

| PROGRAM | $:$ BACHELOR OF TECHNOLOGY |
| :--- | :--- |
|  | CHEMICAL ENGINEERING |
| $\underline{\text { SUBJECT }}$ | $:$ TRANSFER PROCESSES 2A |
| $\underline{\text { CODE }}$ | $:$ TPRCHA2 |
| $\underline{\text { DATE }}$ | $:$ SUMMER SSA EXAMINATION |
|  | $:\left(\begin{array}{l}\text { DURATION } \\ \underline{\text { WEIGHT }}\end{array}\right.$ |
| $\underline{\text { TOTAL MARKS }}$ | $: 72: 60$ |

EXAMINER(S) : DR R HUBERTS
MODERATOR : MRS N SEEDAT
NUMBER OF PAGES : 11 PAGES

REQUIREMENTS : Use of scientific (non-programmable) calculator is permitted (only one per candidate)

## HINTS AND INSTRUCTIONS TO CANDIDATE(S):

- ATTEMPT ALL QUESTIONS. Please answer each question to the best of your ability.
- Write your details (module name and code, ID number, student number etc.) on script(s).
- Number each question clearly; questions may be answered in any order.
- Make sure that you read each question carefully before attempting to answer the question.
- Transfer the answers accurately onto Blackboard (Bb).


## Question One

[Total: 12 Marks]


Consider a cube of dimension $\mathrm{d}=1 \mathrm{~cm}$, temperature 400 K , emissivity 0.8 and absorptivity 0.9 hanging in a room where the air temperature is 300 K and the wall, ceiling and floor are at 310 K . The relevant heat transfer coefficient is 10 $\mathrm{Wm}^{-2} \mathrm{~K}^{-1} .1 .1$. Calculate the percentage of the total heat that is lost from the cube surface due to convection.
1.2. What will happen to the temperature of the block with time? Explain.

## Question Two

[Total: 34 Marks]
$0.01 \mathrm{kgs}^{-1}$ of a pharmaceutical liquid, consisting mainly of water (assume same physical properties), is to be sterilized by heating from 300 K to 350 K in a straight 0.02 m internal diameter stainless-steel tube. For this tube, a uniform surface temperature of 373 K is maintained by steam condensing on the outer surface of the tube. Thermal resistance of the tube wall may be neglected, and fully developed velocity and temperature profiles may be assumed.
2.1. Is the steam temperature constant? Explain.
2.2. Draw an annotated diagram in your script and estimate the length of the tube.
2.3. What type of heat is used to increase the liquid temperature?

## Question Three

[Total: 10 Marks]
Acetone diffuses through air at 273 K in an equimolar counter current flow mode through a cylinder of length 1 m and diameter increasing gradually from 0.1 m to 0.2 m . The drop in acetone concentration from the inlet to the outlet of the cylinder is $5 \mathrm{molm}^{-3}$. What is the steady state diffusion rate of the acetone?

Question Four
[Total: 16 Marks]


Carbon dioxide is stored in an elevated square rubber tank with wall thickness 0.01 m and dimensions $2 \mathrm{~m} \times 3 \mathrm{~m} \times 1 \mathrm{~m}$ high at an absolute pressure of 200 kPa . Neglect the concentration of carbon dioxide in the air next to the tank and estimate how much carbon dioxide is lost from the tank in $\mathrm{gd}^{-1}$ due to diffusion through all six surfaces in total.
[16]

## END

## Data Sheets

## Lengths, areas and volumes:

Circumference of a circle $\pi d$
Area of a cylinder $\pi \mathrm{dL}$
Area of a circle $\pi \mathrm{d}^{2} / 4$
Surface area of a sphere $\pi \mathrm{d}^{2}$
Volume of a sphere $\pi d^{3} / 6$

## Heat transfer data:

Table 1.1 Typical values of the convection heat transfer coefficient

| Process | $h$ <br> $\left(\mathbf{W} / \mathbf{m}^{2} \cdot \mathbf{K}\right)$ |
| :--- | :---: |
| Free convection |  |
| $\quad$ Gases |  |
| $\quad$ Liquids | $2-25$ |
| Forced convection | $50-1000$ |
| $\quad$ Gases |  |
| $\quad$ Liquids |  |
| Convection with phase change | $25-250$ |
| $\quad$ Boiling or condensation | $100-20,000$ |

Table 1.5 Summary of heat transfer processes

| Mode | Mechanism(s) | Rate Equation | Equation <br> Number | Transport <br> Property or <br> Coefficient |
| :--- | :--- | :--- | :--- | :--- |
| Conduction | Diffusion of energy due <br> to random molecular <br> motion | $q_{x}^{\prime \prime}\left(\mathrm{W} / \mathrm{m}^{2}\right)=-k \frac{d T}{d x}$ | $(1.1)$ | $k(\mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$ |
| Convection | Diffusion of energy due <br> to random molecular <br> motion plus energy <br> transfer due to bulk | $q^{\prime \prime}\left(\mathrm{W} / \mathrm{m}^{2}\right)=h\left(T_{s}-T_{\infty}\right)$ | $(1.3 \mathrm{a})$ | $h\left(\mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$ |
| Radiation | motion (advection $)$ <br> Energy transfer by <br> electromagnetic waves | $q^{\prime \prime}\left(\mathrm{W} / \mathrm{m}^{2}\right)=\varepsilon \sigma\left(T_{s}^{4}-T_{\text {surf }}^{4}\right)$ <br> or $q(\mathrm{~W})=h_{r} A\left(T_{s}-T_{\text {sur }}\right)$ | $(1.7)$ <br> $(1.8)$ | $\varepsilon$ <br> $h_{r}\left(\mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$ |

