



## FACULTY OF SCIENCE

### ACADEMY OF COMPUTER SCIENCE AND SOFTWARE ENGINEERING

<b>MODULE</b>	<b>GRAPHICS IT18X77</b>
<b>CAMPUS</b>	AUCKLAND PARK CAMPUS (APK)
<b>FSAO SSA</b>	JULY
<b>DATE:</b> 2020-07	<b>SESSION:</b> Morning
<b>ASSESSOR(S):</b>	<b>MR. A. MAGANLAL</b>
<b>MODERATOR:</b>	<b>DR. D VOGTS (NMU)</b>
<b>DURATION:</b> 120 MINUTES	<b>MARKS:</b> 100

Please read the following instructions carefully:

1. Answer **all** the questions.
  2. Answer questions in order.
  3. Answer only in the answer sheets provided.
  4. Use diagrams where necessary to assist in your explanations.
  5. Non-programmable calculators are allowed.
  6. Round final answers to three decimal places.
  7. Write *cleanly* and *legibly*.
  8. This paper contains **6** question(s).
  9. This paper consists of **2** page(s).
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**QUESTION 1: Rotation Calculation**

Answer only one part. Either **Matrix** or **Quaternion**

**(a) Matrix**

Construct a matrix to rotate  $347^\circ$  (clockwise) around the axis specified by

$$(-11, 6, 22) \rightarrow (-3, 0, 17)$$

Rotate the point  $(22, 0, 3)$  around this axis.

**(b) Quaternion**

Construct a quaternion to rotate  $347^\circ$  (clockwise) about the axis  $(8, -6, -5)$ .

Use the quaternion to rotate  $(33, -6, -19)$  around this axis.

<b>Total: 15</b>
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**QUESTION 2: Lighting Equation**

Write down the Phong lighting equation for a single colour light source and object (black and white model). Now calculate the viewed intensity of a point on an object given the following attributes:

- The object is not emissive at all.
- The ambient light intensity is 0.214.
- The object has an ambient coefficient of 0.936.
- The object has a diffuse reflection coefficient of 0.745.
- The object has a specular reflection coefficient of 0.996.
- The shininess (specular highlight) factor is 3.
- The intensity of the incoming light (both specular and diffuse) is 0.401.
- The point we are considering is  $(4, -11, -6)$ .
- The normal at the surface is  $(-0.624242, 0.780303, 0.0380749)$ .
- The light is positioned at  $(1, -8, 12)$ .
- The viewer is positioned at  $(-6, 2, 16)$ .

<b>Total: 15</b>
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**QUESTION 3: Proof**

(a) **Provide** the *formula* for a **Bézier curve of degree three (3)** [05]

(b) **Show** that a **Bézier curve of degree three (3)** is affine invariant. [10]

<b>Total: 15</b>
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**QUESTION 4: Ray Tracing Intersection**

(a) Describe how to calculate the intersection point between a ray described by  $\mathbf{o} + t\mathbf{d}$  (where  $\mathbf{d}$  is a unit vector) and a sphere described by  $(x - c_x)^2 + (y - c_y)^2 + (z - c_z)^2 = r^2$ . [08]

(b) How will you determine if the ray is entering or exiting the sphere? [02]

<b>Total: 10</b>
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**QUESTION 5: Rasterisation vs Ray Tracing**

**Discuss** how *forward shading rasterisation* and *naive recursive ray tracing* differ in terms of application of realistic lighting. Your discussion should include how *visibility* is calculated, how reflection/refraction is computed and the relative speed of the technique.

Total: 20
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**QUESTION 6: Application**

A still image of an *theater stage* is to be rendered. The stage is lit by an array of spot lights, directly above the stage. Rasterisation was selected as a method for rendering the scene. Answer the questions that follow:

- (a) **Provide** a *definition* for *global lighting model*. [05]
- (b) **Discuss** how *radiosity* works. Your discussion must include details of patches, form factors and methods for solving radiosity as well as how radiosity can be integrated into the rasterisation process. [15]
- (c) **Discuss** why *radiosity* should be used to render the scene as opposed to *photon mapping*. [05]

Total: 25
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