



UNIVERSITY
OF
JOHANNESBURG

PROGRAM : BACCALAUREUS TECHNOLOGIAE
CHEMICAL ENGINEERING

SUBJECT : **CHEMICAL ENGINEERING
TECHNOLOGY 4 (HEAT AND MASS)**

CODE : **WARC432**

DATE : WINTER EXAMINATION
2 JUNE 2014

DURATION : (X-PAPER) 08:30 - 11:30

WEIGHT : 40 : 60

TOTAL MARKS : 103

EXAMINER : DR R. HUBERTS 080207003

MODERATOR : PROF M.S. O'NYANGO 2242

NUMBER OF PAGES : 14

INSTRUCTIONS : ANSWER ALL QUESTIONS.
NON-PROGRAMMABLE CALCULATORS PERMITTED
(ONLY ONE PER CANDIDATE).

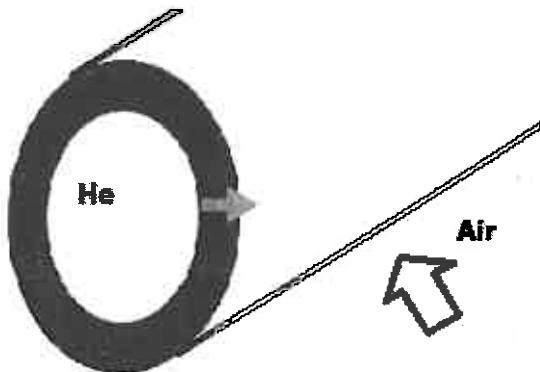
QUESTION 1

A 2m long black body metal wire of diameter 0.005m and at a temperature of $T_w = 400K$ runs through a grey body hard rubber pipe of outer and inner diameter 0.05m and 0.025m. A vacuum exists between the wire and the inner hard rubber pipe surface. The hard rubber pipe is coated on the outside with a layer of soft rubber, the thickness of which is given on Bb. Draw an annotated diagram of the system. If the temperature of the inner hard rubber area exposed to the vacuum is $T_{si} = 300K$, what is the temperature of the outer soft rubber surface, T_{ho} , at steady state in K? Ignore edge effects and use the thermal conductivity of rubber at 300K.

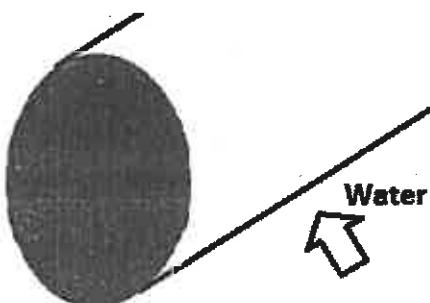
[33]**QUESTION 2**

- 2.1. Derive the mass diffusion equation (in the radial direction) for steady state one-dimensional diffusion through a stationary cylindrical medium and answer the question on Bb. (4)

Helium gas is transported outside a factory in Durban at 20°C through a silica pipe with outer diameter 0.05m and wall thickness of given on Bb. The absolute pressure in the pipe is maintained at 500kPa.



- 2.2. What is the rate of diffusion of the helium through the silica pipe wall in mol s^{-1} per meter of pipe length? (20)
- 2.3. If air blows over the pipe at a velocity given on Bb, what is the coefficient, h_m in ms^{-1} , for helium mass transfer from the outer surface of the pipe to the surrounding air? (16)

[40]**QUESTION 3**

Boiling water at 0.2ms^{-1} flows over a heated cylinder of outer diameter 0.05m.

- 3.1. What is the heat flux q'' in Wm^{-2} if it is maintained at 80% of the maximum possible? The diameter of the cylinder is given on Bb. Assume a pressure of 1 atm. (27)
- 3.2. Describe the boiling process. (3)

[30]

TOTAL MARKS = 103
FULL MARKS = 103

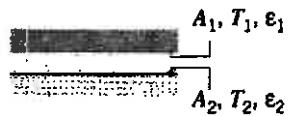
DATA SHEETS**Lengths, areas and volumes:**Circumference of a circle πd Area of a cylinder πdL Area of a circle $\pi d^2/4$ Surface area of a sphere πd^2 Volume of a sphere $\pi d^3/6$ **Radiation:**

| $F_{21}A_2 = F_{12}A_1$ | Surface Material | Emissivity Coefficient - ϵ - |
|-------------------------|------------------|--|
| | Rubber Nat Hard | 0.91 |
| | Rubber Nat Soft | 0.86 |

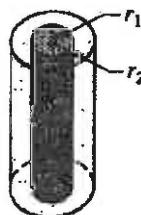
TABLE A.3 Continued**Other Materials (Continued)**

| Description/ Composition | Temperature (K) | Density, ρ (kg/m ³) | Thermal Conductivity, k (W/m · K) | Specific Heat, c , (J/kg · K) |
|-----------------------------|--------------------|--|---|---------------------------------------|
| Ice | 273 | 920 | 1.88 | 2040 |
| | 253 | — | 2.03 | 1945 |
| Leather (sole) | 300 | 998 | 0.159 | — |
| Paper | 300 | 930 | 0.180 | 1340 |
| Paraffin | 300 | 900 | 0.240 | 2890 |
| Rock | | | | |
| Granite, Barre | 300 | 2630 | 2.79 | 775 |
| Limestone, Salem | 300 | 2320 | 2.15 | 810 |
| Marble, Halston | 300 | 2680 | 2.80 | 830 |
| Quartzite, Sioux | 300 | 2640 | 5.38 | 1105 |
| Sandstone, Berea | 300 | 2150 | 2.90 | 745 |
| Rubber, vulcanized | | | | |
| Soft | 300 | 1100 | 0.13 | 2010 |
| Hard | 300 | 1190 | 0.16 | — |
| Sand | 300 | 1515 | 0.27 | 800 |
| Soil | 300 | 2050 | 0.52 | 1840 |
| Snow | 273 | 110 | 0.049 | — |
| | | 500 | 0.190 | — |
| Teflon | 300 | 2200 | 0.35 | — |
| | 400 | | 0.45 | — |
| Tissue, human | | | | |
| Skin | 300 | — | 0.37 | — |
| Fat layer (adipose) | 300 | — | 0.2 | — |
| Muscle | 300 | — | 0.41 | — |
| Wood, cross grain | | | | |
| Balsa | 300 | 140 | 0.055 | — |
| Cypress | 300 | 465 | 0.097 | — |
| Fir | 300 | 415 | 0.11 | 2720 |
| Oak | 300 | 545 | 0.17 | 2385 |
| Yellow pine | 300 | 640 | 0.15 | 2805 |
| White pine | 300 | 435 | 0.11 | — |
| Wood, radial | | | | |
| Oak | 300 | 545 | 0.19 | 2385 |
| Fir | 300 | 420 | 0.14 | 2720 |

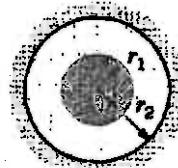
^aAdapted from References 1 and 8-13.

