



**PROGRAM** : BACCALAUREUS INGENERIAE  
CIVIL ENGINEERING

**SUBJECT** : GEOTECHNICAL ENGINEERING 3B

**CODE** : GTG3B21

**DATE** : SSA EXAMINATION  
JUN 2016

**DURATION** : 3h

**WEIGHT** : 50: 50

**TOTAL MARKS** : 100

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**ASSESSOR** : DR. M FERENTINOU

**MODERATOR** : PROF. FN OKONTA File Number

**NUMBER OF PAGES** : 3 PAGES, 2 ANNEXURES, GRAPH PAPER,

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**INSTRUCTIONS** : ONLY ONE POCKET CALCULATOR PER CANDIDATE  
MAY BE USED.  
QUESTIONS PAPERS MUST BE HANDED IN  
ANSWER ALL QUESTIONS.  
COMPLETE THE FRONT PAGE OF THE EXAMINATION  
BOOKLET CORRECTLY WITH RESPECT TO DETAILS  
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**QUESTION 1**

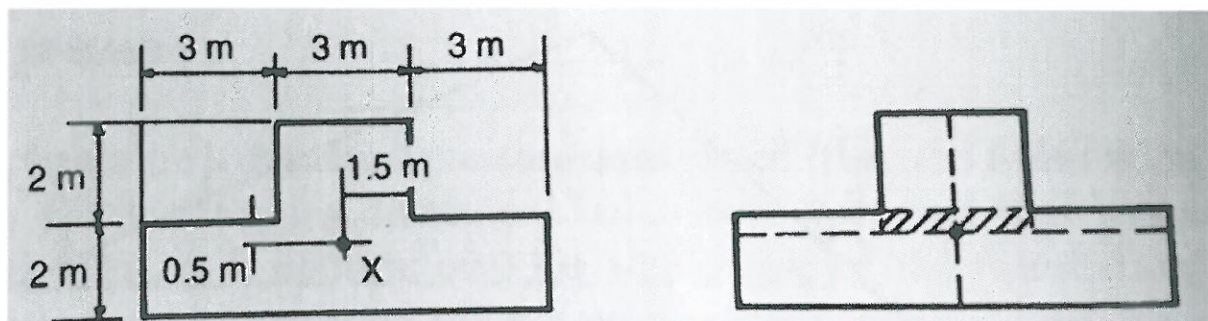
The components of stress tensor are given as follows:  $\sigma_x = 210 \text{ kPa}$ ,  $\sigma_y = 375.00 \text{ kPa}$  and  $\tau_{xy} = 75 \text{ kPa}$ .

- Determine the magnitude and directions, of major and minor principal stresses.
- Determine the magnitude and directions of the maximum shear stress.
- Determine the normal and shear stresses acting on a soil element inclined  $55^\circ$  from the horizontal plane. Give both analytical and graphical solution.

**QUESTION 2 (20 MARKS)**

The plan of a foundation is given below. The uniform pressure on soil is  $P = 40 \text{ kN/m}^2$ .