Table 6.2 Selected dimensionless groups of heat and mass transfer

| Group | Definition | Interpretation |
| :---: | :---: | :---: |
| Biot number (Bi) | $\frac{h L}{k_{\mathrm{s}}}$ | Ratio of the internal thermal resistance of a solid to the boundary layer thermal resistance. |
| Mass transfer Biot number ( $B i_{m}$ ) | $\frac{h_{m} L}{D_{\mathrm{AB}}}$ | Ratio of the internal species transfer resistance to the boundary layer species transfer resistance. |
| Bond number ( Bo ) | $\frac{g\left(\rho_{i}-\rho_{v}\right) L^{2}}{\sigma}$ | Ratio of gravitational and surface tension forces. |
| Coefficient of friction $\left(C_{f}\right)$ | $\frac{\tau_{s}}{\rho V^{2} / 2}$ | Dimensionless surface shear stress. |
| Eckert number (Ec) | $\frac{V^{2}}{c_{p}\left(T_{s}-T_{\infty}\right)}$ | Kinetic energy of the flow relative to the boundary layer enthalpy difference. |
| Fourier number (Fo) | $\frac{\alpha t}{L^{2}}$ | Ratio of the heat conduction rate to the rate of thermal energy storage in a solid. Dimensionless time. |
| Mass transfer Fourier number ( $\mathrm{Fo}_{\mathrm{m}}$ ) | $\frac{D_{\mathrm{AB}} t}{L^{2}}$ | Ratio of the species diffusion rate to the rate of species storage. Dimensionless time. |
| Friction factor $(f)$ | $\frac{\Delta p}{(L D)\left(\rho u_{m}^{2} / 2\right)}$ | Dimensionless pressure drop for internal flow. |
| Grashof number $\left(G r_{L}\right)$ | $\frac{g \beta\left(T_{s}-T_{\infty}\right) L^{3}}{\nu^{2}}$ | Ratio of buoyancy to viscous forces. |
| Colburn $j$ factor $\left(j_{H}\right)$ | St $P r^{2 / 3}$ | Dimensionless heat transfer coefficient. |
| Colburn $j$ factor ( $j_{m}$ ) | $S t_{m} S c^{2 / 3}$ | Dimensionless mass transfer coefficient. |
| Jakob number (Ja) | $\frac{c_{p}\left(T_{s}-T_{s a l}\right)}{h_{f g}}$ | Ratio of sensible to latent energy absorbed during liquid-vapor phase change. |
| Lewis number (Le) | $\frac{\alpha}{D_{\mathrm{AB}}}$ | Ratio of the thermal and mass diffusivities. |
| Nusselt number ( $N u_{L}$ ) | $\frac{h L}{k_{f}}$ | Dimensionless temperature gradient at the surface. |
| Peclet number ( $P e_{L}$ ) | $\frac{V L}{\alpha}=R e_{L} P r$ | Dimensionless independent heat transfer parameter. |
| Prandtl number $(P r)$ | $\frac{c_{p} \mu}{k}=\frac{\nu}{\alpha}$ | Ratio of the momentum and thermal diffusivities |
| Reynolds number ( $\operatorname{Re}_{L}$ ) | $\frac{V L}{\nu}$ | Ratio of the inertia and viscous forces. |
| Schmidt number (Sc) | $\frac{\nu}{D_{A B}}$ | Ratio of the momentum and mass diffusivities. |
| Sherwood number $\left(S h_{L}\right)$ | $\frac{h_{m} L}{D_{A B}}$ | Dimensionless concentration gradient at the surface. |
| Stanton number (St) | $\frac{h}{\rho V c_{p}}=\frac{N u_{L}}{R e_{L} P r}$ | Modified Nusselt number. |
| Mass transfer Stanton number ( $S t_{m}$ ) | $\frac{h_{m}}{V}=\frac{S h_{L}}{R e_{L} S c}$ | Modified Sherwood number. |
| Weber number (We) | $\frac{\rho V^{2} L}{\sigma}$ | Ratio of inertia to surface tension forces. |

Table 7.9 Summary of convection heat transfer correlations for external flow ${ }^{a, b}$