TABLE 13.3 Special Diffuse, Gray, Two-Surface Enclosures**Large (Infinite) Parallel Planes**

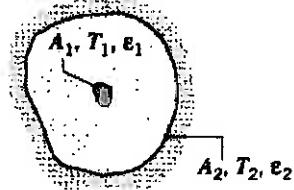
$$\frac{A_1}{A_2} = 1 \quad F_{12} = 1 \quad q_{12} = \frac{A\sigma(T_1^4 - T_2^4)}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1} \quad (13.24)$$

Long (Infinite) Concentric Cylinders

$$\frac{A_1}{A_2} = \frac{r_1}{r_2} \quad F_{12} = 1 \quad q_{12} = \frac{\sigma A_1 (T_1^4 - T_2^4)}{\frac{1}{\epsilon_1} + \frac{1 - \epsilon_2}{\epsilon_2} \left(\frac{r_1}{r_2} \right)^2} \quad (13.25)$$

Concentric Spheres

$$\frac{A_1}{A_2} = \frac{r_1^2}{r_2^2} \quad F_{12} = 1 \quad q_{12} = \frac{\sigma A_1 (T_1^4 - T_2^4)}{\frac{1}{\epsilon_1} + \frac{1 - \epsilon_2}{\epsilon_2} \left(\frac{r_1}{r_2} \right)^2} \quad (13.26)$$

Small Convex Object in a Large Cavity

$$\frac{A_1}{A_2} \approx 0 \quad F_{12} = 1 \quad q_{12} = \sigma A_1 \epsilon_1 (T_1^4 - T_2^4) \quad (13.27)$$

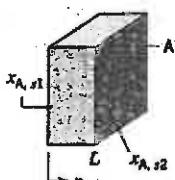
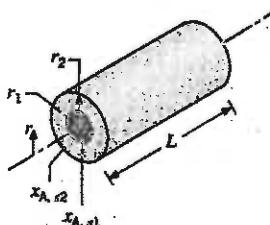
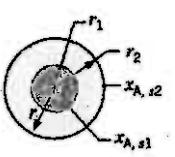
TABLE A.9 Henry's Constant for Selected Gases in Water at Moderate Pressure^a

| T (K) | $H = p_{A,i}/x_{A,i}$ (bars) | | | | | | | |
|----------|------------------------------|-----------------|------------------|-----------------|-----------------|-----------------|----------------|----------------|
| | NH ₃ | Cl ₂ | H ₂ S | SO ₂ | CO ₂ | CH ₄ | O ₂ | H ₂ |
| 273 | 21 | 265 | 260 | 165 | 710 | 22,880 | 25,500 | 58,000 |
| 280 | 23 | 365 | 335 | 210 | 960 | 27,800 | 30,500 | 61,500 |
| 290 | 26 | 480 | 450 | 315 | 1300 | 35,200 | 37,600 | 66,500 |
| 300 | 30 | 615 | 570 | 440 | 1730 | 42,800 | 45,700 | 71,600 |
| 310 | — | 755 | 700 | 600 | 2175 | 50,000 | 52,500 | 76,000 |
| 320 | — | 860 | 835 | 800 | 2650 | 56,300 | 56,800 | 78,600 |
| 323 | — | 890 | 870 | 850 | 2870 | 58,000 | 58,000 | 79,000 |

^aAdapted with permission from Reference 23.TABLE A.10 The Solubility of Selected Gases and Solids^a

| Gas | Solid | T | $S = C_{A,i}/p_{A,i}$ |
|-----------------|------------------|-----|-----------------------------|
| | | (K) | (kmol/m ³ · bar) |
| O ₂ | Rubber | 298 | 3.12×10^{-3} |
| N ₂ | Rubber | 298 | 1.56×10^{-3} |
| CO ₂ | Rubber | 298 | 40.15×10^{-3} |
| He | SiO ₂ | 293 | 0.45×10^{-3} |
| H ₂ | Ni | 358 | 9.01×10^{-3} |

^aAdapted with permission from Reference 22.TABLE 14.1 Summary of Species Diffusion Solutions for Stationary Media with Specified Surface Concentrations^a

| Geometry | Species Concentration Distribution, $x_A(x)$ or $x_A(r)$ | Species Diffusion Resistance, $R_{m,dif}$ |
|---|--|--|
|  | $x_A(x) = (x_{A,s2} - x_{A,s1}) \frac{x}{L} + x_{A,s1}$ | $R_{m,dif} = \frac{L}{D_{AB}A}^b$ |
|  | $x_A(r) = \frac{x_{A,s1} - x_{A,s2}}{\ln(r_1/r_2)} \ln\left(\frac{r}{r_2}\right) + x_{A,s2}$ | $R_{m,dif} = \frac{\ln(r_2/r_1)^c}{2\pi LD_{AB}}$ |
|  | $x_A(r) = \frac{x_{A,s1} - x_{A,s2}}{1/r_1 - 1/r_2} \left(\frac{1}{r} - \frac{1}{r_2} \right) + x_{A,s2}$ | $R_{m,dif} = \frac{1}{4\pi D_{AB}} \left(\frac{1}{r_1} - \frac{1}{r_2} \right)^c$ |

^aAssuming C and D_{AB} are constant.^b $N_{A,x} = (C_{A,s1} - C_{A,s2})/R_{m,dif}$.^c $N_{A,r} = (C_{A,s1} - C_{A,s2})/R_{m,dif}$.