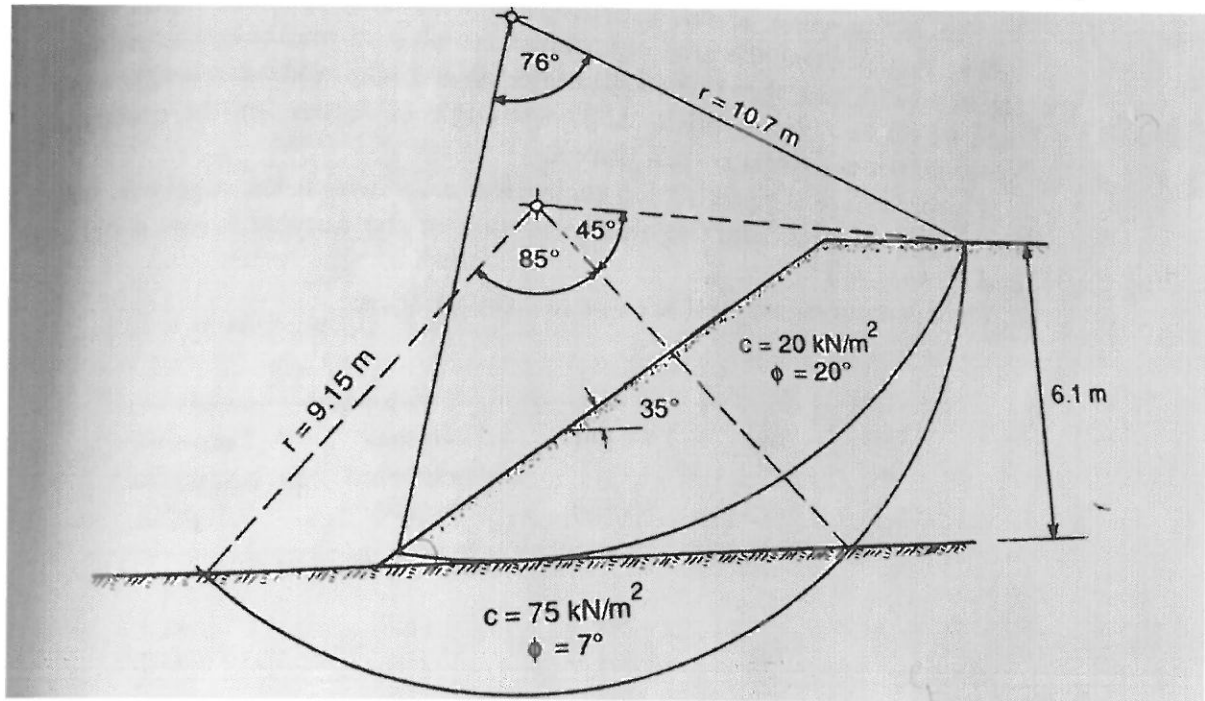
- Determine the vertical stress increments due to the foundation load to a depth of 5m below point X. (You can use the selection rectangles indicated in the Figure.)
- Determine the vertical stress increment at a point 3m below the foundation and 4m from its centre along one of the axis of the axis of symmetry.

**QUESTION 3 (10 MARKS)**

A soft, normally consolidated clay layer is 15m thick with a natural moisture content  $w = 45\%$ . The clay has a saturated unit weight  $\gamma_{\text{sat}} = 17.2 \text{ kN/m}^3$ , a particle specific gravity  $G_s = 2.68$  and a liquid limit  $LL = 65\%$ . A foundation load will subject the centre of the layer to vertical stress increase of  $10.0 \text{ kN/m}^2$ . Determine the value of the settlement of the foundation, if ground water level is at the surface of the clay.

**QUESTION 4 (30 MARKS)**

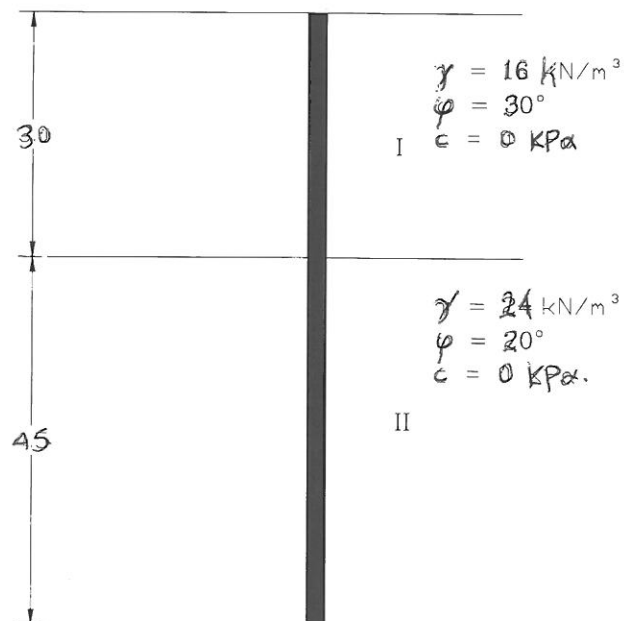
The embankment in the figure below is made up from a soil with  $c = 20 \text{ kN/m}^2$  and  $\phi = 20^\circ$ . The soil on which the embankment sits has  $\phi = 7^\circ$  and  $c = 75 \text{ kN/m}^2$ . For both soils  $\gamma = 19.3 \text{ kN/m}^3$ . Determine the factor of safety only for the shallow and dip slip surfaces shown.