| Correlation |  | Geometry | Conditions |
| :---: | :---: | :---: | :---: |
| $\delta=5 x R e_{x}^{-1 / 2}$ | (7.19) | Flat plate | Laminar, $T_{f}$ |
| $C_{f, x}=0.664 R_{x}^{-1 / 2}$ | (7.20) | Flat plate | Laminar, local, $T_{f}$ |
| $N u_{x}=0.332 \operatorname{Rex}_{x}^{1 / 2} \mathrm{Pr}^{1 / 3}$ | (7.23) | Flat plate | Laminar, local, $T_{f}, 0.6 \leq P r \leq 50$ |
| $\delta_{i}=\delta \mathrm{Pr}^{-1 / 3}$ | (7.24) | Flat plate | Laminar, $T_{f}$ |
| $\bar{C}_{f . x}=1.328 R e_{x}^{-1 / 2}$ | (7.30) | Flat plate | Laminar, average, $T_{j}$ |
| $\overline{N u}_{x}=0.664 R_{x}^{1 / 2} \mathrm{Pr}^{1 / 3}$ | (7.31) | Flat plate | Laminar, average, $T_{f}, 0.6 \leqslant P r r \leqslant 50$ |
| $N u_{x}=0.565 P e_{x}^{1 / 2}$ | (7.33) | Flat plate | Laminar, local, $T_{j}, \operatorname{Pr} \leq 0.05$ |
| $C_{f_{x}}=0.0592 R e_{x}^{-1 / s}$ | (7.35) | Flat plate | Turbulent, local, $T_{f}, R e_{x} \leqslant 10^{8}$ |
| $\delta=0.37 x R e_{x}^{-1 / 5}$ | (7.36) | Flat plate | Turbulent, local, $T_{f}, R e_{x} \leqslant 10^{8}$ |
| $N u_{x}=0.0296 \mathrm{Re}_{x}^{4 / 5} \mathrm{Pr}^{1 / 3}$ | (7.37) | Flat plate | $\begin{aligned} & \text { Turbulent, local, } T_{f}, R e_{x} \leqslant 10^{8} \text {, } \\ & 0.6 \leqslant \operatorname{Pr} \leqslant 60 \end{aligned}$ |
| $\bar{C}_{f L}=0.074 R e_{L}^{-1 / 5}-1742 R e_{L}^{-1}$ | (7.43) | Flat plate | Mixed, average, $T_{f}, R e_{x, c}=5 \times 10^{5}$, $R e_{L} \leqslant 10^{8}$ |
| $\widetilde{N u}_{L}=\left(0.037 \operatorname{Re}_{L}^{4 / 5}-871\right) P r^{1 / 3}$ | (7.41) | Flat plate | $\begin{aligned} & \text { Mixed, average, } T_{f}, R e_{x_{, ~}, c}=5 \times 10^{5}, \\ & R e_{L} \leq 10^{8}, 0.6<\operatorname{Pr}<60 \end{aligned}$ |
| $\begin{aligned} & \overline{\overline{N u} u_{D}}=C R e_{D}^{m} P r^{1 / 3} \\ & \text { (Table 7.2) } \end{aligned}$ | (7.55b) | Cylinder | $\begin{aligned} & \text { Average, } T_{f}, 0.4<\operatorname{Re}_{D}<4 \times 10^{5}, \\ & \operatorname{Pr} \geqq 0.7 \end{aligned}$ |
| $\begin{aligned} & \overline{N u}_{D}=C R e_{D}^{m} P r^{n}\left(P r / P r_{s}\right)^{1 / 4} \\ & \text { (Table 7.4) } \end{aligned}$ | (7.56) | Cylinder | $\begin{aligned} & \text { Average, } T_{\infty}, 1<R e_{D}<10^{6} \text {, } \\ & 0.7<\operatorname{Pr}<500 \end{aligned}$ |


| $\overline{\overline{N u}}_{D}=$ | $0.3+\left[0.62 R e_{D}^{1 / 2} \operatorname{Pr}^{1 / 3}\right.$ |  | Cylinder |
| ---: | :--- | ---: | :--- |


| $\begin{aligned} & \left.+0.06 \operatorname{Re}_{D}^{2 / 3}\right) \mathrm{Pr}^{0.4} \\ & \times\left(\mu / \mu_{s}\right)^{1 / 4} \end{aligned}$ | (7.59) | , | $0.71<\operatorname{Pr}<380$ |
| :---: | :---: | :---: | :---: |
| $\overline{N u}_{D}=2+0.6 R e_{D}^{1 / 2} \mathrm{Pr}^{1 / 3}$ | (7.60) | Falling drop | Average, $T_{\infty}$ |
| $\overline{\overline{N u}}_{D}=1.13 C_{1} \operatorname{Re}_{D, \text { max }}^{m} \operatorname{Pr}^{1 / 3}$ <br> (Tables 7.5, 7.6) | (7.63) | Tube bank ${ }^{\text {c }}$ | $\begin{aligned} & \text { Average, } \bar{T}_{f}, 2000<R e_{D, \max }<4 \times 10^{4}, \\ & \operatorname{Pr} \geq 0.7 \end{aligned}$ |
| $\begin{aligned} & \overline{N u}_{D}=C R e_{D, \text { max }}^{m} P^{0.36}\left(P r_{P r} / P r_{s}\right)^{1 / 4} \\ & \text { (Tables 7.7,7.8) } \end{aligned}$ | (7.67) | Tube bank ${ }^{\boldsymbol{c}}$ | $\begin{aligned} & \text { Average, } \bar{T}, 1000<R e_{D}<2 \times 10^{6} \text {, } \\ & 0.7<\operatorname{Pr}<500 \end{aligned}$ |
| Single round nozzle | (7.79) | Impinging jet | $\begin{aligned} & \text { Average, } T_{f}, 2000<R e<4 \times 10^{5} \text {, } \\ & 2<(H / D)<12,2.5<(r / D)<7.5 \end{aligned}$ |
| Single slot nozzle | (7.82) | Impinging jet | $\begin{aligned} & \text { Average, } T_{f}, 3000<R e<9 \times 10^{4} \text {, } \\ & 2<(H / W)<10,4<(x / W)<20 \end{aligned}$ |
| Array of round nozzles | (7.84) | Impinging jet | $\begin{aligned} & \text { Average, } T_{f}, 2000<R e<10^{5}, \\ & 2<(H / D)<12,0.004<A_{r}<0.04 \end{aligned}$ |
| Array of slot nozzles | (7.87) | Impinging jet | $\begin{aligned} & \text { Average, } T_{r}, 1500<R e<4 \times 10^{4} \\ & 2<(H / W)<80,0.008<A_{r}<2.5 A_{r, o} \end{aligned}$ |
| $\overline{\varepsilon \bar{j}_{H}}=\varepsilon \bar{j}_{m}=2.06 R e_{D}^{-0.575}$ | (7.91) | Packed bed of spheres ${ }^{c}$ | Average, $\bar{T}, 90 \leq R e_{D} \leq 4000, \operatorname{Pr} \approx 0.7$ |

