



**PROGRAM**

NATIONAL DIPLOMA

*EXTRACTION METALLURGY*

**SUBJECT**

METALLURGICAL THERMODYNAMICS 2

**CODE**

**THM 21-2 (Extraction Metallurgy)**

**Main Examination**

**DATE**

13 JUNE 2015

**TIME**

08:30

**WEIGHT**

40:60

**TOTAL MARKS**

64

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**ASSESSOR**

N. TSHIONGO-MAKGWE

**MODERATOR**

MARCEL KALEMBA

**NUMBER OF PAGES**

3 PAGES AND A 3-PAGE ANNEXURE

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**INSTRUCTIONS**

First read carefully through all questions; only then

- Answer all questions in any sequence – but
- Please start answering each question on a new page
- You must clearly demonstrate how you arrived at a given answer, results alone are insufficient
- Finally: Check whether an answer makes sense; is the result likely?
- Calculators are permitted, brains also, but nothing else because
- All data required for calculations are provided in the Annexure

## Question 1

[10]

### General

- 1.1 Briefly describe the zeroth law of thermodynamics (2)
- 1.2 Give the formula for the standard free energy change and describe in words the condition when a reaction is feasible. (2)
- 1.3 The free energy is composed of two terms that reflect two fundamental forces of nature; shortly describe in words which two fundamental forces are operating and to which terms of the free energy they relate. (2)
- 1.4 Are exothermic reactions always feasible? (2)
- 1.5 If gases are involved, what can you generally state about the entropy change of the reaction? Give an example! (2)

## Question 2

[8]

### Heat

- 2.1 You have to design a plant that is able to evaporate 55 t/h of water to produce steam at 300°C; the feed water is at 25°C, the steam at 1 atm. How much power do you need? (8)

Assume no losses; use mean heat capacities

## Question 3

[12]

### Equilibrium constant

Consider the reduction of metal oxides to the respective metals by hydrogen gas:

- 3.1 Formulate the reaction and define the equilibrium constant K for the reduction of a metal oxide of the composition MO (4)
- 3.2 Calculate and compare the equilibrium constants at 1000°C for manganese oxide ( $MnO$ ) and cupric oxide ( $CuO$ ) (6)
- 3.3 Based on the values of the equilibrium constants, what qualitative statement can you make as regards the usefulness of this reaction for the industrial production of the two metals? (2)

**Question 4****[12]****Gibbs**

In an industrial process, the production of MnO from Mn-dioxide, pyrolusite, at 750°C is required.

- 4.1 Formulate the reaction in which pyrolusite is reduced to MnO with coke and calculate the free energy change for this reduction process at the given temperature. (4)
- 4.2 Formulate the reaction in which pyrolusite forms MnO by dissociation and calculate the free energy change for this process at the given temperature. (4)
- 4.3 Express in words which of the two reactions you would choose and why? (4)

**Question 5****[22]****Processes**

Consider the reduction of magnetite with coke to form iron

- 5.1 Formulate the overall reaction (2)
- 5.2 How much coke (in t) would you have to add for the reduction of 1 t of magnetite?  
Assume stoichiometric requirements and coke to be pure carbon (2)
- 5.3 Estimate the volume of gas (in m<sup>3</sup>) that is produced by the reduction of 1 t of magnetite  
Assume stoichiometric requirements (3)
- 5.4 If you were to completely combust the produced gas, how much energy could you recover? (4)
- 5.5 Determine whether the reduction of magnetite is an exo- or endo-thermic process (3)
- 5.6 As regards the change of entropy for the reaction, what could you predict?  
Do not calculate yet but give a reason for your answer (1)
- 5.7 Demonstrate that the reaction is not feasible at standard conditions (3)
- 5.8 Estimate the temperature at which the reaction becomes feasible. (4)