### QUESTION 5 (20 MARKS)

Details of the soil retained behind a smooth wall are given in the Figure below. The upper layer I of sand of unit weight  $\gamma = 16\text{kN/m}^3$ , having shear strength parameters  $c = 0$  and  $\phi = 30^\circ$  and a lower layer II of sandy clay of unit weight  $\gamma = 24\text{kN/m}^3$  having shear strength parameters  $c = 0$  and  $\phi = 20^\circ$ .

- a. Draw the diagram of the pressure distribution on the back of the wall and  
b. determine the total horizontal active thrust acting on the back of the wall.  
Determine its point of application, (use Coulomb theory).





# APPENDIX

You may use any of the following equations and tables

$$r = \sqrt{\left(\frac{\sigma_z - \sigma_x}{2}\right)^2 + \tau_{zx}^2}$$

$$\sigma_1 = \frac{\sigma_x + \sigma_z}{2} + \sqrt{\left(\frac{\sigma_x - \sigma_z}{2}\right)^2 + \tau_{zx}^2}$$

$$\sigma_3 = \frac{\sigma_x + \sigma_z}{2} - \sqrt{\left(\frac{\sigma_x - \sigma_z}{2}\right)^2 + \tau_{zx}^2}$$

$$\tau_{\max} = \frac{\sigma_1 - \sigma_3}{2}$$

$$\theta_1 = \frac{1}{2} \cos^{-1} \sqrt{\frac{1}{1 + [2\tau_{zx}/(\sigma_z - \sigma_x)]^2}}$$

$$\sigma = \frac{\sigma_1 + \sigma_3}{2} \pm \frac{\sigma_1 - \sigma_3}{2} \cos 2\theta$$

$$\tau = \frac{\sigma_1 - \sigma_3}{2} \sin 2\theta$$

$$\tau_n = -\frac{(\sigma_x - \sigma_y)}{2} \sin 2\theta + \tau_{xy} \cos 2\theta$$

$$\sigma_n = \frac{(\sigma_x + \sigma_y)}{2} + \frac{(\sigma_x - \sigma_y)}{2} \cos 2\theta + \tau_{xy} \sin 2\theta$$

