

UNIVERSITY
JOHANNESBURG

## Department of Accounting

# Financial Recording, Analysis and Management B 

## FRAM0B1

## LAST ASSESSMENT OPPORTUNITY

19 November 2019

Time: 3 hours
Marks: 100
Assessor: $\quad$ Mr M de Wet

Moderator: Prof G Els

## INSTRUCTIONS

- This paper consists of $\mathbf{1 5}$ pages (including the formulae sheet and interest factors tables) AND a separate, pre-printed answer book.
- Clearly PRINT your initial(s), surname and student number in the spaces provided on the answer book.
- Answer ALL questions in the spaces provided in black or blue pen in the answer book. Please remember that marks are ONLY allocated to answers written in these spaces!
- Please note that questions may have more than one correct answer!
- You may complete all workings and/or calculations on the question paper.
- Silent, non-programmable calculators may be used, unless otherwise instructed.
- Round all calculations to TWO decimal places unless instructed otherwise.
- Answers with Tippex and in pencil will not be marked and the paper will not be eligible for a remark.


## Section one: multiple choice questions (33)

## QUESTION 1 (1)

Which of the following statements about return is least accurate?
A Return is compensation for taking on a certain degree of risk.
B Return is made up of the dividends earned by owning a share.
C Return consists of dividends paid to share holders as well as capital gains on a share.
D The return can be negative.

## QUESTION 2 (1)

Which of the following is true about a rational investor:
A A rational investor will maximize return at all cost
B A rational investor will aim to minimize risk for a given level of return
C A rational investor will aim to maximize risk for a given level of return
D A rational investor will aim to minimize return for a given level of risk

## QUESTION 3 (1)

The price paid for the 'rental' of borrowed funds is commonly referred to as the ...

A interest rate.
B inflation rate.
C rental rate.
D transaction cost.

## QUESTION 4 (1)

Using financial statements to decide whether to invest in a company is known as...
A financial statement analysis.
B financial responsibility.
C financial accountability.
D None of the above.

## QUESTION 5 (1)

If a price index is 89 , which ONE of the following statements is/are correct about average prices?
A Prices have risen by $89 \%$ relative to the base year.
B Prices are now 0.89 times the base year.
C Prices have declined by $11 \%$ relative to the base year.
D Prices have increased by $11 \%$ relative to the base year.

## Consider the following regression line and answer questions 6-8:

$$
Y=23+1.2 X+\hat{\mathrm{u}}
$$

## QUESTION 6 (1)

In the above regression line, $Y$ represents ...
A the explanatory variable.
B the intercept.
C the residual term.
D the dependent variable.

## QUESTION 7 (1)

In the above regression line, û represents ...
A the explanatory variable.
B the intercept.
C the residual term.
D the dependent variable.

## QUESTION 8 (1)

The slope of the $X$ variable is ...
A $\quad$ Y
B 23
C û
D $\quad 1.2$

## QUESTION 9 (1)

Markets in which funds are transferred from those who have excess funds available to those who have a shortage of available funds are called ...

A commodity markets.
B funds markets.
C derivative exchange markets.
D financial markets.

## QUESTION 10 (1)

Which ONE of the following functions does every financial market perform?
A It determines the level of interest rates.
B It allows ordinary shares to be traded.
C It allows loans to be made.
D It channels funds from lenders-savers to borrowers-spenders.

## QUESTION 11 (1)

Which ONE of the following is not a disadvantage of calculating an arithmetic mean?
A It may be influenced by extreme values
B It may give undue weight to extreme values
C It is unsuitable for use in mathematical tables
D The calculated value may not correspond to any individual value in the distribution

## QUESTION 12 (1)

One of the most common measures of an asset's risk is ...
A standard deviation.
B standard error.
C rate of return.
D normal distribution of the asset.

## QUESTION 13 (1)

Which ONE of the following statements of the coefficient of variation is the most accurate?
A It measures the risk of an asset relative to the total return of an asset
B It measures the risk of an asset per unit of return
C It is also known as the standard deviation of an asset's return
D None of the above are correct

## QUESTION 14 (1)

Consider a company with a relatively high $\mathrm{P} / \mathrm{E}$ ratio, which ONE of the following statements is most accurate?

A The company is a low earnings growth company
B The company is a high earnings growth company
C The company is seen by investors as a high risk company
D The company is mispriced, and the price must fall

## QUESTION 15 (1)

Which indexing method is most appropriate to use when indexing the price of a commodity of which the basic nature of the commodity is changing over time?

A Fixed-base method
B Splicing method
C Chain-base method
D Paasche indexing method

## QUESTION 16 (1)

Firms that require funds from external sources can obtain such funds ...
(i) from the capital market.
(ii) from retained earnings.
(iii) from suppliers' credit.
(iv) from the money market.