${ }^{a}$ Correlations in this table pertain to isothermal surfaces; for special cases involving an unheated starting length or a uniform surface heat flux, see Section 7.2.4.
${ }^{6}$ When the heat and mass transfer analogy is applicable, the corresponding mass transfer correlations may be obtained by replacing Nu and Pr by $S h$ and $S c$, respectively.
For tube banks and packed beds, properties are evaluated at the average fluid temperature, $\bar{T}=\left(T_{i}+T_{o}\right) / 2$, or the average film temperature, $\bar{T}_{f}=\left(T_{s}+\bar{T}\right) / 2$.
Table A. 6 Thermophysical Properties of Saturated Water ${ }^{\boldsymbol{a}}$

| Temperature, $T$ <br> (K) | $\underset{\underset{P}{\text { Pressure, }} \text { (bars) }{ }^{\boldsymbol{b}}}{ }$ | Specific Volume ( $\mathrm{m}^{3} / \mathrm{kg}$ ) |  | Heat of Vaporization, $\boldsymbol{h}_{f g}$$(\mathbf{k J} / \mathrm{kg})$ | $\begin{gathered} \text { Specific } \\ \text { Heat } \\ (\mathbf{k J} / \mathbf{k g} \cdot \mathbf{K}) \end{gathered}$ |  | $\begin{aligned} & \text { Viscosity } \\ & \left(\mathbf{N} \cdot \mathbf{s} / \mathbf{m}^{2}\right) \end{aligned}$ |  | $\begin{aligned} & \text { Thermal } \\ & \text { Conductivity } \\ & (\mathbf{W} / \mathbf{m} \cdot K) \end{aligned}$ |  | $\underset{\substack{\text { PrandtI } \\ \text { Number }}}{ }$ |  |  | ExpansionCoeffi-cient$\boldsymbol{\beta}_{f} 10^{6}$$\left(\mathbf{K}^{-1}\right)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\boldsymbol{v}_{f} \cdot 10^{3}$ | $v_{g}$ |  | $c_{p, f}$ | $c_{p, g}$ | $\mu_{f} \cdot 10^{6}$ | $\mu_{g} \cdot 10^{6}$ | $k_{f} \cdot 10^{3}$ | $k_{g} \cdot 10^{3}$ | $\mathrm{Pr}_{\text {f }}$ | $\mathrm{Pr}_{\mathrm{g}}$ |  |  |  |
| 273.15 | 0.00611 | 1.000 | 206.3 | 2502 | 4.217 | 1.854 | 1750 | 8.02 | 569 | 18.2 | 12.99 | 0.815 | 75.5 | -68.05 | 273.15 |
| 275 | 0.00697 | 1.000 | 181.7 | 2497 | 4.211 | 1.855 | $1652^{-}$ | 8.09 | 574 | 18.3 | 12.22 | 0.817 | 75.3 | -32.74 | 275 |
| 280 | 0.00990 | 1.000 | 130.4 | 2485 | 4.198 | 1.858 | 1422 | 8.29 | 582 | 18.6 | 10.26 | 0.825 | 74.8 | 46.04 | 280 |
| 285 | 0.01387 | 1.000 | 99.4 | 2473 | 4.189 | 1.861 | 1225 | 8.49 | 590 | 18.9 | 8.81 | 0.833 | 74.3 | 114.1 | 285 |
| 290 | 0.01917 | 1.001 | 69.7 | 2461 | 4.184 | 1.864 | 1080 | 8.69 | 598 | 19.3 | 7.56 | 0.841 | 73.7 | 174.0 | 290 |