$$s_c = m_v \Delta \sigma' H$$

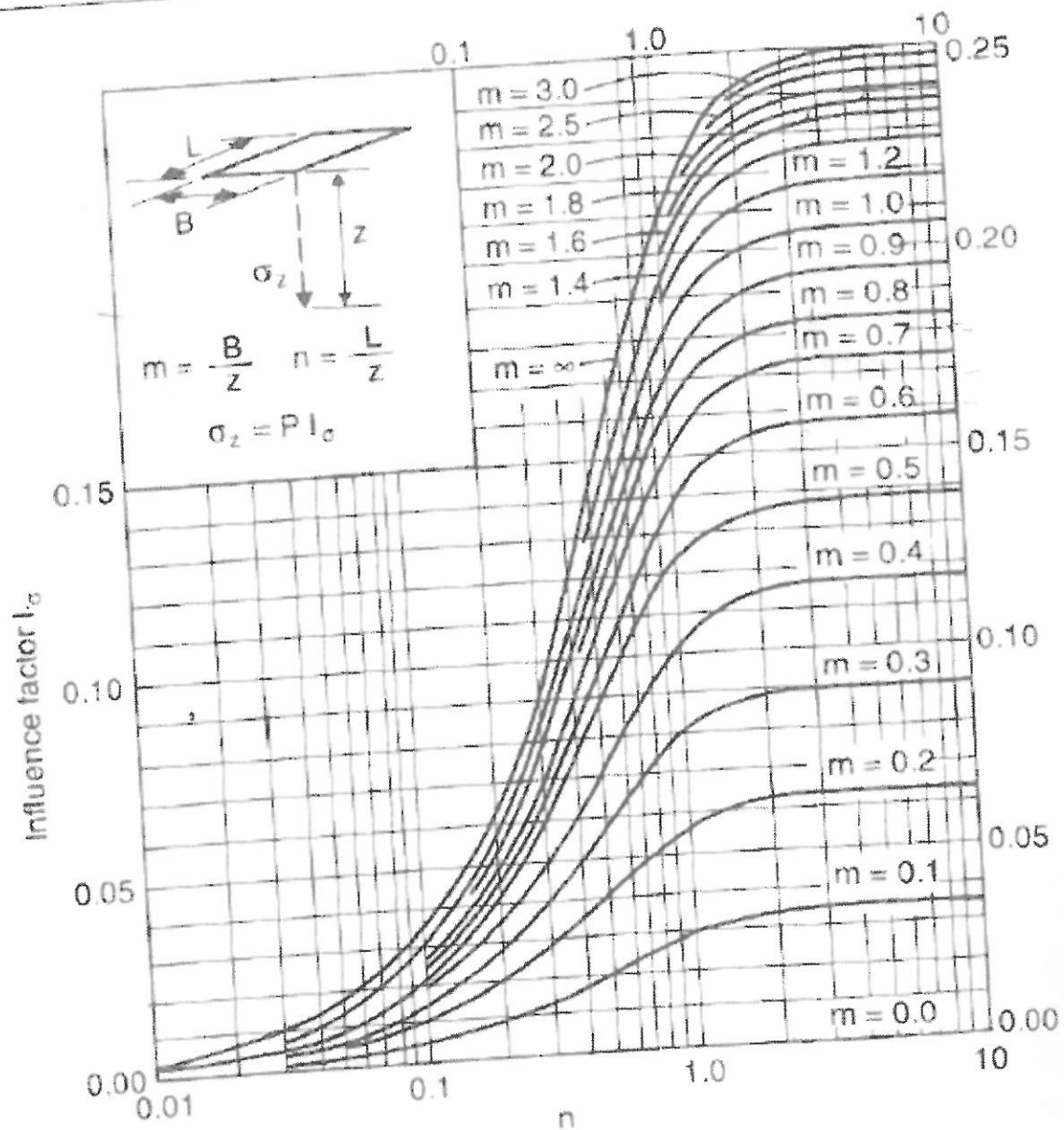
$$s_c = \frac{e_0 - e_1}{1 + e_0} H$$

$$Cc := 0.009 (wL - 10\%)$$

$$\delta c = \frac{C_c}{1 + e_0} \log \frac{\sigma'_1}{\sigma'_0} H$$

$$s_c = \frac{C_c \log(\sigma'_1/\sigma'_0)}{1 + e_0} H$$

### Soil Mechanics



$$F = \frac{c' L_a + \tan \phi' \Sigma (W \cos \alpha - id)}{\Sigma W \sin \alpha}$$

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi}$$

$$K_p = \frac{1 + \sin \phi}{1 - \sin \phi}$$

$$P_a = \frac{1}{2} K_a \gamma H^2 \quad P_p = \frac{1}{2} K_p \gamma H^2$$

$$K_a = \left( \frac{\frac{\sin(\alpha - \phi)}{\sin \alpha}}{\sqrt{[\sin(\alpha + \delta)]} + \sqrt{\left[ \frac{\sin(\phi + \delta) \sin(\phi - \beta)}{\sin(\alpha - \beta)} \right]}} \right)^2$$

$$K_p = \left( \frac{\frac{\sin(\alpha + \phi)}{\sin \alpha}}{\sqrt{[\sin(\alpha - \delta)]} - \sqrt{\left[ \frac{\sin(\phi + \delta) \sin(\phi + \beta)}{\sin(\alpha - \beta)} \right]}} \right)^2$$







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**QUESTION 1 (20 MARKS)**

The components of stress tensor are given as follows:  $\sigma_x = 25\text{kPa}$   $\sigma_y = 50\text{kPa}$  and  $\tau_{xy} = -70\text{kPa}$ .

- Determine the magnitude and directions, of major and minor principal stresses.
- Determine the magnitude and directions of the maximum shear stress.
- Determine the normal and shear stresses acting on a soil element inclined  $30^\circ$  from the horizontal plane. Give both analytical and graphical solution.