Which of the above statements are correct?
A (i) and (ii)
B (i) and (iii)
C (i), (iii) and (iv)
D (i), (ii), (iii) and (iv)

## QUESTION 17 (1)

Which of the following is not a classification group when considering classification of cost according to nature: materials, labour or expense cost:

A materials
B direct cost
C labour
D expenses

## QUESTION 18 (1)

Direct cost can be described as ...
A costs that can be clearly identified with the cost object we are trying to cost.
B costs incurred in the form of wages and salaries, together with related employment costs.
C The cost of obtaining the materials and receiving them within the organisation.
D costs that cannot be directly attributed to a particular cost unit.

## QUESTION 19 (1)

Which ONE of the following time value of money statements is least correct?

A Interest earned on money partly compensate for the natural loss in the value of money
B The future value of money is typically smaller than the present value of money
C The future value of money is typically larger that the present value of money
D Interest rates are typically used as discount rates

## QUESTION 20 (1)

The money market is the market in which ... are traded.

A new issues of securities
B previously issued securities
C short-term debt instruments
D long-term debt instruments

## QUESTION 21 (1)

The secondary market is the market in which ... are traded.

A new issues of securities
B previously issued securities
C short-term debt instruments
D long-term debt instruments

Refer to the following table, showing exchange rate quotations for various currency pairs, to answer question 22 to 24.

| ZAR/JPY | EUR/ZAR | NZD/ZAR | CAD/ZAR |
| :---: | :---: | :---: | :---: |
| 0.34 | 16.74 | 9.23 | 10.53 |

## QUESTION 22 (2)

How many Rand (ZAR) do you require to purchase one Euro (EUR)?
A 9.23
B $\quad 16.74$
C 0.059
D $\quad 10.53$

## QUESTION 23 (2)

How many New Zealand dollars (NZD) do you require to purchase one Rand?
A $\quad 9.23$
B $\quad 16.74$
C 0.108
D $\quad 10.53$

## QUESTION 24 (2)

If I purchase goods from Canada priced at 1298 Canadian dollar (CAD), how much Rand would I require to purchase these goods:

A $\quad 1298$
B $\quad 10.53$
C $\quad 123.267$
D $\quad 13667.94$

## QUESTION 25 (2)

A company's total monthly costs ( RC ) were plotted against production $(\mathrm{P})$ for the last 50 months and a regression line valuated to be $C=1089+27 P+$ Error. Which ONE, or more, of the following statements about the breakdown of weekly costs is/are true?

A Fixed costs are R1 089 and variable costs per unit are R27.
B Fixed costs are R27 and variable costs per unit are R1089.
C Fixed costs are R40 and variable costs per unit are R27.
D One cannot determine fixed and variable costs based on the information given.

## QUESTION 26 (2)

Assume that the expected return on a company with the name RR capital is $17 \%$ and the typical variance of this stock is $9 \%$, what is this RR capital's coefficient of variation:

A $17 \%$
B $9 \%$
C $\quad 1.889$
D 0.529

## QUESTION 27 (2)

You are considering Combat Ltd as a possible investment choice and determined the following possible returns as well as respective probability that each return realizes.

| Possible return | Probability |
| :---: | :---: |
| $3 \%$ | $25 \%$ |
| $17 \%$ | $49 \%$ |
| $14 \%$ | $26 \%$ |

What is the expected return for Combat Ltd?
A $6.667 \%$
B More information is required to answer this question
C $\quad 12.81 \%$
D $-12.81 \%$

## Section two: true and false (15)

## QUESTION 28

State whether the following statements are true or false:

|  | True | False |
| :---: | :---: | :---: |
| A. The closer the correlation coefficient is to -1 , the weaker the relationship between two variables are. |  |  |
| B. Compounded interest is only payed on the initial principal amount. |  |  |
| C. If the interest due at the end of an interest period is added to the principal, so that the interest computed for the next interest period is based on this new interest amount (old principal plus interest), then the interest is said to have been compounded. |  |  |
| D. The beta coefficient of a linear regression can be calculated by using the following equation: $\frac{\Delta Y}{\Delta X}$ |  |  |
| E. If you are a depositor and the bank offers you an option of $8 \%$ simple interest and $8 \%$ compounded interest on your deposit, you should choose the simple interest rate option. |  |  |
| F. If you and a friend deposit the same amount of money at the same interest rate today and you earn semi-annually compounded interest and your friend earns monthly compounded interest, you will have more money in the bank, relative to your friend, at the end of two years assuming not you or your friend makes any additional deposits. |  |  |
| G. Fads or rumours may be reflected in the price of a share. |  |  |
| H. Quoted interest rate is known as the nominal rate. |  |  |
| I. Expense costs include the cost of obtaining the materials and receiving them within the organisation. |  |  |
| J. Cost accounting mainly relates to the determination of the total cost of a product, from the purchase of raw materials to delivery to the consumer. |  |  |


| K. The return on an investment represents the compensation for taking on a <br> certain degree of risk. Return measures the increase in wealth of the holder <br> of the particular instrument. |  |  |
| :---: | :---: | :--- |
| L. Two assets with different expected returns and different standard deviations <br> can be compared to one another by calculating and comparing their <br> coefficient of variation. |  |  |
| M. Depreciation is the loss of value of a fixed asset such as equipment, <br> machinery, motor vehicles, etc., through age. |  |  |
| N. The line of best fit method is a method that can be used to establish the trend <br> in a time series |  |  |
| O. Standard deviation (or $\sigma$ ) measures the expected return of an asset. |  |  |

## Section three: time value of money calculations (14)

QUESTION 29 (2)
Assume that Mrs. Kumalo deposits R2 500 into an account today, what is her account balance at the end of 10 years if she earns $4 \%$ interest p.a., compounded quarterly?