| 295 | 0.02617 | 1.002 | 51.94 | 2449 | 4.181 | 1.868 | 959 | 8.89 | 606 | 19.5 | 6.62 | 0.849 | 72.7 | 227.5 | 295 |
| 300 | 0.03531 | 1.003 | 39.13 | 2438 | 4.179 | 1.872 | 855 | 9.09 | 613 | 19.6 | 5.83 | 0.857 | 71.7 | 276.1 | 300 |
| 305 | 0.04712 | 1.005 | 29.74 | 2426 | 4.178 | 1.877 | 769 | 9.29 | 620 | 20.1 | 5.20 | 0.865 | 70.9 | 320.6 | 305 |
| 310 | 0.06221 | 1.007 | 22.93 | 2414 | 4.178 | 1.882 | 695 | 9.49 | 628 | 20.4 | 4.62 | 0.873 | 70.0 | 361.9 | 310 |
| 315 | 0.08132 | 1.009 | 17.82 | 2402 | 4.179 | 1.888 | 631 | 9.69 | 634 | 20.7 | 4.16 | 0.883 | 69.2 | 400.4 | 315 |
| 320 | 0.1053 | 1.011 | 13.98 | 2390 | 4.180 | 1.895 | 577 | 9.89 | 640 | 21.0 | 3.77 | 0.89 | 68.3 | 436.7 | 320 |
| 325 | 0.1351 | 1.013 | 11.06 | 2378 | 4.182 | 1.903 | 528 | 10.09 | 645 | 21.3 | 3.42 | 0.90 | 67.5 | 471.2 | 325 |
| 330 | 0.1719 | 1.016 | 8.82 | 2366 | 4.184 | 1.911 | 489 | 10.29 | 650 | 21.7 | 3.15 | 0.908 | 66.6 | 504.0 | 330 |
| 335 | 0.2167 | 1.018 | 7.09 | 2354 | 4.186 | 1.920 | 453 | 10.49 | 656 | 22.0 | 2.88 | 0.916 | 65.8 | 535.5 | 335 |
| 340 | 0.2713 | 1.021 | 5.74 | 2342 | 4.188 | 1.930 | 420 | 10.69 | 660 | 22.3 | 2.66 | 0.925 | 64.9 | 566.0 | 340 |
| 345 | 0.3372 | 1.024 | 4.683 | 2329 | 4.191 | 1.941 | 389 | 10.89 | 668 | 22.6 | 2.45 | 0.933 | 64.1 | 595.4 | 345 |
| 350 | 0.4163 | 1.027 | 3.846 | 2317 | 4.195 | 1.954 | 365 | 11.09 | 668 | 23.0 | 2.29 | 0.942 | 63.2 | 624.2 | 350 |
| 355 | 0.5100 | 1.030 | 3.180 | 2304 | 4.199 | 1.968 | 343 | 11.29 | 671 | 23.3 | 2.14 | 0.951 | 62.3 | 652.3 | 355 |
| 360 | 0.6209 | 1.034 | 2.645 | 2291 | 4.203 | 1.983 | 324 | 11.49 | 674 | 23.7 | 2.02 | 0.960 | 61.4 | 697.9 | 360 |
| 365 | 0.7514 | 1.038 | 2.212 | 2278 | 4.209 | 1.999 | 306 | 11.69 | 677 | 24.1 | 1.91 | 0.969 | 60.5 | 707.1 | 365 |
| 370 | 0.9040 | 1.041 | 1.861 | 2265 | 4.214 | 2.017 | 289 | 11.89 | 679 | 24.5 | 1.80 | 0.978 | 59.5 | 728.7 | 370 |
| 373.15 | 1.0133 | 1.044 | 1.679 | 2257 | 4.217 | 2.029 | 279 | 12.02 | 680 | 24.8 | 1.76 | 0.984 | 58.9 | 750.1 | 373.15 |
| 375 | 1.0815 | 1.045 | 1.574 | 2252 | 4.220 | 2.036 | 274 | 12.09 | 681 | 24.9 | 1.70 | 0.987 | 58.6 | 761 | 375 |
| 380 | 1.2869 | 1.049 | 1.337 | 2239 | 4.226 | 2.057 | 260 | 12.29 | 683 | 25.4 | 1.61 | 0.999 | 57.6 | 788 | 380 |
| 85 | 1.5233 | 1.053 | 1.142 | 2225 | 4.232 | 2.080 | 248 | 12.49 | 685 | 25.8 | 1.53 | 1.00 | 56.6 | 814 | 385 |

