} \times \mathrm{m} \times \\
& { }_{n} C_{x}=\frac{n!}{x!(n-x)!} \\
& { }_{n} P_{x}=\frac{n!}{(n-x)!} \\
& \mathrm{n}=\frac{\mathrm{z}^{2} \times \pi(1-\pi)}{\mathrm{E}^{2}} \\
& \mathrm{n}=\left(\frac{\mathrm{Z} \times \sigma}{\mathrm{E}}\right)^{2} \\
& P(x)=\frac{n!}{x!(n-x)!} \cdot \pi^{x} \cdot(1-\pi)^{n-x}
\end{aligned}
$$

QUANTITATIVE TECHNIQUES B, STAQTB1, STAQ1B1, 2022, PAPER C

TABLE OF THE STANDARD NORMAL (z) DISTRIBUTION

| Z | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0 | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| 0.1 | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| 0.2 | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | 0.1026 | 0.1064 | 0.1103 | 0.1141 |
| 0.3 | 0.1179 | 0.1217 | 0.1255 | 0.1293 | 0.1331 | 0.1368 | 0.1406 | 0.1443 | 0.1480 | 0.1517 |
| 0.4 | 0.1554 | 0.1591 | 0.1628 | 0.1664 | 0.1700 | 0.1736 | 0.1772 | 0.1808 | 0.1844 | 0.1879 |
| 0.5 | 0.1915 | 0.1950 | 0.1985 | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| 0.6 | 0.2257 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | 0.2881 | 0.2910 | 0.2939 | 0.2967 | 0.2995 | 0.3023 | 0.3051 | 0.3078 | 0.3106 | 0.3133 |
| 0.9 | 0.3159 | 0.3186 | 0.3212 | 0.3238 | 0.3264 | 0.3289 | 0.3315 | 0.3340 | 0.3365 | 0.3389 |
| 1.0 | 0.3413 | 0.3438 | 0.3461 | 0.3485 | 0.3508 | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| 1.1 | 0.3643 | 0.3665 | 0.3686 | 0.3708 | 0.3729 | 0.3749 | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| 1.2 | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | 0.3997 | 0.4015 |
| 1.3 | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.4207 | 0.4222 | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| 2.0 | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| 2.1 | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| 2.2 | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| 2.3 | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| 2.4 | 0.4918 | 0.4920 | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| 2.5 | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| 2.6 | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| 2.7 | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| 2.8 | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| 2.9 | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3.0 | 0.4987 | 0.4987 | 0.4987 | 0.4988 | 0.4988 | 0.4989 | 0.4989 | 0.4989 | 0.4990 | 0.4990 |
| 3.1 | 0.4990 | 0.4991 | 0.4991 | 0.4991 | 0.4992 | 0.4992 | 0.4992 | 0.4992 | 0.4993 | 0.4993 |

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THE CHI-SQUARE DISTRIBUTION TABLE