TABLE A.8 Binary Diffusion Coefficients at One Atmosphere^{a,b}

| Substance A | Substance B | T (K) | D_{AB} (m ² /s) |
|-------------------------|------------------|----------|---------------------------------|
| Gases | | | |
| NH ₃ | Air | 298 | 0.28×10^{-4} |
| H ₂ O | Air | 298 | 0.26×10^{-4} |
| CO ₂ | Air | 298 | 0.16×10^{-4} |
| H ₂ | Air | 298 | 0.41×10^{-4} |
| O ₂ | Air | 298 | 0.21×10^{-4} |
| He | Air | 293 | 0.70×10^{-4} |
| Acetone | Air | 273 | 0.11×10^{-4} |
| Benzene | Air | 298 | 0.88×10^{-5} |
| Naphthalene | Air | 300 | 0.62×10^{-5} |
| Ar | N ₂ | 293 | 0.19×10^{-4} |
| H ₂ | O ₂ | 273 | 0.70×10^{-4} |
| H ₂ | N ₂ | 273 | 0.68×10^{-4} |
| N ₂ | CO ₂ | 273 | 0.35×10^{-4} |
| CO ₂ | N ₂ | 293 | 0.16×10^{-4} |
| CO ₂ | O ₂ | 273 | 0.14×10^{-4} |
| O ₂ | N ₂ | 273 | 0.18×10^{-4} |
| Dilute Solutions | | | |
| Caffeine | H ₂ O | 298 | 0.63×10^{-9} |
| Ethanol | H ₂ O | 298 | 0.12×10^{-4} |
| Glucose | H ₂ O | 298 | 0.69×10^{-9} |
| Glycerol | H ₂ O | 298 | 0.94×10^{-9} |
| Acetone | H ₂ O | 298 | 0.13×10^{-4} |
| CO ₂ | H ₂ O | 298 | 0.20×10^{-4} |
| O ₂ | H ₂ O | 298 | 0.24×10^{-4} |
| H ₂ | H ₂ O | 298 | 0.63×10^{-4} |
| N ₂ | H ₂ O | 298 | 0.26×10^{-4} |
| Solids | | | |
| O ₂ | Rubber | 298 | 0.21×10^{-9} |
| N ₂ | Rubber | 298 | 0.15×10^{-9} |
| CO ₂ | Rubber | 298 | 0.11×10^{-9} |
| He | SiO ₂ | 293 | 0.4×10^{-13} |
| H ₂ | Fe | 293 | 0.26×10^{-12} |
| Cd | Cu | 293 | 0.27×10^{-12} |
| Al | Cu | 293 | 0.13×10^{-12} |

^aAdapted with permission from References 20, 21, and 22.^bAssuming ideal gas behavior, the pressure and temperature dependence of the diffusion coefficient for a binary mixture of gases may be estimated from the relation

$$D_{AB} \propto P^{-1} T^{1/2}$$

TABLE 3.3 One-dimensional, steady-state solutions to the heat equation with no generation

| | Plane Wall | Cylindrical Wall ^a | Spherical Wall ^a |
|-------------------------------------|----------------------------------|---|---|
| Heat equation | $\frac{d^2T}{dx^2} = 0$ | $\frac{1}{r} \frac{d}{dr} \left(r \frac{dT}{dr} \right) = 0$ | $\frac{1}{r^2} \frac{d}{dr} \left(r^2 \frac{dT}{dr} \right) = 0$ |
| Temperature distribution | $T_{x,1} - \Delta T \frac{x}{L}$ | $T_{x,2} + \Delta T \frac{\ln(r/r_2)}{\ln(r_1/r_2)}$ | $T_{r,1} - \Delta T \left[\frac{1 - (r_1/r)}{1 - (r_1/r_2)} \right]$ |
| Heat flux (q'') | $k \frac{\Delta T}{L}$ | $\frac{k \Delta T}{r \ln(r_2/r_1)}$ | $\frac{k \Delta T}{r^2 [(1/r_1) - (1/r_2)]}$ |
| Heat rate (q) | $kA \frac{\Delta T}{L}$ | $\frac{2\pi L k \Delta T}{\ln(r_2/r_1)}$ | $\frac{4\pi k \Delta T}{(1/r_1) - (1/r_2)}$ |
| Thermal resistance ($R_{t,cond}$) | $\frac{L}{kA}$ | $\frac{\ln(r_2/r_1)}{2\pi L k}$ | $\frac{(1/r_1) - (1/r_2)}{4\pi k}$ |

^aThe critical radius of insulation is $r_c = k/h$ for the cylinder and $r_c = 2k/h$ for the sphere.

TABLE 8.4 Summary of convection correlations for flow in a circular tube^{a,b,c}

| Correlation | Conditions |
|--|--|
| $f = 64/Re_D$ | (8.19) Laminar, fully developed |
| $Nu_D = 4.36$ | (8.53) Laminar, fully developed, uniform q''_w , $Pr \geq 0.6$ |
| $Nu_D = 3.66$ | (8.55) Laminar, fully developed, uniform T_s , $Pr \geq 0.6$ |
| $Nu_D = 3.66$ + $\frac{0.0668(D/L)Re_D Pr}{1 + 0.04[(D/L)Re_D Pr]^{2/3}}$ | (8.56) Laminar, thermal entry length ($Pr \gg 1$ or an unheated starting length), uniform T_s |
| or | |
| $Nu_D = 1.86 \left(\frac{Re_D Pr}{L/D} \right)^{1/3} \left(\frac{\mu}{\mu_s} \right)^{0.14}$ | (8.57) Laminar, combined entry length $\{[Re_D Pr/(L/D)]^{1/2}(\mu/\mu_s)^{0.14}\} \geq 2$, uniform T_s , $0.48 < Pr < 16,700$, $0.0044 < (\mu/\mu_s) < 9.75$ |
| $f = 0.316 Re_D^{-1/4}$ | (8.20a) ^c Turbulent, fully developed, $Re_D \leq 2 \times 10^4$ |
| $f = 0.184 Re_D^{-1/5}$ | (8.20b) ^c Turbulent, fully developed, $Re_D \geq 2 \times 10^4$ |
| or | |
| $f = (0.790 \ln Re_D - 1.64)^{-2}$ | (8.21) ^c Turbulent, fully developed, $3000 \leq Re_D \leq 5 \times 10^6$ |
| $Nu_D = 0.023 Re_D^{4/5} Pr^n$ | (8.60) ^d Turbulent, fully developed, $0.6 \leq Pr \leq 160$, $Re_D \geq 10,000$, $(L/D) \approx 10$, $n = 0.4$ for $T_s > T_m$ and $n = 0.3$ for $T_s < T_m$ |
| or | |
| $Nu_D = 0.027 Re_D^{4/5} Pr^{1/3} \left(\frac{\mu}{\mu_s} \right)^{0.14}$ | (8.61) ^d Turbulent, fully developed, $0.7 \leq Pr \leq 16,700$, $Re_D \geq 10,000$, $L/D \geq 10$ |
| or | |
| $Nu_D = \frac{(f/8)(Re_D - 1000)Pr}{1 + 12.7(f/8)^{1/2}(Pr^{2/3} - 1)}$ | (8.63) ^d Turbulent, fully developed, $0.5 < Pr < 2000$, $3000 \leq Re_D \leq 5 \times 10^6$, $(L/D) \geq 10$ |
| $Nu_D = 4.82 + 0.0185(Re_D Pr)^{0.827}$ | (8.65) Liquid metals, turbulent, fully developed, uniform q''_w , $3.6 \times 10^3 < Re_D < 9.05 \times 10^3$, $10^2 < Pe_D < 10^4$ |
| $Nu_D = 5.0 + 0.025(Re_D Pr)^{0.8}$ | (8.66) Liquid metals, turbulent, fully developed, uniform T_s , $Pe_D > 100$ |