Table A. 4 Thermophysical Properties
of Gases at Atmospheric Pressure ${ }^{a}$

| $\boldsymbol{T}$ | $\rho$ <br> $\left(\mathrm{kg} / \mathrm{m}^{3}\right)$ | $c_{p}$ <br> $(\mathrm{kJJ} / \mathrm{kg} \cdot \mathrm{K})$ | $\mu \cdot 10^{7}$ <br> $\left(\mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2}\right)$ | $\nu \cdot 10^{6}$ <br> $\left(\mathrm{~m}^{2} / \mathrm{s}\right)$ | $k \cdot 10^{3}$ <br> $(\mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$ | $\alpha \cdot 10^{6}$ <br> $\left(\mathrm{~m}^{2} / \mathrm{s}\right)$ | $\operatorname{Pr}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |


| Air |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 100 | 3.5562 | 1.032 | 71.1 | 2.00 | 9.34 | 2.54 | 0.786 |
| 150 | 2.3364 | 1.012 | 103.4 | 4.426 | 13.8 | 5.84 | 0.758 |
| 200 | 1.7458 | 1.007 | 132.5 | 7.590 | 18.1 | 10.3 | 0.737 |
| 250 | 1.3947 | 1.006 | 159.6 | 11.44 | 22.3 | 15.9 | 0.720 |
| 300 | 1.1614 | 1.007 | 184.6 | 15.89 | 26.3 | 22.5 | 0.707 |
| 350 | 0.9950 | 1.009 | 208.2 | 20.92 | 30.0 | 29.9 | 0.700 |
| 400 | 0.8711 | 1.014 | 230.1 | 26.41 | 33.8 | 38.3 | 0.690 |
| 450 | 0.7740 | 1.021 | 250.7 | 32.39 | 37.3 | 47.2 | 0.686 |
| 500 | 0.6964 | 1.030 | 270.1 | 38.79 | 40.7 | 56.7 | 0.684 |
| 550 | 0.6329 | 1.040 | 288.4 | 45.57 | 43.9 | 66.7 | 0.683 |
| 600 | 0.5804 | 1.051 | 305.8 | 52.69 | 46.9 | 76.9 | 0.685 |
| 650 | 0.5356 | 1.063 | 322.5 | 60.21 | 49.7 | 87.3 | 0.690 |
| 700 | 0.4975 | 1.075 | 338.8 | 68.10 | 52.4 | 98.0 | 0.695 |
| 750 | 0.4643 | 1.087 | 354.6 | 76.37 | 54.9 | 109 | 0.702 |
| 800 | 0.4354 | 1.099 | 369.8 | 84.93 | 57.3 | 120 | 0.709 |
| 850 | 0.4097 | 1.110 | 384.3 | 93.80 | 59.6 | 131 | 0.716 |
| 900 | 0.3868 | 1.121 | 398.1 | 102.9 | 62.0 | 143 | 0.720 |
| 950 | 0.3666 | 1.131 | 411.3 | 112.2 | 64.3 | 155 | 0.723 |
| 1000 | 0.3482 | 1.141 | 424.4 | 121.9 | 66.7 | 168 | 0.726 |
| 1100 | 0.3166 | 1.159 | 449.0 | 141.8 | 71.5 | 195 | 0.728 |
| 1200 | 0.2902 | 1.175 | 473.0 | 162.9 | 76.3 | 224 | 0.728 |
| 1300 | 0.2679 | 1.189 | 496.0 | 185.1 | 82 | 238 | 0.719 |
| 1400 | 0.2488 | 1.207 | 530 | 213 | 91 | 303 | 0.703 |
| 1500 | 0.2322 | 1.230 | 557 | 240 | 100 | 350 | 0.685 |
| 1600 | 0.2177 | 1.248 | 584 | 268 | 106 | 390 | 0.688 |
| 1700 | 0.2049 | 1.267 | 611 | 298 | 113 | 435 | 0.685 |
| 1800 | 0.1935 | 1.286 | 637 | 329 | 120 | 482 | 0.683 |
| 1900 | 0.1833 | 1.307 | 663 | 362 | 128 | 534 | 0.677 |
| 2000 | 0.1741 | 1.337 | 689 | 396 | 137 | 589 | 0.672 |
| 2100 | 0.1658 | 1.372 | 715 | 431 | 147 | 646 | 0.667 |
| 2200 | 0.1582 | 1.417 | 740 | 468 | 160 | 714 | 0.655 |
| 2300 | 0.1513 | 1.478 | 766 | 506 | 175 | 783 | 0.647 |
| 2400 | 0.1448 | 1.558 | 792 | 547 | 196 | 869 | 0.630 |
| 2500 | 0.1389 | 1.665 | 818 | 589 | 222 | 960 | 0.613 |
| 3000 | 0.1135 | 2.726 | 955 | 841 | 486 | 1570 | 0.536 |
| Ammonia ( $\mathbf{N H}_{3}$ ) |  |  |  |  |  |  |  |
| 300 | 0.6894 | 2.158 | 101.5 | 14.7 | 24.7 | 16.6 | 0.887 |
| 320 | 0.6448 | 2.170 | 109 | 16.9 | 27.2 | 19.4 | 0.870 |
| 340 | 0.6059 | 2.192 | 116.5 | 19.2 | 29.3 | 22.1 | 0.872 |
| 360 | 0.5716 | 2.221 | 124 | 21.7 | 31.6 | 24.9 | 0.872 |
| 380 | 0.5410 | 2.254 | 131 | 24.2 | 34.0 | 27.9 | 0.869 |

Table 3.3 One-dimensional, steady-state solutions to the heat equation with no generation

|  | Plane Wall | Cylindrical Wall ${ }^{a}$ | Spherical Wall $^{a}$ |
| :--- | :---: | :---: | :---: |
| Heat equation | $\frac{d^{2} T}{d x^{2}}=0$ | $\frac{1}{r} \frac{d}{d r}\left(r \frac{d T}{d r}\right)=0$ | $\frac{1}{r^{2}} \frac{d}{d r}\left(r^{2} \frac{d T}{d r}\right)=0$ |
| Temperature <br> distribution | $T_{s, 1}-\Delta T \frac{x}{L}$ | $T_{s, 2}+\Delta T \frac{\ln \left(r / r_{2}\right)}{\ln \left(r_{1} / r_{2}\right)}$ | $T_{s, 1}-\Delta T\left[\frac{1-\left(r_{1} / r\right)}{1-\left(r_{1} / r_{2}\right)}\right]$ |
| Heat flux ( $\left.q^{\prime \prime}\right)$ | $k \frac{\Delta T}{L}$ | $\frac{k \Delta T}{r \ln \left(r_{2} / r_{1}\right)}$ | $\frac{k \Delta T}{r^{2}\left[\left(1 / r_{1}\right)-\left(1 / r_{2}\right)\right]}$ |
| Heat rate $(q)$ | $k A \frac{\Delta T}{L}$ | $\frac{2 \pi L k \Delta T}{\ln \left(r_{2} / r_{1}\right)}$ | $\frac{4 \pi k \Delta T}{\left(1 / r_{1}\right)-\left(1 / r_{2}\right)}$ |
| Thermal |  |  |  |
| resistance $\left(R_{t, c o n d}\right)$ |  |  |  |

"The critical radius of insulation is $r_{\text {tr }}=k / h$ for the cylinder and $r_{\text {cr }}=2 k / h$ for the sphere.