## QUESTION 30 (8)

Complete the following table by solving the missing values $\mathbf{A}-\mathbf{D}$ :

| Present value | Interest rate | Number of years | Compounding <br> method | Future value |
| :---: | :---: | :---: | :---: | :---: |
| R4 821 | $8 \%$ | 12 | Monthly | A |
| R9 182 | B | 4 | Quarterly | R11928 |
| R3 372 | $12 \%$ | C | Annually | R6884 |
| D | $21 \%$ | 3 | Monthly | R3029 |

## QUESTION 31 (2)

How much would I have to deposit in an account today, that pays $12 \%$ interest p.a. compounded quarterly, so that I may have a balance of R20 000 in the account at the end of 10 years?

## QUESTION 32 (2)

How long does it take for your money to grow to ten times its original value if the interest rate is $5 \%$ compounded annually?

## Section four: risk and return calculations and cumulative frequencies (20)

QUESTION 33 (14)
Mr. Zulu is an asset manager at one of South Africa's largest asset management firms. Mr. Zulu receives R100 000 from a client whom wants to invest the funds in an asset that provides an optimal risk/return profile. There are two possible investment options, asset A or B. The following two tables depicts the possible returns and the probability associated with each return for each of the two assets. Help Mr. Zulu determine the optimal asset to invest in by calculating the expected return for each asset, the risk (variance) of each asset, and the coefficient of variation of each asset.

Return profile for asset A:

| Possible return ( $\boldsymbol{R}_{\boldsymbol{i}}$ ) | Probability of return ( $\boldsymbol{P}_{\boldsymbol{i}}$ ) |
| :--- | :---: |
| $8 \%$ | $55 \%$ |
| $12 \%$ | $21 \%$ |
| $-10 \%$ | $16 \%$ |
| $18 \%$ | $8 \%$ |
| Expected return: (A) |  |
| Risk: (B) |  |
| Coefficient of variation (C) |  |

## Return profile for asset B:

| Possible return ( $\boldsymbol{R}_{\boldsymbol{i}}$ ) | Probability of return ( $\boldsymbol{P}_{\boldsymbol{i}}$ ) |
| :--- | :---: |
| $1 \%$ | $21 \%$ |
| $19 \%$ | $40 \%$ |
| $41 \%$ | $8 \%$ |
| $-21 \%$ | $11 \%$ |
| Expected return: (D) |  |
| Risk: (E) |  |
| Coefficient of variation (F) |  |

Based on your results, advise Mr. Zulu on which asset will be optimal to invest in and state why (G).

## QUESTION 34 (6)

Complete the cumulative frequency column in the table for the data provided.

| Examination score <br> $(\boldsymbol{x})$ | Frequency $(\boldsymbol{f})$ | Cumulative <br> frequency $(\boldsymbol{c f})$ |
| :---: | :---: | :---: |
| $30 \leq x<40$ | 8 | 8 |
| $40 \leq x<50$ | 20 | A |
| $50 \leq x<60$ | 16 | B |
| $60 \leq x<70$ | 9 | C |
| $70 \leq x<80$ | 21 | D |
| $80 \leq x<90$ | 11 | E |
| $90 \leq x<100$ | 9 | F |

## Section five: Linear regression analysis (9)

## QUESTION 35 (9)

You are given the following regression line:

$$
\text { South African top } 40 \text { index }=489-1.5 \text { US Dollar/South African Rand }
$$

A. Which variable in the regression is the dependent variable?
B. What is the intercept value of this regression line?
C. What is the slope of this regression line?
D. If the US Dollar/South African Rand goes up with one unit, what will happen with the South African Top 40 Index?
E. Report on the relationship between the South African top 40 index and the US Dollar/South African Rand.
F. If we expect the future South African Rand to trade at 14.56 against the US Dollar, what should the value of the South African top 40 index be given the provided regression line?