**The end**

METALLURGICAL THERMODYNAMICS



Name	Substance			Enthalpy $H^\circ_{298}$ J/mol	Entropy $S^\circ_{298}$ J/(mol K)	Heat Capacity		
	Formula	State	Mol Mass g/mol			Temp Range K	a	b
Manganese	Mn	sol	54.9		32.0	298 - 1517	20.7	18.7
	Mnliq	liq		12 100	40.0	1517 - 2332		28.6
Manganese carbonate	MnCO <sub>3</sub>	sol	114.9	- 894 100	85.8	298 - 700	58.1	85.4
Manganese oxide	MnO	sol	70.9	- 385 221	59.7	298 - 1500	42.9	10.9
Mn-dioxide, <i>pyrolusite</i>	MnO <sub>2</sub>	sol	86.9	- 520 029	53.0	298 - 523	35.1	66.0
Mercury (quicksilver)	Hg	liq	200.6		75.9	298 - 630	28.4	-2.1
	Hggas	gas		61 291	174.8	630 - 3000		27.4
Mercury oxide, <i>red mercury</i>	HgO	sol	216.6	- 90 789	70.3	298 - 800	36.6	27.6
Mercury sulfide, <i>cinnabar</i>	HgS	sol	232.7	- 53 346	82.4	298 - 1098	43.9	15.4
	HgSgas	gas		127 194	254.2	1098 - 2000	36.6	0.5
Methane	CH <sub>4</sub>	gas	16.0	- 74 873	186.2	298 - 1000	19.3	54.8
Nickel	Ni	sol	58.7		29.9	298 - 1728	19.1	23.5
	Ni liq	liq		17 472	40.0	1728 - 3187		43.1
Nickel carbonate	NiCO <sub>3</sub>	sol	118.7	- 694 544	86.2	298 - 700	67.1	68.1
Nickel carbonyl	Ni(CO) <sub>4</sub>	gas	170.8	- 602 910	410.6	298 - 2000	152.7	29.1
Nickel oxide	NiO	sol	74.7	- 239 701	38.0	298 - 2228	20.9	36.5
Nickel sulfide, <i>millerite</i>	NiS	sol	90.8	- 87 864	53.0	298 - 1249	36.5	27.4
Ni-sulfide, <i>heazlewoodite</i>	Ni <sub>3</sub> S <sub>2</sub>	sol	208.1	- 216 313	133.9	298 - 1062		150
Nitrogen	N <sub>2</sub>	gas	28.0		191.6	298 - 1600	28.0	3.1
Oxygen	O <sub>2</sub>	gas	32.0		205.1	298 - 5000	31.9	2.5
Palladium	Pd	sol	106.4		37.8	298 - 1825	24.2	6.4
Palladium oxide	PdO	sol	122.4	- 115 478	38.9	298 - 1200	21.0	34.7
Platinum	Pt	sol	195.1		41.6	298 - 2045	24.3	5.4
	Pt liq	liq		19 665	51.3	2045 - 4096		34.7
Silicon	Si	sol	28.1		18.8	298 - 1685	19.7	6.1
	Si liq	liq		50 208	48.6	1685 - 3504		25.5
Silica	SiO <sub>2</sub>	sol	60.1	- 910 857	41.5	298 - 1996	29.2	56.8
	SiO <sub>2</sub> liq	liq		- 901 292	49.3	1996 - 3000		65.0
Silver	Ag	sol	107.9		42.7	298 - 1234	24.3	2.5
	Ag liq	liq		11 297	51.8	1234 - 2433		28.0
Slag, calcium <i>ortho silicate</i>	Ca <sub>2</sub> SiO <sub>4</sub>	sol	172.2	- 2 315 216	120.8	298 - 2403	145.9	40.8
	Ca <sub>2</sub> SiO <sub>4</sub> liq	liq		- 2 244 000	170.8	2403 - 2800		164
Slag, <i>fayalite</i>	Fe <sub>2</sub> SiO <sub>4</sub>	sol	203.8	- 1 479 902	145.2	298 - 1490	125.5	60.6
	Fe <sub>2</sub> SiO <sub>4</sub> liq	liq		- 1 387 728	61.9	1490 - 1700		153
Sulfur	S	sol	32.1		32.1	298 - 388	16.8	20.1
	S liq	liq		2 122	37.6	388 - 882	30.0	6.8
	S <sub>2</sub> gas	gas		128 599	228.2	882 - 5000	35.2	1.9
Sulfur dioxide	SO <sub>2</sub>	gas	64.1	- 296 813	248.2	50 - 500	30.8	31.9
	SO <sub>2</sub> hi	hi				500 - 5000	52.5	3.0
Tin	grey	Sngt	sol	- 2 092	44.1	298 - 398	25.8	25.8
white	Sn	sol	150.7		51.2	298 - 505	21.6	18.1
	Sn liq	liq		7 029	65.1	505 - 800		28.8
Tin dioxide, <i>cassiterite</i>	SnO <sub>2</sub>	sol	150.7	- 577 631	49.0	298 - 1903	58.7	18.2
	Ice	sol		- 279 850		< 273		78.8
Water	H <sub>2</sub> O	liq	18.0	- 285 830	69.9	298 - 373	73.0	7.9
	H <sub>2</sub> O gas	gas		- 241 827	188.8	373 - 1600	30.1	75.5
Zinc	Zn	sol	65.4		41.6	298 - 693	22.2	10.5
	Zn liq	liq		7 322	52.2	693 - 1 180		27.1
	Zn gas	gas		130 415	161.0	1 180 - 2 000		31.4
Zinc carbonate, <i>smithsonite</i>	ZnCO <sub>3</sub>	sol	125.4	- 812 780	82.4	298 - 500	38.9	138.1
Zinc oxide, <i>zinclite</i>	ZnO	sol	81.4	- 350 460	43.6	298 - 2248	41.4	9.5
Zinc sulfide, <i>sphalerite</i>	ZnS	sol	97.4	- 201 669	57.7	298 - 1293	44.7	53.3
							10.6	52.8