## Radiation Data:

Stefan Boltzmann constant $=5.67 \times 10^{-8} \mathrm{Wm}^{-2} \mathrm{~K}^{-1}$

Table 13.3 Special Diffuse, Gray, Two-Surface Enclosures

## Large (Infinite) Parallel Planes



$$
\begin{align*}
A_{1} & =A_{2}=A \quad q_{12}=\frac{A \sigma\left(T_{1}^{4}-T_{2}^{4}\right)}{F_{12}} \tag{13.24}
\end{align*}=1 \quad \frac{1}{\varepsilon_{1}}+\frac{1}{\varepsilon_{2}}-1
$$

Long (Infinite) Concentric
Cylinders


$$
\begin{align*}
\frac{A_{1}}{A_{2}} & =\frac{r_{1}}{r_{2}}  \tag{13.25}\\
F_{12} & =1
\end{align*} \quad q_{12}=\frac{\sigma A_{1}\left(T_{1}^{4}-T_{2}^{4}\right)}{\frac{1}{\varepsilon_{1}}+\frac{1-\varepsilon_{2}}{\varepsilon_{2}}\left(\frac{r_{1}}{r_{2}}\right)}
$$

## Concentric Spheres



$$
\begin{align*}
\frac{A_{1}}{A_{2}} & =\frac{r_{1}^{2}}{r_{2}^{2}}  \tag{13.26}\\
F_{12} & =1
\end{align*} \quad q_{12}=\frac{\sigma A_{1}\left(T_{1}^{4}-T_{2}^{4}\right)}{\frac{1}{\varepsilon_{1}}+\frac{1-\varepsilon_{2}}{\varepsilon_{2}}\left(\frac{r_{1}}{r_{2}}\right)^{2}}
$$

Small Convex Object in a Large Cavity
$A_{A_{2}, T_{2}, \varepsilon_{2},}^{A_{1}, T_{1}, \varepsilon_{1}}$

$$
\begin{equation*}
\frac{A_{1}}{A_{2}} \approx 0 \quad q_{12}=\sigma A_{1} \varepsilon_{1}\left(T_{1}^{4}-T_{2}^{4}\right) \tag{13.27}
\end{equation*}
$$

## Diffusion Data:

Table A. 8 Binary Diffusion Coefficients at One Atmosphere ${ }^{a, b}$

| Substance A | Substance B | $\begin{gathered} \boldsymbol{T} \\ (\mathbf{K}) \end{gathered}$ | $\underset{\left(\mathbf{m}^{2} / \mathbf{s}\right)}{D_{\mathrm{AB}}}$ |
| :---: | :---: | :---: | :---: |
| Gases |  |  |  |
| $\mathrm{NH}_{3}$ | Air | 298 | $0.28 \times 10^{-4}$ |
| $\mathrm{H}_{2} \mathrm{O}$ | Air | 298 | $0.26 \times 10^{-4}$ |
| $\mathrm{CO}_{2}$ | Air | 298 | $0.16 \times 10^{-4}$ |
| $\mathrm{H}_{2}$ | Air | 298 | $0.41 \times 10^{-4}$ |
| $\mathrm{O}_{2}$ | Air | 298 | $0.21 \times 10^{-4}$ |
| Acetone | Air | 273 | $0.11 \times 10^{-4}$ |
| Benzene | Air | 298 | $0.88 \times 10^{-5}$ |
| Naphthalene | Air | 300 | $0.62 \times 10^{-5}$ |
| Ar | $\mathrm{N}_{2}$ | 293 | $0.19 \times 10^{-4}$ |
| $\mathrm{H}_{2}$ | $\mathrm{O}_{2}$ | 273 | $0.70 \times 10^{-4}$ |
| $\mathrm{H}_{2}$ | $\mathrm{N}_{2}$ | 273 | $0.68 \times 10^{-4}$ |
| $\mathrm{H}_{2}$ | $\mathrm{CO}_{2}$ | 273 | $0.55 \times 10^{-4}$ |
| $\mathrm{CO}_{2}$ | $\mathrm{N}_{2}$ | 293 | $0.16 \times 10^{-4}$ |
| $\mathrm{CO}_{2}$ | $\mathrm{O}_{2}$ | 273 | $0.14 \times 10^{-4}$ |
| $\mathrm{O}_{2}$ | $\mathrm{N}_{2}$ | 273 | $0.18 \times 10^{-4}$ |
| Dilute Solutions |  |  |  |
| Caffeine | $\mathrm{H}_{2} \mathrm{O}$ | 298 | $0.63 \times 10^{-9}$ |
| Ethanol | $\mathrm{H}_{2} \mathrm{O}$ | 298 | $0.12 \times 10^{-8}$ |
| Glucose | $\mathrm{H}_{2} \mathrm{O}$ | 298 | $0.69 \times 10^{-9}$ |
| Glycerol | $\mathrm{H}_{2} \mathrm{O}$ | 298 | $0.94 \times 10^{-9}$ |
| Acetone | $\mathrm{H}_{2} \mathrm{O}$ | 298 | $0.13 \times 10^{-8}$ |
| $\mathrm{CO}_{2}$ | $\mathrm{H}_{2} \mathrm{O}$ | 298 | $0.20 \times 10^{-8}$ |
| $\mathrm{O}_{2}$ | $\mathrm{H}_{2} \mathrm{O}$ | 298 | $0.24 \times 10^{-8}$ |
| $\mathrm{H}_{2}$ | $\mathrm{H}_{2} \mathrm{O}$ | 298 | $0.63 \times 10^{-8}$ |
| $\mathrm{N}_{2}$ | $\mathrm{H}_{2} \mathrm{O}$ | 298 | $0.26 \times 10^{-8}$ |
| Solids |  |  |  |
| $\mathrm{O}_{2}$ | Rubber | 298 | $0.21 \times 10^{-9}$ |
| $\mathrm{N}_{2}$ | Rubber | 298 | $0.15 \times 10^{-9}$ |
| $\mathrm{CO}_{2}$ | Rubber | 298 | $0.11 \times 10^{-9}$ |
| He | $\mathrm{SiO}_{2}$ | 293 | $0.4 \times 10^{-13}$ |
| $\mathrm{H}_{2}$ | Fe | 293 | $0.26 \times 10^{-12}$ |
| Cd | Cu | 293 | $0.27 \times 10^{-18}$ |
| Al | Cu | 293 | $0.13 \times 10^{-33}$ |