**QUESTION 2 (20 MARKS)**

A 4.5 square foundation exerts a uniform pressure  $P = 200\text{kN/m}^2$  on a soil mass.

- Determine the vertical stress increments due to the foundation load to a depth of 10m below its centre.
- Determine the vertical stress increment at a point 3m below the foundation and 4m from its centre along one of the axis of symmetry.

**QUESTION 3 (20 MARKS)**

The following results were obtained from an oedometer test on a specimen of saturated clay:

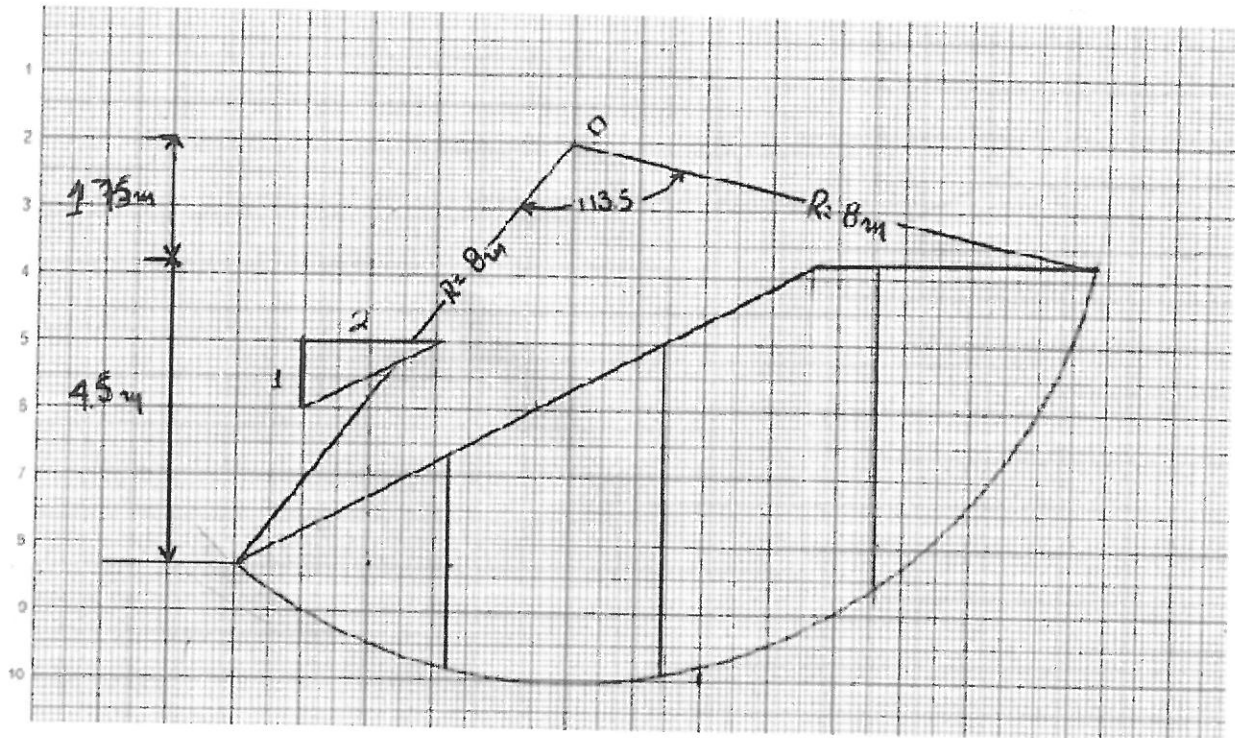
Pressure ( $\text{kN/m}^2$ )	27	54	107	214	429	214	107	54
Void ratio	1.243	1.217	1.144	1.068	0.994	1.001	1.012	1.024

A layer of this clay 8m thick lies below a 4m depth of sand, the water table being at the surface. The saturated unit weight of soils is  $19\text{kN/m}^3$ . A 4m depth of fill of unit weight  $21\text{kN/m}^3$  is placed on the sand over an extensive area. Determine the final settlement due to consolidation of the clay.