## METALLURGICAL THERMODYNAMICS



Substance Name	Formula	State	Mol Mass g/mol	Enthalpy $H^\circ_{298}$ J/mol	Entropy $S^\circ_{298}$ J/(mol K)	Temp Range K	Heat Capacity				
							a	b	$C_{p,m}$ $\times 10^3$	J/(mol K)	
Acetylene	$C_2H_2$	gas	26.0	226 731	201.0	298 - 3000	50.2	14.2	72.9		
Aluminium	Al	sol	27.0		28.3	298 - 933	19.8	14.4	28.5		
	Alliq	liq		10 711	39.8	933 - 2790			31.7		
Aluminium oxide, alumina	$Al_2O_3$	sol	102.0	-1 675 274	50.9	298 - 800	58.2	83.5	101		
	$Al_2O_3$ hi				800 - 2327	112.2	12.7	133			
Cadmium	Cd	sol	112.4		51.8	298 - 594	22.3	12.2	27.4		
	Cdliq	liq		6 192	62.2	594 - 1040			29.7		
	Cdgas	gas		111 796	167.7	1040 - 1500			20.8		
Cadmium carbonate	$CdCO_3$	sol	172.4	-751 865	92.5	298 - 600	43.1	131.8	99.9		
Cadmium oxide	CdO	sol	128.4	-258 990	54.8	298 - 1500	43.0	9.7	51.5		
Calcium oxide, lime	CaO	sol	56.1	-635 089	38.1	298 - 3200	46.0	6.0	56.0		
Ca-carbonate, calcite	$CaCO_3$	sol	100.1	-1 206 921	92.9	298 - 1200	74.8	50.2	110		
Carbon, graphite	C	sol	12.0		5.7	298 - 1100	4.9	17.2	16.3		
Carbon monoxide	CO	gas	28.0	+110 541	197.7	298 - 5000	30.9	1.9	33.0		
Carbon dioxide	$CO_2$	gas	44.0	-393 505	213.8	298 - 500	26.0	37.2	35.6		
	$CO_2$ hi				500 - 5000	51.9	3.0	60.1			
Chromium	Cr	sol	52.0		23.6	298 - 2130	20.3	12.1	30.0		
	Crliq	liq		16 900	31.6	2130 - 2945			39.3		
Chromium(III)-oxide	$Cr_2O_3$	sol	152.0	-1 139 701	81.2	298 - 2603	114.8	11.2	131		
Iron-chrome spinel chromite	$Fe [Cr_2O_4]$	sol	223.8	-1 458 124	142.0	298 - 2123	140.1	35.5	183		
Copper	Cu	sol	63.5		33.2	298 - 1358	22.0	7.4	28.0		
	Culiq	liq		13 138	42.8	1358 - 2843			32.8		
Copper(I)-oxide, cuprite	$Cu_2O$	sol	143.1	-170 707	92.3	298 - 1508	56.4	25.8	79.7		
	$Cu_2O$ liq	liq		-105 939	135.0	1508 - 2000			99.9		
Copper(II)-oxide, tenorite	CuO	sol	79.5	-156 063	42.6	298 - 1397	40.8	13.9	48.6		
Chalcopyrite	$CuFeS_2$	sol	183.5	-190 372	125.0	298 - 830	78.6	63.6	114		