${ }^{a}$ Adapted with permission from References 20, 21, and 22.
${ }^{b}$ Assuming ideal gas behavior, the pressure and temperature dependence of the diffusion coefficient for a binary mixture of gases may be estimated from the relation

$$
D_{\mathrm{AB}} \propto p^{-1} T^{3 / 2}
$$

Table A. 9 Henry's Constant for Selected Gases in Water at Moderate Pressure ${ }^{a}$

| $\boldsymbol{H}=\boldsymbol{p}_{A, i} / x_{A, i}$ (bars) |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $T$ <br> (K) | $\mathbf{N H}_{3}$ | $\mathrm{Cl}_{2}$ | $\mathrm{H}_{2} \mathrm{~S}$ | $\mathrm{SO}_{2}$ | $\mathrm{CO}_{2}$ | $\mathrm{CH}_{4}$ | $\mathrm{O}_{2}$ | $\mathrm{H}_{2}$ |
| 273 | 21 | 265 | 260 | 165 | 710 | 22,880 | 25,500 | 58,000 |
| 280 | 23 | 365 | 335 | 210 | 960 | 27,800 | 30,500 | 61,500 |
| 290 | 26 | 480 | 450 | 315 | 1300 | 35,200 | 37,600 | 66,500 |
| 300 | 30 | 615 | 570 | 440 | 1730 | 42,800 | 45,700 | 71,600 |
| 310 | - | 755 | 700 | 600 | 2175 | 50,000 | 52,500 | 76,000 |
| 320 | - | 860 | 835 | 800 | 2650 | 56,300 | 56,800 | 78,600 |
| 323 | - | 890 | 870 | 850 | 2870 | 58,000 | 58,000 | 79,000 |

${ }^{a}$ Adapted with permission from Reference 23.
Table A. 10 The Solubility of
Selected Gases and Solids ${ }^{a}$

|  | Solid | $T$ <br> $(\mathbf{K})$ | $S=C_{A, i} / \boldsymbol{p}_{A, i}$ <br> $\left(\mathbf{k m o l} / \mathbf{m}^{3} \cdot \mathbf{b a r}\right)$ |
| :--- | :--- | :---: | :---: |
| Gas | Rubber | 298 | $3.12 \times 10^{-3}$ |
| $\mathrm{O}_{2}$ | Rubber | 298 | $1.56 \times 10^{-3}$ |
| $\mathrm{~N}_{2}$ | $\mathrm{Rubber}^{2}$ | 298 | $40.15 \times 10^{-3}$ |
| $\mathrm{CO}_{2}$ | $\mathrm{SiO}_{2}$ | 293 | $0.45 \times 10^{-3}$ |
| He | Ni | 358 | $9.01 \times 10^{-3}$ |
| $\mathrm{H}_{2}$ |  |  |  |

"Adapted with permission from Reference 22.

Table 14.1 Summary of Species Diffusion Solutions for Stationary

## Media with Specified Surface Concentrations ${ }^{a}$

| Geometry | Species Concentration <br> Distribution, $x_{\mathrm{A}}(x)$ or $x_{\mathrm{A}}(r)$ | Species Diffusion <br> Resistance, $R_{m, ~ d i f ~}^{\prime}$ |
| :--- | :---: | :---: |



$$
x_{A}(x)=\left(x_{A, s 2}-x_{A, s 1}\right) \frac{x}{L}+x_{A, s 1} \quad R_{m, \mathrm{dif}}={\frac{L}{D_{\mathrm{AB}} A}}^{b}
$$



$$
x_{A}(r)=\frac{x_{A, s 1}-x_{A, s 2}}{\ln \left(r_{1} / r_{2}\right)} \ln \left(\frac{r}{r_{2}}\right)+x_{A, s 2} \quad R_{m, \text { dif }}=\frac{\ln \left(r_{2} / r_{1}\right)^{c}}{2 \pi L D_{\mathrm{AB}}}
$$



$$
x_{A}(r)=\frac{x_{A, s 1}-x_{A, s 2}}{1 / r_{1}-1 / r_{2}}\left(\frac{1}{r}-\frac{1}{r_{2}}\right)+x_{A, s 2}
$$

$$
R_{m, \text { dif }}=\frac{1}{4 \pi D_{\mathrm{AB}}}\left(\frac{1}{r_{1}}-\frac{1}{r_{2}}\right)^{c}
$$

${ }^{a}$ Assuming $C$ and $D_{\mathrm{AB}}$ are constant.
${ }^{b} N_{\mathrm{A}, x}=\left(C_{\mathrm{A}, s 1}-C_{\mathrm{A}, s 2}\right) / R_{m, \text { dif }}$.
${ }^{c} N_{\mathrm{A}, r}=\left(C_{\mathrm{A}, s 1}-C_{\mathrm{A}, s 2}\right) / R_{m, \text { dif }}$.