**QUESTION 4 (20 MARKS)**

Determine the factor of safety for the given failure surface, for the slope in figure below. The unit weight is  $\gamma = 20\text{ kN/m}^3$ , and relevant strength parameters  $c = 8\text{kPa}$  and  $\phi = 20^\circ$ . Assume that there is no allowance made for a tension crack to develop. Use Fellenius analysis method.

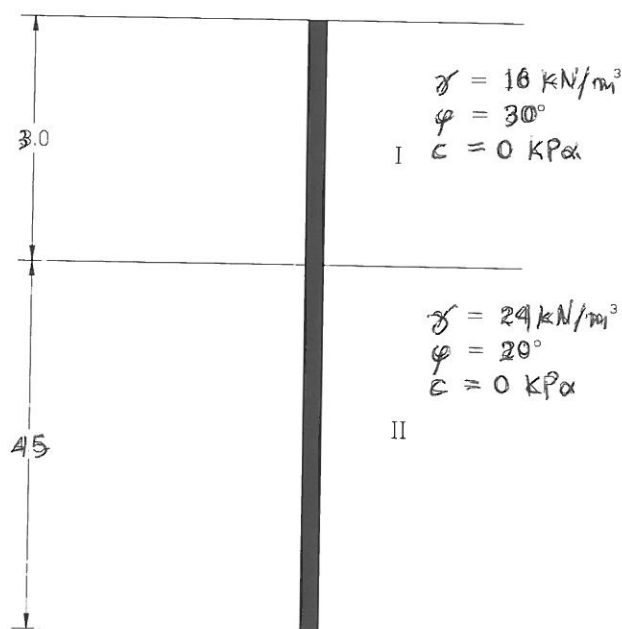
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### QUESTION 5 (20 MARKS)

Details of the soil retained behind a smooth wall are given in the Figure below. The upper layer I of sand of unit weight  $\gamma = 16 \text{ kN/m}^3$ , having shear strength parameters  $c = 0$  and  $\phi = 30^\circ$  and a lower layer II of sandy clay of unit weight  $\gamma = 24 \text{ kN/m}^3$  having shear strength parameters  $c = 0$  and  $\phi = 20^\circ$ .

- Draw the diagram of the pressure distribution on the back of the wall
- Determine the total horizontal active thrust acting on the back of the wall, determine its point of application, (use Rankine theory).





# APPENDIX

You may use any of the following equations and tables

$$r = \sqrt{\left(\frac{\sigma_z - \sigma_x}{2}\right)^2 + \tau_{zx}^2}$$

$$\sigma_1 = \frac{\sigma_x + \sigma_z}{2} + \sqrt{\left(\frac{\sigma_z - \sigma_x}{2}\right)^2 + \tau_{zx}^2}$$

$$\sigma_3 = \frac{\sigma_x + \sigma_z}{2} - \sqrt{\left(\frac{\sigma_z - \sigma_x}{2}\right)^2 + \tau_{zx}^2}$$

$$\tau_{\max} = \frac{\sigma_1 - \sigma_3}{2}$$

$$\theta_1 = \frac{1}{2} \cos^{-1} \sqrt{\frac{1}{1 + [2\tau_{zx}/(\sigma_z - \sigma_x)]^2}}$$

$$\sigma = \frac{\sigma_1 + \sigma_3}{2} \pm \frac{\sigma_1 - \sigma_3}{2} \cos 2\theta$$

$$\tau = \frac{\sigma_1 - \sigma_3}{2} \sin 2\theta$$

$$\tau_n = -\frac{(\sigma_x - \sigma_y)}{2} \sin 2\theta + \tau_{xy} \cos 2\theta$$