^aThe mass transfer correlations may be obtained by replacing Nu_D and Pr by Sh_D and Sc , respectively.^bProperties in Equations 8.53, 8.55, 8.60, 8.61, 8.63, 8.65, and 8.66 are based on T_m ; properties in Equations 8.19, 8.20, and 8.21 are based on $T_f = (T_s + T_m)/2$; properties in Equations 8.56 and 8.57 are based on $\bar{T}_m = (T_{m,i} + T_{m,o})/2$.^cEquations 8.20 and 8.21 pertain to smooth tubes. For rough tubes, Equation 8.63 should be used with the results of Figure 8.3.^dAs a first approximation, Equation 8.60, 8.61, or 8.63 may be used to evaluate the average Nusselt number \bar{Nu}_D over the entire tube length, if $(L/D) \geq 10$. The properties should then be evaluated at the average of the mean temperature, $\bar{T}_m = (T_{m,i} + T_{m,o})/2$.^eFor tubes of noncircular cross section, $Re_D = D_h u_w / \nu$, $D_h = 4A_e/P$, and $u_w = \dot{m}/\rho A_e$. Results for fully developed laminar flow are provided in Table 8.1. For turbulent flow, Equation 8.60 may be used as a first approximation.

TABLE 7.9 Summary of convection heat transfer correlations for external flow^{a, b}

| Correlation | | Geometry | Conditions |
|--|---------|------------------------------------|---|
| $\delta = 5x Re_x^{-1/2}$ | (7.19) | Flat plate | Laminar, T_f |
| $C_{J_x} = 0.664 Re_x^{-1/2}$ | (7.20) | Flat plate | Laminar, local, T_f |
| $Nu_x = 0.332 Re_x^{1/2} Pr^{1/3}$ | (7.23) | Flat plate | Laminar, local, T_f , $0.6 \leq Pr \leq 50$ |
| $\delta_c = \delta Pr^{-1/3}$ | (7.24) | Flat plate | Laminar, T_f |
| $\bar{C}_{J_x} = 1.328 Re_x^{-1/2}$ | (7.30) | Flat plate | Laminar, average, T_f |
| $\bar{Nu}_x = 0.664 Re_x^{1/2} Pr^{1/3}$ | (7.31) | Flat plate | Laminar, average, T_f , $0.6 \leq Pr \leq 50$ |
| $Nu_x = 0.565 Re_x^{1/2}$ | (7.33) | Flat plate | Laminar, local, T_f , $Pr \leq 0.05$ |
| $C_{J_x} = 0.0592 Re_x^{-1/5}$ | (7.35) | Flat plate | Turbulent, local, T_f , $Re_x \leq 10^3$ |
| $\delta = 0.37x Re_x^{-1/3}$ | (7.36) | Flat plate | Turbulent, local, T_f , $Re_x \leq 10^4$ |
| $Nu_x = 0.0296 Re_x^{4/5} Pr^{1/3}$ | (7.37) | Flat plate | Turbulent, local, T_f , $Re_x \leq 10^3$, $0.6 \leq Pr \leq 60$ |
| $\bar{C}_{J_x} = 0.074 Re_L^{-1/3} - 1742 Re_L^{-1}$ | (7.43) | Flat plate | Mixed, average, T_f , $Re_{x,c} = 5 \times 10^3$, $Re_L \leq 10^8$ |
| $\bar{Nu}_L = (0.037 Re_L^{4/5} - 871) Pr^{1/3}$ | (7.41) | Flat plate | Mixed, average, T_f , $Re_{x,c} = 5 \times 10^3$, $Re_L \leq 10^8$, $0.6 < Pr < 60$ |
| $Nu_D = C Re_D^n Pr^{1/3}$ (Table 7.2) | (7.55b) | Cylinder | Average, T_f , $0.4 < Re_D < 4 \times 10^5$, $Pr \geq 0.7$ |
| $Nu_D = C Re_D^n Pr^{0.36} (Pr/Pr_s)^{1/4}$ (Table 7.4) | (7.56) | Cylinder | Average, T_f , $1 < Re_D < 10^6$, $0.7 < Pr < 500$ |
| $Nu_D = 0.3 + [0.62 Re_D^{1/2} Pr^{1/3} \times [1 + (0.4/Pr)^{2/3}]^{-1/4} \times [1 + (Re_D/282,000)^{3/8}]^{1/5}]$ | (7.57) | Cylinder | Average, T_f , $Re_D Pr > 0.2$ |
| $\bar{Nu}_D = 2 + (0.4 Re_D^{1/2} + 0.06 Re_D^{2/3}) Pr^{0.4} \times (\mu/\mu_s)^{1/4}$ | (7.59) | Sphere | Average, T_f , $3.5 < Re_D < 7.6 \times 10^4$, $0.71 < Pr < 380$ |
| $\bar{Nu}_D = 2 + 0.6 Re_D^{1/2} Pr^{1/3}$ | (7.60) | Falling drop | Average, T_f |
| $\bar{Nu}_D = 1.13 C_1 Re_{D,\max}^n Pr^{1/3}$ (Tables 7.5, 7.6) | (7.63) | Tube bank ^c | Average, \bar{T} , $2000 < Re_{D,\max} < 4 \times 10^4$, $Pr \geq 0.7$ |
| $\bar{Nu}_D = C Re_{D,\max}^n Pr^{0.36} (Pr/Pr_s)^{1/4}$ (Tables 7.7, 7.8) | (7.67) | Tube bank ^c | Average, \bar{T} , $1000 < Re_D < 2 \times 10^6$, $0.7 < Pr < 500$ |
| Single round nozzle | (7.79) | Impinging jet | Average, T_f , $2000 < Re < 4 \times 10^5$, $2 < (H/D) < 12$, $2.5 < (r/D) < 7.5$ |
| Single slot nozzle | (7.82) | Impinging jet | Average, T_f , $3000 < Re < 9 \times 10^4$, $2 < (H/W) < 10$, $4 < (x/W) < 20$ |
| Array of round nozzles | (7.84) | Impinging jet | Average, T_f , $2000 < Re < 10^5$, $2 < (H/D) < 12$, $0.004 < A_r < 0.04$ |
| Array of slot nozzles | (7.87) | Impinging jet | Average, T_f , $1500 < Re < 4 \times 10^4$, $2 < (H/W) < 80$, $0.008 < A_r < 2.5 A_{r,s}$ |
| $\bar{e}_{j_H} = \bar{e}_{j_m} = 2.06 Re_D^{-0.575}$ | (7.91) | Packed bed of spheres ^c | Average, \bar{T} , $90 \leq Re_D \leq 4000$, $Pr \approx 0.7$ |