## Section six: horizontal statement analysis (9)

## QUESTION 36 (9)

Consider the following extract from company ABC's Statement of Comprehensive Income:

|  | $\mathbf{2 0 1 9}$ (R’000) | $\mathbf{2 0 1 8}$ (R’000) |
| :--- | :---: | :---: |
| Sales | 18273 | 17367 |
| Cost of sales | 8817 | 8099 |
| Gross profit | 9456 | 9268 |

Convert the statement so that a horizontal analysis can be conducted.

|  | 2019 (R'000) | 2018 (R'000) |
| :--- | :---: | :---: |
| Sales | D) | A) |
| Cost of sales | E) | B) |
| Gross profit | F) | C) |

---00o---

## Formula sheet

$$
\begin{aligned}
& R=D_{t}+\frac{\left(P_{t}-P_{t-1}\right)}{P_{t-1}} \times \frac{100}{1} \\
& R_{e}=\sum\left(R_{i}\right)\left(P_{i}\right) \\
& \sigma=\sqrt{\sum^{n}\left(R_{i}-R_{e}\right)^{2} \times P_{i}} \\
& C V=\frac{\sigma}{R_{e}} \\
& r=\frac{n \sum x y-\sum x \sum y}{\sqrt{\left(n \sum x^{2}-\left(\sum x\right)^{2}\right)\left(n \sum y^{2}-\left(\sum y\right)^{2}\right)}} \\
& b=\frac{n \sum x y-\sum x \sum y}{n \sum x^{2}-\left(\sum x\right)^{2}} \\
& a=\frac{\sum y}{n}-b \frac{\sum x}{n} \\
& =\bar{y}-b \bar{x} \\
& \mathrm{FV}_{n}=\mathrm{PV}_{0} \times(1+i)^{n} \\
& \mathrm{i}_{\mathrm{e}}+1=\left(1+\frac{i}{m}\right)^{m}
\end{aligned}
$$

## Factor tables

TABLE 1: Future value of R1 at the end of $n$ periods

| n | 0\% | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% | 11\% | 12\% | 13\% | 14\% | 15\% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1 | 1.0000 | 1.0100 | 1.0200 | 1.0300 | 1.0400 | 1.0500 | 1.0600 | 1.0700 | 1.0800 | 1.0900 | 1.1000 | 1.1100 | 1.1200 | 1.1300 | 1.1400 | 1.1500 |
| 2 | 1.0000 | 1.0201 | 1.0404 | 1.0609 | 1.0816 | 1.1025 | 1.1236 | 1.1449 | 1.1664 | 1.1881 | 1.2100 | 1.2321 | 1.2544 | 1.2769 | 1.2996 | 1.3225 |
| 3 | 1.0000 | 1.0303 | 1.0612 | 1.0927 | 1.1249 | 1.1576 | 1.1910 | 1.2250 | 1.2597 | 1.2950 | 1.3310 | 1.3676 | 1.4049 | 1.4429 | 1.4815 | 1.5209 |
| 4 | 1.0000 | 1.0406 | 1.0824 | 1.1255 | 1.1699 | 1.2155 | 1.2625 | 1.3108 | 1.3605 | 1.4116 | 1.4641 | 1.5181 | 1.5735 | 1.6305 | 1.6890 | 1.7490 |
| 5 | 1.0000 | 1.0510 | 1.1041 | 1.1593 | 1.2167 | 1.2763 | 1.3382 | 1.4026 | 1.4693 | 1.5386 | 1.6105 | 1.6851 | 1.7623 | 1.8424 | 1.9254 | 2.0114 |
