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## FACULTY OF SCIENCE

### DEPARTMENT OF MATHEMATICS

NATIONAL DIPLOMA IN ENGINEERING:  
*ELECTRICAL, MECHANICAL, INDUSTRIAL AND MINING ENGINEERING, COMPUTER  
SYSTEMS, MINERALS SURVEYING*

**MODULE** MAT2AW2  
**ENGINEERING MATHEMATICS 2**  
**CAMPUS** DFC

### NOVEMBER EXAMINATION

**DATE** 09/11/2014

**SESSION** 08:30 – 11:30

**ASSESSORS**

**MR IK LETLHAGE**

**INTERNAL MODERATOR**

**MR P SELOANE**

**DURATION** 3 HOURS

**MARKS** 100

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**SURNAME AND INITIALS:** \_\_\_\_\_

**STUDENT NUMBER:** \_\_\_\_\_

**COURSE:** \_\_\_\_\_

**LECTURER:** \_\_\_\_\_

**CONTACT NO:** \_\_\_\_\_

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**NUMBER OF PAGES:** 20 (VERIFY THAT THE NUMBER OF PAGES IN YOUR SCRIPT IS CORRECT)

**INSTRUCTIONS** : ANSWER ALL THE QUESTIONS  
USE THE BLANK PAGES AT THE BACK TO DO ROUGH WORK  
NO PAGES SHOULD BE REMOVED FROM THIS PAPER.  
USE ONLY BLUE OR BLACK INK TO WRITE. NO PENCIL.

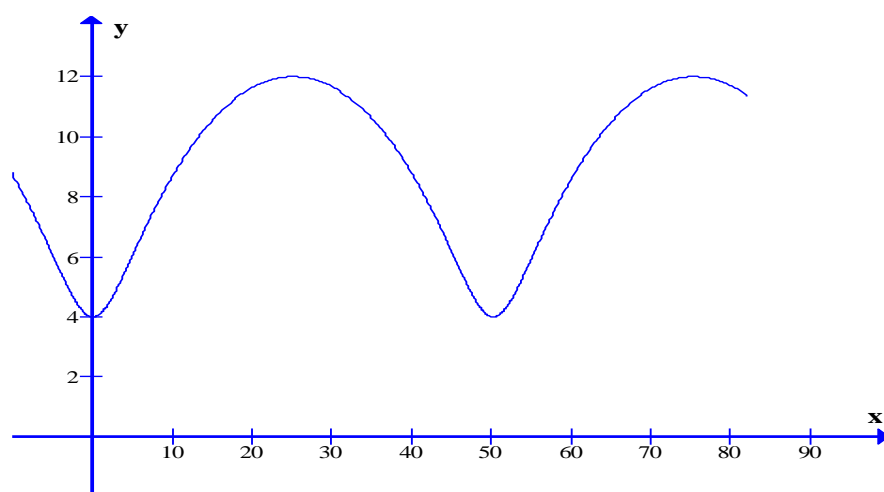
**REQUIREMENTS** : INFORMATION BOOKLET  
: NON-PROGRAMMABLE SCIENTIFIC CALCULATOR



[illegible]

1.4 The curtate cycloid is defined by the following parametric equations:

$x = 8\theta - 4\sin\theta$ ,  $y = 8 - 4\cos\theta$  and part of the graph is shown below.

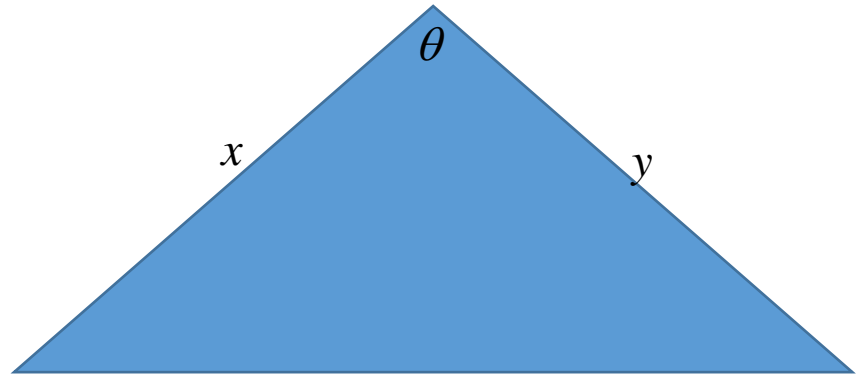


Find  $\frac{d^2y}{dx^2}$  in its simplest form.

(5)




2.2 A surveyor wants to calculate the area of a triangular field. She measures two adjacent sides and finds that the one side has length  $x = 155m$  and the other side has length  $y = 220m$ . Each of these measurements has a possible error of  $0.3m$ . She measures the angle between the two sides and finds that it is  $\theta = 30^\circ$ , with a possible error of  $0.23^\circ$ . Find the maximum error in the calculation of the area,  $A$ , of the field. The area is given by  $A = \frac{1}{2}xy \sin \theta$ .

[illegible]

2.3 A right circular cone is filled with water. Let  $h$  denote the height and  $r$  the radius of the water level at a given instant. Suppose that the cone has a hole at the bottom, denoted by  $O$ , and water is dripping through this hole. If the water is leaving the cone at a rate of  $0.001m^3 / \text{min}$  and the height of the water is decreasing at a rate of  $0.3m / \text{min}$  at the instant when  $h = 1m$  and  $r = 0.75m$ , calculate the rate at which the radius is changing. Is this an increase or a decrease? Give reasons for your answer.