^aCorrelations in this table pertain to isothermal surfaces; for special cases involving an unheated starting length or a uniform surface heat flux, see Section 7.2.4.

^bWhen the heat and mass transfer analogy is applicable, the corresponding mass transfer correlations may be obtained by replacing Nu and Pr by Sh and Sc , respectively.

^cFor tube banks and packed beds, properties are evaluated at the average fluid temperature, $\bar{T} = (T_f + T_o)/2$, or the average film temperature, $\bar{T}_f = (T_f + \bar{T})/2$.

**TABLE 7.2 Constants of Equation
7.55b for the circular cylinder
in cross flow [14, 15]**

| Re_D | C | m |
|----------------|-------|-------|
| 0.4-4 | 0.989 | 0.330 |
| 4-40 | 0.911 | 0.385 |
| 40-4000 | 0.683 | 0.466 |
| 4000-40,000 | 0.193 | 0.618 |
| 40,000-400,000 | 0.027 | 0.805 |

**TABLE A.4 Thermophysical Properties
of Gases at Atmospheric Pressure^a**

| T (K) | ρ (kg/m ³) | c_p (kJ/kg · K) | $\mu \cdot 10^7$ (N · s/m ²) | $\nu \cdot 10^6$ (m ² /s) | $k \cdot 10^3$ (W/m · K) | $\alpha \cdot 10^6$ (m ² /s) | P_f |
|------------|--------------------------------|----------------------|---|---|-----------------------------|--|-------|
| Air | | | | | | | |
| 100 | 3.5562 | 1.032 | 71.1 | 2.00 | 9.34 | 2.54 | 0.786 |
| 150 | 2.3364 | 1.012 | 103.4 | 4.426 | 13.8 | 5.84 | 0.758 |
| 200 | 1.7458 | 1.007 | 132.5 | 7.590 | 18.1 | 10.3 | 0.737 |
| 250 | 1.3947 | 1.006 | 159.6 | 11.44 | 22.3 | 15.9 | 0.720 |
| 300 | 1.1614 | 1.007 | 184.6 | 15.89 | 26.3 | 22.5 | 0.707 |
| 350 | 0.9950 | 1.009 | 208.2 | 20.92 | 30.0 | 29.9 | 0.700 |
| 400 | 0.8711 | 1.014 | 230.1 | 26.41 | 33.8 | 38.3 | 0.690 |
| 450 | 0.7740 | 1.021 | 250.7 | 32.39 | 37.3 | 47.2 | 0.686 |
| 500 | 0.6964 | 1.030 | 270.1 | 38.79 | 40.7 | 56.7 | 0.684 |
| 550 | 0.6329 | 1.040 | 288.4 | 45.57 | 43.9 | 66.7 | 0.683 |
| 600 | 0.5804 | 1.051 | 305.8 | 52.69 | 46.9 | 76.9 | 0.685 |
| 650 | 0.5356 | 1.063 | 322.5 | 60.21 | 49.7 | 87.3 | 0.690 |
| 700 | 0.4975 | 1.075 | 338.8 | 68.10 | 52.4 | 98.0 | 0.695 |
| 750 | 0.4643 | 1.087 | 354.6 | 76.37 | 54.9 | 109 | 0.702 |
| 800 | 0.4354 | 1.099 | 369.8 | 84.93 | 57.3 | 120 | 0.709 |
| 850 | 0.4097 | 1.110 | 384.3 | 93.80 | 59.6 | 131 | 0.716 |
| 900 | 0.3868 | 1.121 | 398.1 | 102.9 | 62.0 | 143 | 0.720 |
| 950 | 0.3666 | 1.131 | 411.3 | 112.2 | 64.3 | 155 | 0.723 |
| 1000 | 0.3482 | 1.141 | 424.4 | 121.9 | 66.7 | 168 | 0.726 |
| 1100 | 0.3166 | 1.159 | 449.0 | 141.8 | 71.5 | 195 | 0.728 |
| 1200 | 0.2902 | 1.175 | 473.0 | 162.9 | 76.3 | 224 | 0.728 |
| 1300 | 0.2679 | 1.189 | 496.0 | 185.1 | 82 | 238 | 0.719 |
| 1400 | 0.2488 | 1.207 | 530 | 213 | 91 | 303 | 0.703 |
| 1500 | 0.2322 | 1.230 | 557 | 240 | 100 | 350 | 0.685 |
| 1600 | 0.2177 | 1.248 | 584 | 268 | 106 | 390 | 0.688 |