| 6 | 1.0000 | 1.0615 | 1.1262 | 1.1941 | 1.2653 | 1.3401 | 1.4185 | 1.5007 | 1.5869 | 1.6771 | 1.7716 | 1.8704 | 1.9738 | 2.0820 | 2.1950 | 2.3131 |
| 7 | 1.0000 | 1.0721 | 1.1487 | 1.2299 | 1.3159 | 1.4071 | 1.5036 | 1.6058 | 1.7138 | 1.8280 | 1.9487 | 2.0762 | 2.2107 | 2.3526 | 2.5023 | 2.6600 |
| 8 | 1.0000 | 1.0829 | 1.1717 | 1.2668 | 1.3686 | 1.4775 | 1.5938 | 1.7182 | 1.8509 | 1.9926 | 2.1436 | 2.3045 | 2.4760 | 2.6584 | 2.8526 | 3.0590 |
| 9 | 1.0000 | 1.0937 | 1.1951 | 1.3048 | 1.4233 | 1.5513 | 1.6895 | 1.8385 | 1.9990 | 2.1719 | 2.3579 | 2.5580 | 2.7731 | 3.0040 | 3.2519 | 3.5179 |
| 10 | 1.0000 | 1.1046 | 1.2190 | 1.3439 | 1.4802 | 1.6289 | 1.7908 | 1.9672 | 2.1589 | 2.3674 | 2.5937 | 2.8394 | 3.1058 | 3.3946 | 3.7072 | 4.0456 |
| 11 | 1.0000 | 1.1157 | 1.2434 | 1.3842 | 1.5395 | 1.7103 | 1.8983 | 2.1049 | 2.3316 | 2.5804 | 2.8531 | 3.1518 | 3.4785 | 3.8359 | 4.2262 | 4.6524 |
| 12 | 1.0000 | 1.1268 | 1.2682 | 1.4258 | 1.6010 | 1.7959 | 2.0122 | 2.2522 | 2.5182 | 2.8127 | 3.1384 | 3.4985 | 3.8960 | 4.3345 | 4.8179 | 5.3503 |
| 13 | 1.0000 | 1.1381 | 1.2936 | 1.4685 | 1.6651 | 1.8856 | 2.1329 | 2.4098 | 2.7196 | 3.0658 | 3.4523 | 3.8833 | 4.3635 | 4.8980 | 5.4924 | 6.1528 |
| 14 | 1.0000 | 1.1495 | 1.3195 | 1.5126 | 1.7317 | 1.9799 | 2.2609 | 2.5785 | 2.9372 | 3.3417 | 3.7975 | 4.3104 | 4.8871 | 5.5348 | 6.2613 | 7.0757 |
| 15 | 1.0000 | 1.1610 | 1.3459 | 1.5580 | 1.8009 | 2.0789 | 2.3966 | 2.7590 | 3.1722 | 3.6425 | 4.1772 | 4.7846 | 5.4736 | 6.2543 | 7.1379 | 8.1371 |
| 16 | 1.0000 | 1.1726 | 1.3728 | 1.6047 | 1.8730 | 2.1829 | 2.5404 | 2.9522 | 3.4259 | 3.9703 | 4.5950 | 5.3109 | 6.1304 | 7.0673 | 8.1372 | 9.3576 |
| 17 | 1.0000 | 1.1843 | 1.4002 | 1.6528 | 1.9479 | 2.2920 | 2.6928 | 3.1588 | 3.7000 | 4.3276 | 5.0545 | 5.8951 | 6.8660 | 7.9861 | 9.2765 | 10.7613 |
| 18 | 1.0000 | 1.1961 | 1.4282 | 1.7024 | 2.0258 | 2.4066 | 2.8543 | 3.3799 | 3.9960 | 4.7171 | 5.5599 | 6.5436 | 7.6900 | 9.0243 | 10.5752 | 12.3755 |
| 19 | 1.0000 | 1.2081 | 1.4568 | 1.7535 | 2.1068 | 2.5270 | 3.0256 | 3.6165 | 4.3157 | 5.1417 | 6.1159 | 7.2633 | 8.6128 | 10.1974 | 12.0557 | 14.2318 |
| 20 | 1.0000 | 1.2202 | 1.4859 | 1.8061 | 2.1911 | 2.6533 | 3.2071 | 3.8697 | 4.6610 | 5.6044 | 6.7275 | 8.0623 | 9.6463 | 11.5231 | 13.7435 | 16.3665 |