| dflarea | . 100 | . 050 | . 025 | . 010 | . 005 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2.70554 | 3.84146 | 5.02389 | 6.63490 | 7.87944 |
| 2 | 4.60517 | 5.99146 | 7.37776 | 9.21034 | 10.59663 |
| 3 | 6.25139 | 7.81473 | 9.34840 | 11.34487 | 12.83816 |
| 4 | 7.77944 | 9.48773 | 11.14329 | 13.27670 | 14.86026 |
| 5 | 9.23636 | 11.07050 | 12.83250 | 15.08627 | 16.74960 |
| 6 | 10.64464 | 12.59159 | 14.44938 | 16.81189 | 18.54758 |
| 7 | 12.01704 | 14.06714 | 16.01276 | 18.47531 | 20.27774 |
| 8 | 13.36157 | 15.50731 | 17.53455 | 20.09024 | 21.95495 |
| 9 | 14.68366 | 16.91898 | 19.02277 | 21.66599 | 23.58935 |
| 10 | 15.98718 | 18.30704 | 20.48318 | 23.20925 | 25.18818 |
| 11 | 17.27501 | 19.67514 | 21.92005 | 24.72497 | 26.75685 |
| 12 | 18.54935 | 21.02607 | 23.33666 | 26.21697 | 28.29952 |
| 13 | 19.81193 | 22.36203 | 24.73560 | 27.68825 | 29.81947 |
| 14 | 21.06414 | 23.68479 | 26.11895 | 29.14124 | 31.31935 |
| 15 | 22.30713 | 24.99579 | 27.48839 | 30.57791 | 32.80132 |
| 16 | 23.54183 | 26.29623 | 28.84535 | 31.99993 | 34.26719 |
| 17 | 24.76904 | 27.58711 | 30.19101 | 33.40866 | 35.71847 |
| 18 | 25.98942 | 28.86930 | 31.52638 | 34.80531 | 37.15645 |
| 19 | 27.20357 | 30.14353 | 32.85233 | 36.19087 | 38.58226 |
| 20 | 28.41198 | 31.41043 | 34.16961 | 37.56623 | 39.99685 |
| 21 | 29.61509 | 32.67057 | 35.47888 | 38.93217 | 41.40106 |
| 22 | 30.81328 | 33.92444 | 36.78071 | 40.28936 | 42.79565 |
| 23 | 32.00690 | 35.17246 | 38.07563 | 41.63840 | 44.18128 |
| 24 | 33.19624 | 36.41503 | 39.36408 | 42.97982 | 45.55851 |
| 25 | 34.38159 | 37.65248 | 40.64647 | 44.31410 | 46.92789 |
| 26 | 35.56317 | 38.88514 | 41.92317 | 45.64168 | 48.28988 |
| 27 | 36.74122 | 40.11327 | 43.19451 | 46.96294 | 49.64492 |
| 28 | 37.91592 | 41.33714 | 44.46079 | 48.27824 | 50.99338 |
| 29 | 39.08747 | 42.55697 | 45.72229 | 49.58788 | 52.33562 |

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| df | CRITICAL VALUES OF STUDENTS T DISTRIBUTION |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1-tailed |  |  |  |  |  |
|  | . 10 | . 05 | . 025 | . 01 | . 005 | . 0005 |
|  | 2-tailed test |  |  |  |  |  |
|  | . 20 | . 10 | . 05 | . 02 | . 01 | . 001 |
| 1 | 3.078 | 6.314 | 12.706 | 31.821 | 63.657 | 636.619 |
| 2 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 | 31.598 |
| 3 | 1.683 | 2.353 | 3.182 | 4.5415 | 5.841 | 12.941 |
| 4 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 | 8.610 |
| 5 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 | 6.859 |
| 6 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 | 5.959 |
| 7 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 | 5.405 |
| 8 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 | 5.041 |
| 9 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 | 4.781 |
| 10 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 | 4.587 |
| 11 | 1.363 | 1.796 | 2.201 | 2.718 | 3.106 | 4.437 |
| 12 | 1.356 | 1.782 | 2.179 | 2.681 | 3.055 | 4.318 |
| 13 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 | 4.221 |
| 14 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 | 4.140 |
| 15 | 1.341 | 1.753 | 2.131 | 2.602 | 2.947 | 4.073 |
| 16 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 | 4.015 |
| 17 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 | 3.965 |
| 18 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 | 3.922 |
| 19 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 | 4.883 |
| 20 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 | 3.850 |
| 21 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 | 3.819 |
| 22 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 | 3.792 |
| 23 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 | 3.767 |
| 24 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 | 3.745 |
| 25 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 | 3.725 |
| 26 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 | 3.707 |
| 27 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 | 3.690 |
| 28 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 | 3.674 |
| 29 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 | 3.659 |
| 30 | 1.310 | 1.697 | 2.042 | 2.457 | 2.750 | 3.646 |