TABLE A.6 Thermophysical Properties of Saturated Water^a

| Temper- ature, T (K) | Pressure, P (bars) ^b | Specific Volume (m ³ /kg) | | | | Heat of Vapor- ization, h_f° (kJ/kg) | | | | Specific Heat (kJ/kg · K) | | | | Thermal Conductivity (W/m · K) | | Prandtl Number | Surface Tension, $\sigma \cdot 10^3$ (N/m) | Expansion Coeffi- cient, $\beta \cdot 10^6$ (K ⁻¹) | Temper- ature, T (K) |
|------------------------------|--------------------------------------|--|-------|-----------|-----------|---|--------------------|------------------|------------------|---------------------------------|--------|-------|------|--------------------------------------|--------|-------------------|---|--|------------------------------|
| | | v_f · 10 ³ | v_t | $c_{p,t}$ | $c_{p,s}$ | $\mu_f \cdot 10^6$ | $\mu_t \cdot 10^6$ | $k_f \cdot 10^3$ | $k_t \cdot 10^3$ | Pr_f | Pr_t | | | | | | | | |
| 273.15 | 0.006111 | 1.000 | 206.3 | 2502 | 4.217 | 1.854 | 1750 | 8.02 | 569 | 18.2 | 12.99 | 0.815 | 75.5 | -68.05 | 273.15 | | | | |
| 275 | 0.00697 | 1.000 | 181.7 | 2497 | 4.211 | 1.855 | 1652 | 8.09 | 574 | 18.3 | 12.22 | 0.817 | 75.3 | -32.74 | 275 | | | | |
| 280 | 0.00990 | 1.000 | 130.4 | 2485 | 4.198 | 1.858 | 1422 | 8.29 | 582 | 18.6 | 10.26 | 0.825 | 74.8 | 46.04 | 280 | | | | |
| 285 | 0.01387 | 1.000 | 99.4 | 2473 | 4.189 | 1.861 | 1225 | 8.49 | 590 | 18.9 | 8.81 | 0.833 | 74.3 | 14.1 | 285 | | | | |
| 290 | 0.01917 | 1.001 | 69.7 | 2461 | 4.184 | 1.864 | 1080 | 8.69 | 598 | 19.3 | 7.56 | 0.841 | 73.7 | 174.0 | 290 | | | | |
| 295 | 0.02617 | 1.002 | 51.94 | 2449 | 4.181 | 1.868 | 959 | 8.89 | 606 | 19.5 | 6.62 | 0.849 | 72.7 | 227.5 | 295 | | | | |
| 300 | 0.03531 | 1.003 | 39.13 | 2438 | 4.179 | 1.872 | 855 | 9.09 | 613 | 19.6 | 5.83 | 0.857 | 71.7 | 276.1 | 300 | | | | |
| 305 | 0.04712 | 1.005 | 29.74 | 2426 | 4.178 | 1.877 | 769 | 9.29 | 620 | 20.1 | 5.20 | 0.865 | 70.9 | 320.6 | 305 | | | | |
| 310 | 0.06221 | 1.007 | 22.93 | 2414 | 4.178 | 1.882 | 695 | 9.49 | 628 | 20.4 | 4.62 | 0.873 | 70.0 | 361.9 | 310 | | | | |
| 315 | 0.08132 | 1.009 | 17.82 | 2402 | 4.179 | 1.888 | 631 | 9.69 | 634 | 20.7 | 4.16 | 0.883 | 69.2 | 400.4 | 315 | | | | |
| 320 | 0.1053 | 1.011 | 13.98 | 2390 | 4.180 | 1.895 | 577 | 9.89 | 640 | 21.0 | 3.77 | 0.894 | 68.3 | 436.7 | 320 | | | | |
| 325 | 0.1351 | 1.013 | 11.06 | 2378 | 4.182 | 1.903 | 528 | 10.09 | 645 | 21.3 | 3.42 | 0.901 | 67.5 | 471.2 | 325 | | | | |
| 330 | 0.1719 | 1.016 | 8.82 | 2366 | 4.184 | 1.911 | 489 | 10.29 | 650 | 21.7 | 3.15 | 0.908 | 66.6 | 504.0 | 330 | | | | |
| 335 | 0.2167 | 1.018 | 7.09 | 2354 | 4.186 | 1.920 | 453 | 10.49 | 656 | 22.0 | 2.88 | 0.916 | 65.8 | 535.5 | 335 | | | | |
| 340 | 0.2713 | 1.021 | 5.74 | 2342 | 4.188 | 1.930 | 420 | 10.69 | 660 | 22.3 | 2.66 | 0.925 | 64.9 | 566.0 | 340 | | | | |
| 345 | 0.3372 | 1.024 | 4.683 | 2329 | 4.191 | 1.941 | 389 | 10.89 | 668 | 22.6 | 2.45 | 0.933 | 64.1 | 595.4 | 345 | | | | |
| 350 | 0.4163 | 1.027 | 3.846 | 2317 | 4.195 | 1.954 | 365 | 11.09 | 668 | 23.0 | 2.29 | 0.942 | 63.2 | 624.2 | 350 | | | | |
| 355 | 0.5100 | 1.030 | 3.180 | 2304 | 4.199 | 1.968 | 343 | 11.29 | 671 | 23.3 | 2.14 | 0.951 | 62.3 | 652.3 | 355 | | | | |
| 360 | 0.6209 | 1.034 | 2.645 | 2291 | 4.203 | 1.983 | 324 | 11.49 | 674 | 23.7 | 2.02 | 0.960 | 61.4 | 697.9 | 360 | | | | |
| 365 | 0.7514 | 1.038 | 2.212 | 2278 | 4.209 | 1.999 | 306 | 11.69 | 677 | 24.1 | 1.91 | 0.969 | 60.5 | 707.1 | 365 | | | | |
| 370 | 0.9040 | 1.041 | 1.861 | 2265 | 4.214 | 2.017 | 289 | 11.89 | 679 | 24.5 | 1.80 | 0.978 | 59.5 | 728.7 | 370 | | | | |
| 373.15 | 1.0133 | 1.044 | 1.679 | 2257 | 4.217 | 2.029 | 279 | 12.02 | 680 | 24.8 | 1.76 | 0.984 | 58.9 | 750.1 | 373.15 | | | | |
| 375 | 1.0815 | 1.045 | 1.574 | 2252 | 4.220 | 2.036 | 274 | 12.09 | 681 | 24.9 | 1.70 | 0.987 | 58.6 | 761 | 375 | | | | |
| 380 | 1.2869 | 1.049 | 1.337 | 2239 | 4.226 | 2.057 | 260 | 12.29 | 683 | 25.4 | 1.61 | 0.999 | 57.6 | 788 | 380 | | | | |
| 385 | 1.5233 | 1.053 | 1.142 | 2225 | 4.232 | 2.080 | 248 | 12.49 | 685 | 25.8 | 1.53 | 1.004 | 56.6 | 814 | 385 | | | | |