## TABLE 2: Present value of R1 at the end of $\boldsymbol{n}$ periods

| n | 0\% | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% | 11\% | 12\% | 13\% | 14\% | 15\% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1 | 1.0000 | 0.9901 | 0.9804 | 0.9709 | 0.9615 | 0.9524 | 0.9434 | 0.9346 | 0.9259 | 0.9174 | 0.9091 | 0.9009 | 0.8929 | 0.8850 | 0.8772 | 0.8696 |
| 2 | 1.0000 | 0.9803 | 0.9612 | 0.9426 | 0.9246 | 0.9070 | 0.8900 | 0.8734 | 0.8573 | 0.8417 | 0.8264 | 0.8116 | 0.7972 | 0.7831 | 0.7695 | 0.7561 |
| 3 | 1.0000 | 0.9706 | 0.9423 | 0.9151 | 0.8890 | 0.8638 | 0.8396 | 0.8163 | 0.7938 | 0.7722 | 0.7513 | 0.7312 | 0.7118 | 0.6931 | 0.6750 | 0.6575 |
| 4 | 1.0000 | 0.9610 | 0.9238 | 0.8885 | 0.8548 | 0.8227 | 0.7921 | 0.7629 | 0.7350 | 0.7084 | 0.6830 | 0.6587 | 0.6355 | 0.6133 | 0.5921 | 0.5718 |
| 5 | 1.0000 | 0.9515 | 0.9057 | 0.8626 | 0.8219 | 0.7835 | 0.7473 | 0.7130 | 0.6806 | 0.6499 | 0.6209 | 0.5935 | 0.5674 | 0.5428 | 0.5194 | 0.4972 |
| 6 | 1.0000 | 0.9420 | 0.8880 | 0.8375 | 0.7903 | 0.7462 | 0.7050 | 0.6663 | 0.6302 | 0.5963 | 0.5645 | 0.5346 | 0.5066 | 0.4803 | 0.4556 | 0.4323 |
| 7 | 1.0000 | 0.9327 | 0.8706 | 0.8131 | 0.7599 | 0.7107 | 0.6651 | 0.6227 | 0.5835 | 0.5470 | 0.5132 | 0.4817 | 0.4523 | 0.4251 | 0.3996 | 0.3759 |
| 8 | 1.0000 | 0.9235 | 0.8535 | 0.7894 | 0.7307 | 0.6768 | 0.6274 | 0.5820 | 0.5403 | 0.5019 | 0.4665 | 0.4339 | 0.4039 | 0.3762 | 0.3506 | 0.3269 |
| 9 | 1.0000 | 0.9143 | 0.8368 | 0.7664 | 0.7026 | 0.6446 | 0.5919 | 0.5439 | 0.5002 | 0.4604 | 0.4241 | 0.3909 | 0.3606 | 0.3329 | 0.3075 | 0.2843 |
| 10 | 1.0000 | 0.9053 | 0.8203 | 0.7441 | 0.6756 | 0.6139 | 0.5584 | 0.5083 | 0.4632 | 0.4224 | 0.3855 | 0.3522 | 0.3220 | 0.2946 | 0.2697 | 0.2472 |
| 11 | 1.0000 | 0.8963 | 0.8043 | 0.7224 | 0.6496 | 0.5847 | 0.5268 | 0.4751 | 0.4289 | 0.3875 | 0.3505 | 0.3173 | 0.2875 | 0.2607 | 0.2366 | 0.2149 |
| 12 | 1.0000 | 0.8874 | 0.7885 | 0.7014 | 0.6246 | 0.5568 | 0.4970 | 0.4440 | 0.3971 | 0.3555 | 0.3186 | 0.2858 | 0.2567 | 0.2307 | 0.2076 | 0.1869 |
| 13 | 1.0000 | 0.8787 | 0.7730 | 0.6810 | 0.6006 | 0.5303 | 0.4688 | 0.4150 | 0.3677 | 0.3262 | 0.2897 | 0.2575 | 0.2292 | 0.2042 | 0.1821 | 0.1625 |
| 14 | 1.0000 | 0.8700 | 0.7579 | 0.6611 | 0.5775 | 0.5051 | 0.4423 | 0.3878 | 0.3405 | 0.2992 | 0.2633 | 0.2320 | 0.2046 | 0.1807 | 0.1597 | 0.1413 |
| 15 | 1.0000 | 0.8613 | 0.7430 | 0.6419 | 0.5553 | 0.4810 | 0.4173 | 0.3624 | 0.3152 | 0.2745 | 0.2394 | 0.2090 | 0.1827 | 0.1599 | 0.1401 | 0.1229 |
| 16 | 1.0000 | 0.8528 | 0.7284 | 0.6232 | 0.5339 | 0.4581 | 0.3936 | 0.3387 | 0.2919 | 0.2519 | 0.2176 | 0.1883 | 0.1631 | 0.1415 | 0.1229 | 0.1069 |
| 17 | 1.0000 | 0.8444 | 0.7142 | 0.6050 | 0.5134 | 0.4363 | 0.3714 | 0.3166 | 0.2703 | 0.2311 | 0.1978 | 0.1696 | 0.1456 | 0.1252 | 0.1078 | 0.0929 |
| 18 | 1.0000 | 0.8360 | 0.7002 | 0.5874 | 0.4936 | 0.4155 | 0.3503 | 0.2959 | 0.2502 | 0.2120 | 0.1799 | 0.1528 | 0.1300 | 0.1108 | 0.0946 | 0.0808 |
| 19 | 1.0000 | 0.8277 | 0.6864 | 0.5703 | 0.4746 | 0.3957 | 0.3305 | 0.2765 | 0.2317 | 0.1945 | 0.1635 | 0.1377 | 0.1161 | 0.0981 | 0.0829 | 0.0703 |
| 20 | 1.0000 | 0.8195 | 0.6730 | 0.5537 | 0.4564 | 0.3769 | 0.3118 | 0.2584 | 0.2145 | 0.1784 | 0.1486 | 0.1240 | 0.1037 | 0.0868 | 0.0728 | 0.0611 |