(6)






(6)

[illegible]

(4)

[illegible]

(6)

[illegible]

(6)

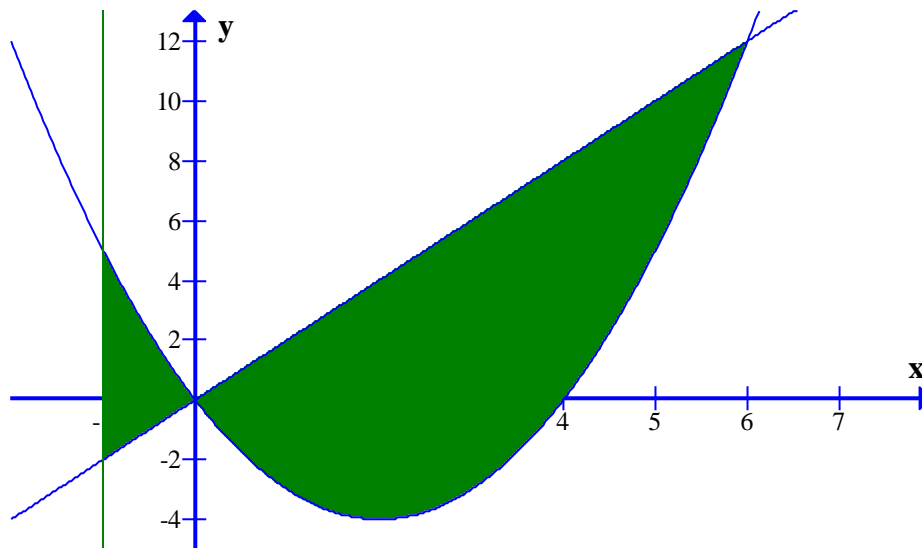
[illegible]

(6)

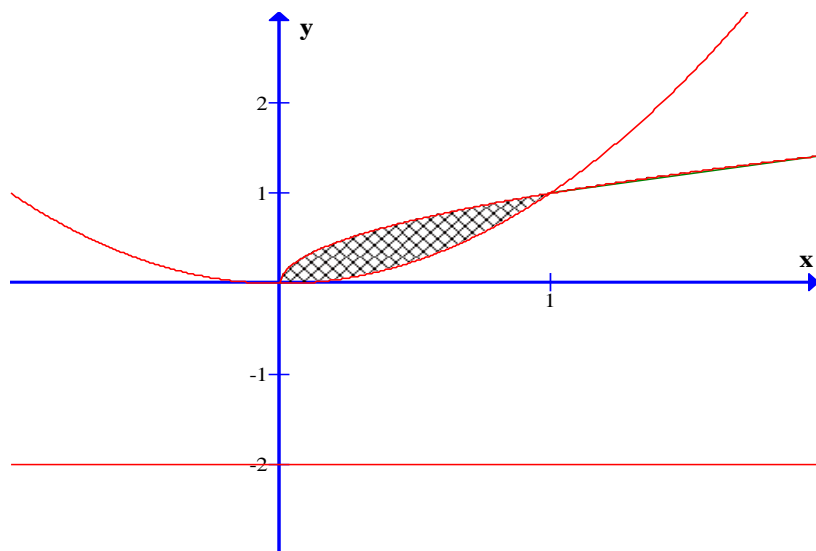
[illegible]

### QUESTION 4

4.1 Calculate the area of the region bounded by the curves  $y = 2x$ ,  $y = x^2 - 4x$  and  $x = -1$ . (5)

[illegible]

4.2 The region bounded by the curves  $y = x^2$  and  $x = y^2$  is revolved about the line  $y = -2$ . Calculate the volume of the resulting solid. (4)




### QUESTION 5

5.1 The rate of change of population is directly proportional to the population and is modelled by the differential equation  $\frac{dP}{dt} = kP$ . Here  $P$  is a function of time  $t$  and  $k$  is a constant.

In 1995 the world population was estimated to be 5.74 billion persons, and in 2000 it was about 6.51 billion. Estimate the 2012 population. (6)

[illegible]

5.2 Solve the differential equation  $\frac{dy}{dx} = \frac{x-y}{x+y}$  (5)



[illegible]

5.3 Show that the differential equation below is exactn and then solve it:

$$(3x^2y^2 + 2xy)dx + (2x^3y + x^2)dy = 0. \quad (4)$$

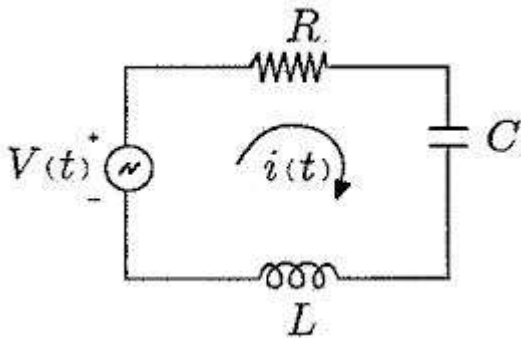
[illegible]

5.4 A resistor with resistance  $R = 10\Omega$ , an inductor with inductance  $L = 2H$  and a battery with electromotive force  $E = 40V$  are connected in series, as shown in the diagram below. According to Kirchhoff's Law,

Potential drop across  $R$  + Potential drop across  $L$  + Potential drop across  $E = 0$ .

That is,  $10I + 2\frac{dI}{dt} + (-E) = 0$ , which simplifies to the differential equation  $2\frac{dI}{dt} + 10I = E$ .

Find the current,  $I$ , subject to the initial condition  $I(0) = 0$ . (5)

[illegible]

5.5 Solve the differential equation  $\frac{dy}{dx} = \frac{2y}{x} - \frac{y^2}{x^2}$  (7)

[illegible]

**[29]**

**MARKS AVAILABLE : 103**

**TOTAL MARKS : 100**

**USE THIS SPACE TO RE-DO ANY QUESTION YOU MAY HAVE CANCELLED**

[illegible]