TABLE 6.2 Selected dimensionless groups of heat and mass transfer

| Group | Definition | Interpretation |
|--|---|---|
| Biot number (Bi) | $\frac{hL}{k_s}$ | Ratio of the internal thermal resistance of a solid to the boundary layer thermal resistance. |
| Mass transfer Biot number (Bi_m) | $\frac{h_m L}{D_{AB}}$ | Ratio of the internal species transfer resistance to the boundary layer species transfer resistance. |
| Bond number (Bo) | $\frac{g(\rho_i - \rho_v)L^2}{\sigma}$ | Ratio of gravitational and surface tension forces. |
| Coefficient of friction (C_f) | $\frac{\tau_s}{\rho V^2/2}$ | Dimensionless surface shear stress. |
| Eckert number (Ec) | $\frac{V^2}{c_p(T_s - T_\infty)}$ | Kinetic energy of the flow relative to the boundary layer enthalpy difference. |
| Fourier number (Fo) | $\frac{\alpha t}{L^2}$ | Ratio of the heat conduction rate to the rate of thermal energy storage in a solid. Dimensionless time. |
| Mass transfer Fourier number (Fo_m) | $\frac{D_{AB}t}{L^2}$ | Ratio of the species diffusion rate to the rate of species storage. Dimensionless time. |
| Friction factor (f) | $\frac{\Delta p}{(L/D)(\rho u_m^2/2)}$ | Dimensionless pressure drop for internal flow. |
| Grashof number (Gr_L) | $\frac{g\beta(T_s - T_\infty)L^3}{\nu^2}$ | Ratio of buoyancy to viscous forces. |
| Colburn j factor (j_H) | $St Pr^{2/3}$ | Dimensionless heat transfer coefficient. |
| Colburn j factor (j_m) | $St_m Sc^{2/3}$ | Dimensionless mass transfer coefficient. |
| Jakob number (Ja) | $\frac{c_p(T_s - T_{sat})}{h_f}$ | Ratio of sensible to latent energy absorbed during liquid-vapor phase change. |
| Lewis number (Le) | $\frac{\alpha}{D_{AB}}$ | Ratio of the thermal and mass diffusivities. |
| Nusselt number (Nu_L) | $\frac{hL}{k_f}$ | Dimensionless temperature gradient at the surface. |
| Peclet number (Pe_L) | $\frac{VL}{\alpha} = Re_L Pr$ | Dimensionless independent heat transfer parameter. |
| Prandtl number (Pr) | $\frac{c_p\mu}{k} = \frac{\nu}{\alpha}$ | Ratio of the momentum and thermal diffusivities. |
| Reynolds number (Re_L) | $\frac{VL}{\nu}$ | Ratio of the inertia and viscous forces. |
| Schmidt number (Sc) | $\frac{\nu}{D_{AB}}$ | Ratio of the momentum and mass diffusivities. |
| Sherwood number (Sh_L) | $\frac{h_m L}{D_{AB}}$ | Dimensionless concentration gradient at the surface. |
| Stanton number (St) | $\frac{h}{\rho V c_p} = \frac{Nu_L}{Re_L Pr}$ | Modified Nusselt number. |
| Mass transfer Stanton number (St_m) | $\frac{h_m}{V} = \frac{Sh_L}{Re_L Sc}$ | Modified Sherwood number. |
| Weber number (We) | $\frac{\rho V^2 L}{\sigma}$ | Ratio of inertia to surface tension forces. |

Heat transfer at a boiling surface:

$$q_s'' = h(T_s - T_{sat}) = h\Delta T_e \dots\dots 10.3$$

Nucleate boiling correlation:

$$q_s'' = \mu_i h_{fg} \left[\frac{g(\rho_l - \rho_v)}{\sigma} \right]^{1/2} \left(\frac{c_{p,l} \Delta T_e}{C_{s,f} h_{fg} \text{Pr}_l^n} \right)^3 \dots\dots 10.5$$

Critical heat flux (Kutateladze and Zuber):

$$q_{max}'' = 0.149 h_{fg} \rho_v \left[\frac{\sigma g(\rho_l - \rho_v)}{\rho_v^2} \right]^{1/4} \dots\dots 10.7$$

TABLE 10.1 Values of $C_{s,f}$ for various surface-fluid combinations [5-7]

| Surface-Fluid Combination | $C_{s,f}$ | n |
|---------------------------|-----------|-----|
| Water-copper | | |
| Scored | 0.0068 | 1.0 |
| Polished | 0.0130 | 1.0 |
| Water-stainless steel | | |
| Chemically etched | 0.0130 | 1.0 |
| Mechanically polished | 0.0130 | 1.0 |
| Ground and polished | 0.0060 | 1.0 |
| Water-brass | 0.0060 | 1.0 |
| Water-nickel | 0.006 | 1.0 |
| Water-platinum | 0.0130 | 1.0 |
| <i>n</i> -Pentane-copper | | |
| Polished | 0.0154 | 1.7 |
| Lapped | 0.0049 | 1.7 |
| Benzene-chromium | 0.0101 | 1.7 |
| Ethyl alcohol-chromium | 0.0027 | 1.7 |

Minimum heat flux (Zuber) (moderate pressures):

$$q_{min}'' = 0.09 \rho_v h_{fg} \left[\frac{g \sigma (\rho_l - \rho_v)}{(\rho_l + \rho_v)^2} \right]^{1/4} \dots\dots 10.8$$

Film pool boiling for $T_s < 300^\circ\text{C}$ (radiation component low):

$$\overline{Nu}_D = \frac{\bar{h}_{conv} D}{k_v} = C \left[\frac{g \sigma (\rho_l - \rho_v) h'_{fg} D^3}{\nu_v k_v (T_s - T_{sat})} \right]^{1/4} \dots\dots 10.9$$