Cu(I)-sulfide, chalcocite	$Cu_2S$	sol	159.1	-81 170	116.2	298 - 1400	47.9	97.2	85.7		
Cu-Matte	$Cu_2S$ liq	liq		-68 325	125.3	1400 - 2000			89.7		
Cu(II)-sulfide, covellite	CuS	sol	95.6	-53 095	66.5	298 - 1300	44.4	11.0	53.0		
Hydrogen	$H_2$	gas	2.0		130.7	298 - 5000	28.2	2.7	35.0		
Iron	Fe	sol	55.8		27.3	298 - 1811	23.1	16.0	38.7		
	Fe liq	liq		13 807	34.9	1811 - 3158			45.0		
Iron(II)-oxide, wüstite	FeO	sol	71.8	-267 270	57.6	298 - 1650	47.9	10.7	58.0		
	FeO liq	liq		-243 212	72.2	1650 - 3687			68.2		
Iron(II)(III)-oxide, magnetite	$Fe_3O_4$	sol	231.5	-1 118 383	146.1	298 - 1870	75.5	240.1	207		
Iron-iron spinel Fe [Fe <sub>2</sub> O <sub>4</sub> ]	$Fe_3O_4$ liq	liq		-980 311	220.0	1870 - 2000			213		
Iron(III)-oxide, hematite	$Fe_2O_3$	sol	159.7	-824 248	87.4	298 - 1700	78.1	99.8	142.0		
Iron carbonate, siderite	$FeCO_3$	sol	115.9	-740 568	92.9	298 - 800	48.7	112.1	106.0		
Iron sulfide, pyrrhotite	FeS	sol	87.9	-105 441	60.8	298 - 1465	31.0	63.0	68.0		
Fe-Matte	FeS liq	liq		-72 977	82.3	1465 - 3000			62.6		
Iron sulfide, pyrite	$FeS_2$	sol	120.0	-171 544	52.9	298 - 1000	56.0	27.8	73.0		
Lead	Pb	sol	207.2		64.8	298 - 600	24.2	8.7	28.1		
	Pb liq	liq		4 770	72.7	600 - 1200			29.7		
Lead oxide, litharge	PbO	sol	223.2	-218 062	68.7	298 - 1159	41.8	16.1	53.1		
	PbO liq	liq		-192 540	90.7	1159 - 2000			65.0		
Lead sulfide, galena	PbS	sol	239.3	-98 634	91.3	298 - 1386	46.6	9.5	54.0		
	PbS liq	liq		-79 806	104.9	1386 - 2000			66.9		
Lead sulfate, anglesite	$PbSO_4$	sol	303.3	-923 137	149.5	298 - 1139	66.5	110.0	144.0		
Magnesium	Mg	sol	24.3		32.7	298 - 922	21.4	11.8	28.5		
	Mg liq	liq			8 954	42.4	922 - 1361			32.6	
	Mg gas	gas		146 440	148.6	1361 - 2000			20.8		
Mg-carbonate, magnesite	$MgCO_3$	sol	84.3	-1 095 798	65.7	298 - 700	47.8	99.0	94.0		
Mg-oxide, periklase	MgO	sol	40.3	-601 241	26.9	298 - 3105	42.8	6.0	53.0		