TABLE 3: Future value of an annuity of $R 1$ per period for $n$ periods

| n | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% | 11\% | 12\% | 13\% | 14\% | 15\% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1,0000 | 1,0000 | 1,0000 | 1,0000 | 1,0000 | 1,0000 | 1,0000 | 1,0000 | 1,0000 | 1,0000 | 1,0000 | 1,0000 | 1,0000 | 1,0000 | 1,0000 |
| 2 | 2,0100 | ,0200 | 300 | 400 | . 0500 | ,0600 | ,0700 | . 0800 | ,090 | 100 | 2,110 | 2,1200 | 2,1300 | 2,140 | 2,1500 |
| 3 | 3,0301 | 3,0604 | 3,0909 | 3,1216 | 3,1525 | ,1836 | 3,2149 | 3,246 | 3,2781 | 3,3100 | 3,3421 | 3,3744 | 3,4069 | 3,4396 | 3,4725 |
| 4 | 4,0604 | 4,1216 | , 1836 | 4,2465 | 4,310 | 4,3746 | 4,4399 | 4,5061 | 4,5731 | 4,6410 | 4,7097 | 4,7793 | 4,8498 | 4,9211 | 4,9934 |
| 5 | 5,1010 | 5,2040 | 5,3091 | 5,4163 | 5,525 | 5,637 | 5,750 | 5,866 | 5,9847 | 6,105 | 6,227 | 6,3528 | 6,4803 | 6,6101 | 6,7424 |
| 6 | 6,1520 | 6,308 | 6,4684 | 633 | 801 | 6,9753 | 1533 | 335 | 7,5233 | 715 | 7,912 | 8,1152 | 8,3227 | 8,5355 | 8,7537 |
| 7 | 7,2135 | 7,4343 | 7,6625 | 7,898 | 42 | 8,393 | 8,6540 | 8,9228 | 9,200 | 9,4872 | 9,7833 | 10,0890 | 10,4047 | 10,7305 | 11,0668 |
| 8 | 8,285 | 8,5 | 8,8923 | 14 | 9,5491 | 9,8975 | 10,2598 | ,636 | ,0285 | 11,435 | 11,85 | 12,2997 | 12,7573 | 13,2328 | 13,7268 |
| 9 | 9,3685 | 9,7 | 10 | 10 | 11 | 11,4913 | 11,9780 | 12,4876 | 02 | 57 | 14,1640 | 7757 | 15,415 | 16,0853 | 16,7858 |
| 10 | 10,462 | 10,949 | 11,463 | 12,006 | 12,5779 | 13,180 | 13,8164 | ,486 | 192 | 93 | 722 | 7,5487 | 18,4197 | 19,337 | 20,3037 |
| 11 | 11,566 | 12, | 12,807 | 13 | 14 | 14,9716 | 15,7836 | 16,6455 | , | 53 | ,56 | ,65 | 21,8143 | ,0445 | 3493 |
| 12 | 12,682 | 13,412 | 14,192 | 15,025 | 15 | 16,8699 | 17,8885 | 18,9771 | 140 | 21,3843 | 22,7132 | ,133 | 5,65 | 7,2707 | 9,0017 |
| 13 | 13,8093 | 14,6803 | 15,6178 | 16,626 | 17 | 18,882 | 14 | 21,4953 | 953 | 522 | 26,21 | 28,0291 | 9,984 | 32,0887 | 34,3519 |
| 14 | 14,9474 | 15,9739 | 17,0863 | 18,291 | 19,598 | 21,015 | 22,550 | 214 | 26,0192 | 7,9750 | 30,0949 | 32,3926 | 34,8827 | 37,5811 | 0,5047 |
| 15 | 16,0969 | 17,2934 | 18,5989 | 20,023 | 21,578 | 23,2760 | 25,129 | 27,1521 | 29,3609 | 31,7725 | 34,4054 | 37,2797 | 40,4175 | 43,8424 | 47,5804 |
| 16 | 17,2579 | 18,639 | 20,156 | 21,824 | 23,657 | 25,6725 | 27,888 | 30,3243 | 33,0034 | 35,9497 | ,1899 | 42,7533 | 46,67 | 50,9804 | 55,7175 |
| 17 | 18,4304 | 20,012 | 21,761 | 23,697 | 25,840 | 28,212 | 30,840 | 33,7502 | 36,9737 | 40,5447 | 44,5008 | 48,8837 | 53,7391 | 59,1176 | 65,0751 |
| 18 | 19,6147 | 21,4123 | 23, | 25,645 | 28,132 | 30,9057 | 33,999 | 37,4502 | 3013 | 45,5992 | 50,3959 | 55,7497 | 61,7251 | 68,3941 | 75,8364 |
| 19 | 20,8109 | 22,8406 | 25,1169 | 27,6712 | 30,5390 | 33,7600 | 37,379 | 41,4463 | 46,0185 | 51,1591 | 56,9395 | 63,4397 | 70,7494 | 78,9692 | 88,2118 |
| 20 | 22,0190 | 24,297 | 26,8704 | 9,7781 | 33,0660 | 36,7856 | 40,995 | 45,7620 | 51,1601 | 57,2750 | 64,2028 | 72,0524 | 80,9468 | 91,0249 | 102,4436 |