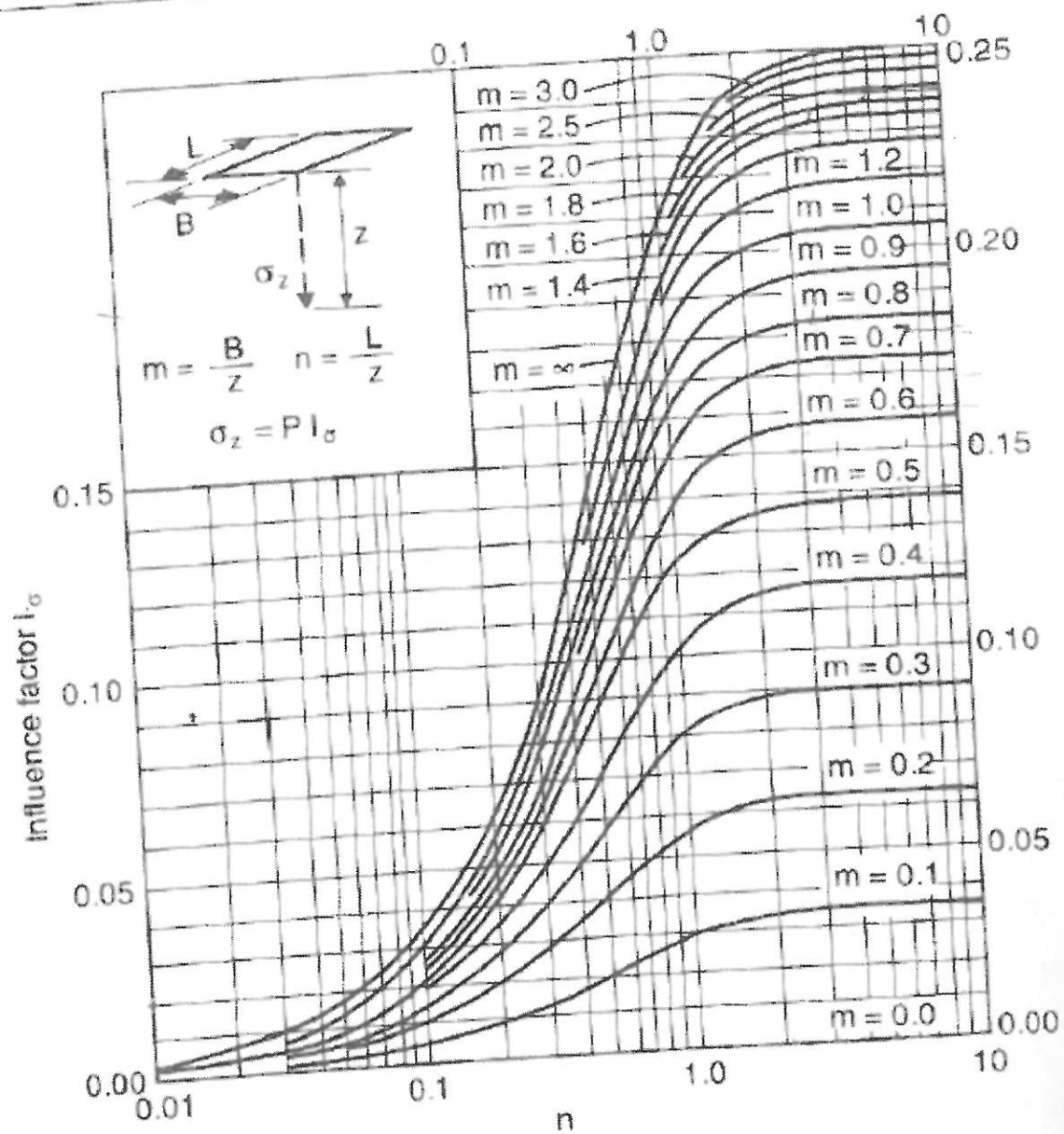
$$\sigma_n = \frac{(\sigma_x + \sigma_y)}{2} + \frac{(\sigma_x - \sigma_y)}{2} \cos 2\theta + \tau_{xy} \sin 2\theta$$

$$s_c = m_v \Delta \sigma' H$$

$$s_c = \frac{e_0 - e_1}{1 + e_0} H$$

$$s_c = \frac{C_c \log(\sigma'_1/\sigma'_0)}{1 + e_0} H$$

## Soil Mechanics



$$F = \frac{c' L_a + \tan \phi' \Sigma (W \cos \alpha - ul)}{\Sigma W \sin \alpha}$$

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi}$$

$$K_p = \frac{1 + \sin \phi}{1 - \sin \phi} \quad P_a = \frac{1}{2} K_a \gamma H^2$$