## METALLURGICAL THERMODYNAMICS

Variable, constant or function		Unit of measurement			
t	time	s	second	=	1 / 60 min
	also measured in	1 h	hour	=	3600 s
	also measured in	1 d	day	=	24 h
m	mass	SI	1 kg	=	1000 g
	also	1 t		=	1000 kg
n	mole	for chemical calculations	mol	=	m / M mol
M	Mole mass	tabulated	g / mol		
V	volume	1 m <sup>3</sup>	cubicmeter	=	1000 L liter
V <sub>mol</sub>	mol volume	volume occupied by 1 mol of an ideal gas at 273 K			= 22.4 L / mol
d	density	= m / V	mass / volume	t / m <sup>3</sup>	kg / L
		density of water at 4°C			= 1 kg / L
p	pressure	SI	1 Pa	Pascal	1 N / m <sup>2</sup>
	old but useful	1 atm	atmosphere	=	101 325 Pa
T	temperature	also measured in °C	K	Kelvin	= 273 + °C
E	energy	E <sub>me</sub>	mechanical	1 Nm	Newtonmeter
		E <sub>mv</sub>	volume work pV	1 atm x L	Literatmosphere
		E <sub>th</sub> or Q	thermal	1 J	Joule
		E <sub>el</sub>	electrical	1 Ws	Wattsecond
P	power	= energy / time	1 J/s		
H <sub>T</sub>	enthalpy	heat content at constant pressure			J / mol
S <sub>T</sub>	entropy	= Q <sub>rev</sub> / T		J / (mol K)	= U + pV
G° <sub>T</sub>	Gibbs free energy	= H° <sub>T</sub> - T S° <sub>T</sub>		J / mol	under standard conditions
G <sub>T</sub>		= G° <sub>T</sub> + RT ln K		J / mol	under non-standard conditions
H° <sub>298</sub> S° <sub>298</sub> G° <sub>298</sub>		enthalpy, entropy or free energy values under standard conditions at room temperature			
ΔH ΔS ΔG		change of enthalpy, entropy or Gibbs free energy in reactions			
ΔH° <sub>T</sub> ΔS° <sub>T</sub> ΔG° <sub>T</sub>		change of enthalpy, entropy or Gibbs free energy under standard conditions at temp. T			
ΔG <sub>T</sub>		= ΔG° <sub>T</sub> + R T ln K = ΔH° <sub>T</sub> - TΔS° <sub>T</sub> + RT ln K			General reaction isotherm
K	equilibrium constant			no units	II products / II reactants
C ≡ C <sub>p</sub>	heat capacity	at constant pressure		J / (mol K)	
C <sub>T</sub>	molar h.c. at T	= ∫ (a + b10 <sup>-3</sup> T) dT		J / (mol K)	to be integrated from T <sub>lo</sub> to T <sub>hi</sub>
C <sub>mean</sub>	mean h.c.	= Q / ΔT		J / (mol K)	valid over entire temperature interval
R	universal gas constant		8.314 J / (mol K)		
F	Faraday constant	96 484 Cb / mol = As / mol			26.8 Ah/mol
N <sub>A</sub>	Avogadro Number	number of particles or molecules per mole of matter			= 6E+23 / mol
Oxygen in air	oav =	21.0% by volume		oam	= 23.2% by mass
Water	M =	18.0 g / mol	1 L = 1 kg		55.5 mol/L
Consumption of electrical energy		1 kWh	= 1000 × 3600 Ws = J		3.6 MJ
μ	10 <sup>-6</sup>	micro	e.g. 1 μL	microliter	= 10 <sup>-6</sup> L
m	10 <sup>-3</sup>	milli	1 ms	millisecond	= 10 <sup>-3</sup> s
	10 <sup>0</sup> = 1	unit			
k	10 <sup>3</sup>	kilo	1 km	kilometer	= 10 <sup>3</sup> m
M	10 <sup>6</sup>	mega	1 Mg	megagram	= 10 <sup>6</sup> g
G	10 <sup>9</sup>	giga	1 GJ	gigajoule	= 10 <sup>9</sup> J