TABLE 4: Present value of an annuity of R1 per period for $n$ periods

| n | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% | 11\% | 12\% | 13\% | 14\% | 15\% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0,9901 | 0,9804 | 0,9709 | 0,9615 | 0,9524 | 0,9434 | 0,9346 | 0,9259 | 0,9174 | 0,9091 | 0,9009 | 0,8929 | 0,8850 | 0,8772 | 0,8696 |
| 2 | 1,9704 | 1,9416 | 1,9135 | 1,8861 | 1,8594 | 1,8334 | 1,8080 | 1,7833 | 1,7591 | 1,7355 | 1,7125 | 1,6901 | 1,6681 | 1,6467 | 1,6257 |
| 3 | 2,9410 | 2,8839 | 2,8286 | 2,7751 | 2,7232 | 2,6730 | 2,6243 | 2,5771 | 2,5313 | 2,4869 | 2,4437 | 2,4018 | 2,3612 | 2,3216 | 2,2832 |
| 4 | 3,9020 | 3,8077 | 3,7171 | 3,6299 | 3,5460 | 3,4651 | 3,3872 | 3,3121 | 3,2397 | 3,1699 | 3,1024 | 3,0373 | 2,9745 | 2,9137 | 2,8550 |
| 5 | 4,8534 | 4,7135 | 4,5797 | 4,4518 | 4,3295 | 4,2124 | 4,1002 | 3,9927 | 3,8897 | 3,7908 | 3,6959 | 3,6048 | 3,5172 | 3,4331 | 3,3522 |
| 6 | 5,7955 | 5,6014 | 5,4172 | 5,2421 | 5,0757 | 4,9173 | 4,7665 | 4,6229 | 4,4859 | 4,3553 | 4,2305 | 4,1114 | 3,9975 | 3,8887 | 3,7845 |
| 7 | 6,7282 | 6,4720 | 6,2303 | 6,0021 | 5,7864 | 5,5824 | 5,3893 | 5,2064 | 5,0330 | 4,8684 | 4,7122 | 4,5638 | 4,4226 | 4,2883 | 4,1604 |
| 8 | 7,6517 | 7,3255 | 197 | 27 | 632 | ,2098 | 713 | 5,7466 | 5,5348 | 5,3349 | 5,1461 | 4,9676 | 4,7988 | 4,6389 | 4,4873 |
| 9 | 8,5660 | 622 | 861 | 353 | 078 | 017 | 6,5152 | 246 | 5,995 | 5,7590 | 5,5370 | 5,3282 | 5,1317 | 4,9464 | 4,7716 |
| 10 | 9,4713 | 8,9826 | 8,5302 | 8,1109 | 217 | 601 | 236 | 101 | 6,4177 | 6,1446 | 5,8892 | 5,6502 | 5,4262 | 5,2161 | 5,0188 |
| 11 | 10,3676 | 9,7868 | 9,2526 | 8,7605 | 8,3064 | 8869 | 987 | 390 | , 8052 | 6,4951 | 6,2065 | 5,9377 | 5,6869 | 5,4527 | 5,2337 |
| 12 | 11,2551 | 10,5753 | 9,9540 | 9,3851 | 8,8633 | 8,3838 | ,9427 | 7,5361 | ,1607 | 6,8137 | ,4924 | 6,1944 | 5,9176 | 5,6603 | 5,4206 |
| 13 | 12,1337 | 11,3484 | 10,6350 | 9,9856 | 9,3936 | 8,8527 | 8,3577 | 7,9038 | 7,4869 | 7,1034 | 6,7499 | 6,4235 | 6,1218 | 5,8424 | 5,5831 |
| 14 | 13,0037 | 12,106 | 11,2961 | 10,563 | 9,8986 | 9,2950 | 8,7455 | 8,2442 | 7,7862 | 7,3667 | 6,9819 | 6,6282 | 6,3025 | 6,0021 | 5,7245 |
| 15 | 13,8651 | 12,8493 | 11,9379 | 11,118 | 10,3797 | 9,7122 | 9,1079 | 8,5595 | 8,0607 | 7,6061 | 7,1909 | 6,8109 | 6,4624 | 6,1422 | 5,8474 |
| 16 | 14,7179 | 13,5777 | 12,5611 | 11,6523 | 10,8378 | 10,1059 | 9,4466 | 8,8514 | 8,3126 | 7,8237 | 7,3792 | 6,9740 | 6,6039 | 6,2651 | 5,9542 |
| 17 | 15,5623 | 14,2919 | 13,1661 | 12,1657 | 11,2741 | 10,4773 | 9,7632 | 9,1216 | 8,5436 | 8,0216 | 7,5488 | 7,1196 | 6,7291 | 6,3729 | 6,0472 |
| 18 | 16,3983 | 14,9920 | 13,7535 | 12,6593 | 11,6896 | 10,8276 | 10,0591 | 9,3719 | 8,7556 | 8,2014 | 7,7016 | 7,2497 | 6,8399 | 6,4674 | 6,1280 |
| 19 | 17,2260 | 15,6785 | 14,3238 | 13,1339 | 12,0853 | 11,1581 | 10,3356 | 9,6036 | 8,9501 | 8,3649 | 7,8393 | 7,3658 | 6,9380 | 6,5504 | 6,1982 |
| 20 | 18,0456 | 16,3514 | 14,8775 | 13,5903 | 12,4622 | 11,4699 | 10,5940 | 9,8181 | 9,1285 | 8,5136 | 7,9633 | 7,4694 | 7,0248 | 6,6231 | 6,2593 |