$C = 0.62$ for horizontal cylinders and $C = 0.67$ for spheres.

$$h_{fg} = h_{fg} + 0.80 c_{p,v} (T_s - T_{sat})$$

Film pool boiling for $T_s > 300^\circ\text{C}$:

$$\bar{h}^{1/3} = \bar{h}_{conv}^{1/3} + \bar{h}_{rad} \cdot \bar{h}^{1/3}$$

if $\bar{h}_{rad} \prec \bar{h}_{conv}$;

$$\bar{h} = \bar{h}_{conv} + \frac{3}{4} \bar{h}_{rad} \dots\dots 10.10$$

$$\text{where } \bar{h}_{rad} = \frac{\varepsilon \sigma (T_s^4 - T_{sat}^4)}{T_s - T_{sat}}$$

External forced convection boiling of a cylinder in cross flow:...10.12 (High:a Low:b)

$$\text{High velocity: } \frac{q''_{\max}}{\rho_v h_{fg} V} = \frac{1}{\pi} \left[1 + \left(\frac{4}{We_D} \right)^{\frac{1}{3}} \right]$$

$$\text{Low velocity: } \frac{q''_{\max}}{\rho_v h_{fg} V} = \frac{\left(\rho_l / \rho_v \right)^{\frac{3}{4}}}{169\pi} + \frac{\left(\rho_l / \rho_v \right)^{\frac{1}{2}}}{19.2\pi We_D^{\frac{1}{3}}}$$

$$We_D = \frac{\rho V^2 D}{\sigma}$$

$$\text{If } \frac{q''_{\max}}{\rho_v h_{fg} V} \leq \left[\frac{0.275}{\pi} \right] \left[\frac{\rho l}{\rho v} \right]^{\frac{1}{2}} + 1 \text{ then the velocity is high, otherwise it is low}$$

CONDENSATION:

Nusselt laminar film condensation correlation:

$$\bar{N}_u_L = \frac{\bar{h}_L L}{k_L} = 0.943 \left[\frac{\rho_L g (\rho_L - \rho_v) h'_{fg} L^3}{\mu_L k_L (T_{sat} - T_s)} \right]^{1/4} \dots\dots 10.31$$

Modified latent heat of formation term for condensation (Rohsenow):

$$h'_{fg} = h_{fg} (1 + 0.68Ja) \dots\dots 10.26$$

Total heat transfer to the surface:

$$q = \bar{h}_L A (T_{sat} - T_s) \dots\dots 10.32$$

Total condensation rate:

$$\dot{m} = \frac{q}{h'_{fg}} = \frac{\bar{h}_L A (T_{sat} - T_s)}{h'_{fg}} \dots\dots 10.33$$

Reynolds number for condensation

$$Re_\delta = \frac{4\dot{m}}{\mu_L b} = \frac{4\rho_l u_m \delta}{\mu_L} \dots\dots 10.35$$

Condensate mass flowrate:

$$m(x) = \rho_l u_m b \delta(x)$$

$$m(x) = b \frac{g \rho_l (\rho_l - \rho_v) \delta(x)^3}{3 \mu_l} \dots\dots 10.19$$

u_m = mean velocity, δ = thickness, b = breadth of plate

Thickness of condensate:

$$\delta(x) = \left[\frac{4k_l \mu_l (T_{sat} - T_s)x}{g \rho_l (\rho_l - \rho_v) h_{fg}} \right]^{1/4}$$

Re_s ≤ 30 for wave-free laminar flow:

$$\frac{\bar{h}_L (v_l^2 / g)^{1/3}}{k_l} = 1.47 Re_\delta^{-1/3} \dots 10.37$$

30 ≤ Re_s ≤ 1800 for wavy laminar flow:

$$V_l = \frac{\mu_l}{\rho_l}$$

$$\frac{\bar{h}_L (v_l^2 / g)^{1/3}}{k_l} = \frac{Re_\delta}{1.08 Re_\delta^{1.22} - 5.2}$$

Re_s > 1800 for turbulent flow:

$$\frac{\bar{h}_L (v_l^2 / g)^{1/3}}{k_l} = \frac{Re_\delta}{8750 + 58 Pr^{-0.5} (Re_\delta^{0.75} - 253)}$$

TABLE 1.5 Summary of heat transfer processes

| Mode | Mechanism(s) | Rate Equation | Equation Number | Transport Property or Coefficient |
|------------|--|---|-----------------|---|
| Conduction | Diffusion of energy due to random molecular motion | $q''_x (\text{W/m}^2) = -k \frac{dT}{dx}$ | (1.1) | $k (\text{W/m} \cdot \text{K})$ |
| Convection | Diffusion of energy due to random molecular motion plus energy transfer due to bulk motion (advection) | $q'' (\text{W/m}^2) = h(T_s - T_w)$ | (1.3a) | $h (\text{W/m}^2 \cdot \text{K})$ |
| Radiation | Energy transfer by electromagnetic waves | $q'' (\text{W/m}^2) = \epsilon \sigma (T_s^4 - T_{\infty}^4)$ or $q (\text{W}) = h_r (T_s - T_{\infty})$ | (1.7) (1.8) | ϵ $h_r (\text{W/m}^2 \cdot \text{K})$ |

TABLE 10.1 Values of C_{ef} for various surface-fluid combinations [5-7]

| Surface-Fluid Combination | C_{ef} | n |
|---------------------------|----------|-----|
| Water-copper | | |
| Scored | 0.0068 | 1.0 |
| Polished | 0.0130 | 1.0 |
| Water-stainless steel | | |
| Chemically etched | 0.0130 | 1.0 |
| Mechanically polished | 0.0130 | 1.0 |
| Ground and polished | 0.0060 | 1.0 |
| Water-brass | 0.0060 | 1.0 |
| Water-nickel | 0.006 | 1.0 |
| Water-platinum | 0.0130 | 1.0 |
| <i>n</i> -Pentane-copper | | |
| Polished | 0.0154 | 1.7 |
| Lapped | 0.0049 | 1.7 |
| Benzene-chromium | 0.0101 | 1.7 |
| Ethyl alcohol-chromium | 0.0027 | 1.7 |