## FACULTY OF SCIENCE

| DEPARTMENT OF MATHEMATICS AND APPLIED MATHEMATICS |  |  |
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| MODULE: MATH | ATICSFOR FINANCE AN |  |
| CAMPUS: SWC |  |  |
| ASSESSMENT: SUPP | MENTARY EXAM |  |
| DATE: | JULY 2019 |  |
| ASSESSORS: | MS M JUGA <br> MR T MOHUBEDU <br> MR MSW POTGIETER |  |
| INTERNAL MODERATOR: | DR J MBA |  |
| DURATION: | 2 HOURS |  |

INITIALS AND SURNAME:

STUDENT NUMBER:

CONTACT NUMBER:

NUMBER OF PAGES: 10 (INCLUDING COVER PAGE)
INSTRUCTIONS:

- ANSWER ALL THE QUESTIONS IN PEN.
- ALL GRAPHS MUST BE DRAWN IN PEN.
- NO PENCIL OR TIPEX ALLOWED.
- SHOW ALL THE NECESSARY CALCULATIONS CLEARLY.
- IF FORMULAS ARE USED THEY MUST BE STATED AS MARKS ARE GIVEN TO THEM.
- ONLY SCIENTIFIC CALCULATORS ARE ALLOWED.
- IF NECESSARY, ROUND OFF TO TWO DECIMAL PLACES.
- THE QUESTIONS CAN BE ANSWERED IN ANY ORDER.


## Question 1

Simplify the following expressions
1.1 $(3 x+1)^{2}-4(x+1)(2 x-5)$
$1.2 \frac{3 x^{2}-x}{x-1}-\frac{3 x}{x+2}$
[2]
$1.3\left(\frac{4 x^{4} \cdot x^{3}}{2 x^{-2}}\right)^{2}$
[3]
$1.4 \quad \ln (x)+\ln \left(x^{3}\right)+1$

$$
\begin{equation*}
1.5 \quad \frac{x^{2}-3 x}{x+1} \div \frac{x}{x^{2}+3 x+2} \tag{3}
\end{equation*}
$$

## Question 2

Rationalize the denominator in the following fractions:
$2.1 \frac{x}{5-\sqrt{2 x}}$
$2.2 \quad \frac{4 x}{\sqrt[5]{x \cdot y^{7}}}$

## Question 3

Solve for $x$ in the following equations:

$$
\begin{equation*}
3.1 \quad \frac{2 x-1}{2 x^{2}+3 x-2}=\frac{x}{x+3} \tag{3}
\end{equation*}
$$

$3.25(x+1)=\frac{1}{2}(x+4)+8 x-2$
$3.3 \quad \log _{5}(x+3)=\log _{5}(4 x+5)$
$3.4 \quad 10 e^{3 x-7}=5$

## Question 4

Simplify the following operation by making use of long division:

$$
\left(x^{4}+3 x^{2}\right) \div(x+4)
$$

## Question 5

Given the function, $f(x)=3^{x-1}-4$, determine the following:
5.1 The $y$ intercept(s).
5.2 State the domain and range of $f(x)$.
5.3 Complete the following table for the function:

| $x$ | -1 | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ |  |  |  |  |  |  |

### 5.4 Sketch the graph of $f(x)$.

6.1 Sketch $g(x)=-5 x$ indicating all intercepts.
6.2 Find the equation of the straight line that passes through the points: $(1 ; 4)$ and $(-5 ; 9)$.

## Question 7

Factorise the following expressions completely:
$7.1 \quad 2 x^{4}-16$
$7.2 \quad 64 a^{3}+8$

## Question 8

8.1 Convert the following into logarithmic form:
8.1.1 $3^{2}=6 x$
8.1.2 $121=11^{2}$
8.2 Convert the following to an equivalent exponential form:
8.2.1 $\log _{x} m=n$
8.2.2 $\log _{7} a=x$

## Question 9

Solve the following systems
9.1 $\left\{\begin{array}{c}2 x-2 y=4 \\ y=-9 x+12\end{array}\right.$
$9.2\left\{\begin{array}{c}y=x \\ x+y=0\end{array}\right.$

## Question 10

[5]
A local building supply store find that the demand function for their concrete mixer is:

$$
p=2,000-25 q
$$

10.1 Determine a revenue function for the product.

### 10.2 Determine the maximum revenue they can expect for the product.

10.3 If the demand for the concrete mixer is 50 units, determine the price.

## Question 11

Surefire LLC finds that their assets total $R 100200.00$ and their liabilities $R 67500.00$. They decide to take out a loan to buy an additional delivery vehicle whilst maintaining a current ratio of more than $C R=3.2$. Determine the maximum amount they can borrow.

Use this space if you want to redo a question. Clearly indicate at the question that the answer is on Page 10.

